Necessarily Transient Quantum Refrigerator

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February 28, 2017

SD, Avijit Misra, Amit Kumar Pal, Aditi Sen (De), Ujjwal Sen arXiv:1606.06985

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February 28, 2017

- Introduction to quantum refrigerator and its working principle
- A thermalization model: Reset model

Necessarily transient cooling in Reset model

- Harmonic oscillator bath model of thermalization
- Info-theoretic aspects of necessarily transient cooling
- Remarks

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- Quantum thermal machine. Working substance is quantum object.
- Small self-contained quantum refrigerator. Each subsystem has a few quantum levels.



At
$$t = 0$$
,
 $T_C \leq T_R \leq T_H$ We take, $T_C = T_R = T_r$
 $\rho_0 = \rho_0^C \otimes \rho_0^R \otimes \rho_0^H$ $\rho_0^i = r_i |0\rangle \langle 0| + (1 - r_i) |1\rangle \langle 1|$
 $r_i = \frac{1}{1 + e^{-E_i/T_i}}, \ i = C, R, H$
 $H_{loc} = \frac{1}{2} \sum E_i \sigma_i^z$,

Sreetama Das

February 28, 2017 5 / 28

Inter-qubit interaction : $H_{int} = g(|010\rangle \langle 101| + |101\rangle \langle 010|)$

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Initially,
$$(1 - r_C)r_R > r_C(1 - r_R)$$

Probability of $|10\rangle$ > Probability of $|01\rangle$

• Apply an unitary operation U: $|10\rangle \rightarrow |01\rangle$ Extra work $(E_R - E_C)$ performed by the external system.

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To cool qubit C, $|101\rangle \longrightarrow |010\rangle$

Choose $T_H > T_r$,

Probability of $|101\rangle$ > Probability of $|010\rangle$

Master equation:

$$\frac{\partial \rho(t)}{\partial t} = -\frac{i}{\hbar} [H_{loc} + H_{int}, \rho(t)] + \Phi(\rho(t))$$

 $\Phi(\rho)$ depends on nature of reservoir, & interaction between qubits & reservoirs.

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$$\Phi(\rho) = \sum_{i=1}^{3} p_i(\rho_0^i \otimes Tr_i\rho(t) - \rho(t))$$

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$$T_C(t) = -E_C / \ln\left(\frac{1 - r_C(t)}{r_C(t)}\right)$$

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• This minimum temperature T_{min} is roughly independent of the p_i 's.

$$\begin{split} E_C &= 1, E_H = 100 \\ T_C &= T_R = 1, T_H = 100 \\ g &= 5 \times 10^{-3}, p_C = p_H = \\ 10^{-5}, p_R &= 10^{-3} \end{split}$$

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Canonical Interaction Parameters:

$$p_C = 10^{-x}, \quad p_R = 10^{-(x+y)}, \quad p_H = 10^{-(x-y)}, \quad x, y > 0$$

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Canonical Interaction Parameters:

 $E_C = 1, E_R = 101, E_H = 100$ $T_C = T_R = 1, T_H = 100$ x = 3.5, y = 2.5

$$p_C = 10^{-x}, \quad p_R = 10^{-(x+y)}, \quad p_H = 10^{-(x-y)}, \quad x, y > 0$$



• T_C decreases with time and after attaining a minimum temperature at a very short time, it starts to increase. The steady state temperature $T_C^S \approx T_C$





 T_1^S : Steady state temp. of $C,\,\delta:T_C-T_1^S$ $T_{min}=minT_C$

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Observations

- In a large area of this region, T_1^S is very near or equal to the initial temperature T_1
- \bullet So, the steady state cooling δ is negligible in those areas.
- T_{min} has low value in those regions.
- TC without SSC is rich in the first quadrant **R** of x y space.
- With increasing g, area of such region in ${f R}$ increases.
- With increasing g, T_{min} decreases.

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Bath hamiltonian:

$$H_b = \sum_{i=1}^{3} \hbar \omega_{i,k} b_{i,k}^{\dagger} b_{i,k}$$

 $\frac{\text{Memoryless qubit-bath interaction}}{\text{collection of harmonic oscillators.}}: Each qubit in contact with a$

Bath hamiltonian:

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Bath-qubit interaction:

$$H_{sb} = \sum_{i=1}^{3} A_i \otimes \chi_i$$

 $A_i = \sigma_i^x$: Lindblad operator, $\chi_i = \sum_{i=1}^3 (\eta_{i,k} b_{i,k} + \eta_{i,k}^* b_{i,k}^{\dagger})$: Collective bath co-ordinates

18 / 28

$$H_{total} = H_{local} + H_{int} + H_b + H_{sb} , \qquad g \gtrsim E_i$$

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19 / 28

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$$\Phi(\rho) = \sum_{i,w} \gamma_i(\omega) \varphi_i^{\omega}(\rho)$$

$$\gamma_i(\omega) = \begin{cases} J_i(\omega)(1 + f(\omega, \beta_i)), & \omega > 0, \\ J_i(|\omega|)f(|\omega|, \beta_i), & \omega < 0. \end{cases}$$

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Necessarily Transient Quantum Refrix February 28, 2017 19 / 28

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 $J_i(\omega) = \alpha_i \omega \exp(-\omega/\Omega)$: Spectral function of the bath

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 $J_i(\omega) = \alpha_i \omega \exp(-\omega/\Omega)$: Spectral function of the bath $f(\omega, \beta) = (\exp(\hbar\beta\omega) - 1)^{-1}$: Bose-Einstein distribution

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$$\begin{split} J_i(\omega) &= \alpha_i \omega \exp(-\omega/\Omega): \text{ Spectral function of the bath} \\ f(\omega,\beta) &= (\exp(\hbar\beta\omega)-1)^{-1}: \text{ Bose-Einstein distribution} \\ \varphi_i^\omega(\rho) &= \mathcal{L}_i^\omega \rho \mathcal{L}_i^{\omega\dagger} - \frac{1}{2} \mathcal{L}_i^{\omega\dagger} \mathcal{L}_i^\omega, \rho \end{split}$$

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Canonical Interaction Parameters: $\alpha_C = 10^{-x}, \alpha_R = 10^{-(x+y)}, \alpha_H = 10^{-(x-y)}$ Canonical Interaction Parameters: $\alpha_C = 10^{-x}, \alpha_R = 10^{-(x+y)}, \alpha_H = 10^{-(x-y)}$



• For low values of g, T_C^S is lower than T_C but with increasing g, T_C^S increases and eventually crosses T_C .

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- For low values of g, T_C^S is lower than T_C but with increasing g, T_C^S increases and eventually crosses T_C .
- Minimum temperature however lower than T_C , and obtained at a significantly low time.

Harmonic oscillator bath model of thermalization



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- The minimum temperature obtained remains almost same over the entire region, variation occuring in the fourth decimal place.

28

Harmonic oscillator bath model of thermalization



- Steady state heating takes place all over the parameter space. So, transient cooling is the only option to cool.
- The minimum temperature obtained remains almost same over the entire region, variation occuring in the fourth decimal place.
- Necessary transient cooling is generic: occurs irrespective of thermalization model.

21 / 28

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Behavior of logarithmic negativity



Figure : for Reset model

$$E_C = 1, E_R = 101, E_H = 100$$
$$T_C = T_R = 1, T_H = 100$$
$$x = 3.5, y = 2.5, g = 10^{-2}$$

• Throughout the region **R**, LN is considerably low or zero.

Behavior of logarithmic negativity



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- The ordering between LN^m_{1:23} and LN^m_{3:12} remains unchanged but that between LN^m_{1:23} and LN^m_{2:13} is reversed in parts of **R**.

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- LN^m decreases with decreasing g.

In the realistic model, no bi-partition entanglement arises for any set of (x, y) for all t > 0

Behavior of Quantum Discord



• In contrast to LN, QD decreases slowly with time.

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- The maximum value QD^m is higher in the region where T_{min} is lower.
- Unlike LN^m, the ordering between QD^m_{1:23}, QD^m_{3:12} and QD^m_{2:13} remains unchanged throughout **R**.

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- The maximum value QD^m is higher in the region where T_{min} is lower.
- Unlike LN^m, the ordering between QD^m_{1:23}, QD^m_{3:12} and QD^m_{2:13} remains unchanged throughout **R**.
- For fixed bi-partition, value of QD^m is higher than the corresponding value of LN^m.

Behavior of Quantum Discord



• QD is oscillatory at small values of t which dies out with increasing t. Maximum value is reached in the steady state.

$$E_C = 1, E_R = 101, E_H = 100$$
$$T_C = T_R = 1, T_H = 100$$
$$x = 3.5, y = 2.5, g = 0.01$$

Behavior of Quantum Discord



- QD is oscillatory at small values of t which dies out with increasing t. Maximum value is reached in the steady state.
- Takes long time to stabilize: time taken to attain steady state > large-time scale we considered.

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- Higher values of QD is observed in low x and high y regions.

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- Takes long time to stabilize: time taken to attain steady state > large-time scale we considered.
- Higher values of QD is observed in low x and high y regions.
- With increasing g, the higher values of QD are found in high x and low y regions.

Behavior of Quantum Discord



Figure : for the realistic model

$$\begin{split} E_C &= 1, E_R = 101, E_H = 100 \\ T_C &= T_R = 1, T_H = 100 \\ x &= 3.5, y = 2.5, g = 0.01 \end{split}$$

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- Takes long time to stabilize: time taken to attain steady state > large-time scale we considered.
- Higher values of QD is observed in low x and high y regions.
- With increasing g, the higher values of QD are found in high x and low y regions.
- Unlike LN, QD negligible or zero in regions where T_{min} has low value.

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26 / 28

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- In case of the realistic model, transient cooling is even more pertinent as steady state heating occurs.

- A self-contained quantum refrigerator where a transient cooling without steady state cooling is obtained.
- Canonical form of interaction parameters facilitates analysis of necessarily transient cooling.
- Phenomenon generic and independent of specific thermalization model.
- In case of the realistic model, transient cooling is even more pertinent as steady state heating occurs.
- Lowest attainable temperature freezes (remains unchanged) wrt system parameters in realistic model.

26 / 28









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