

# Quantum interference between a single spin excitation and a macroscopic atomic ensemble

**Stefan L. Christensen**, J-B. Béguin, E. Bookjans,  
 H. L. Sørensen, J. Müller, J. Appel and E. Polzik  
 Niels Bohr Institute  
 University of Copenhagen



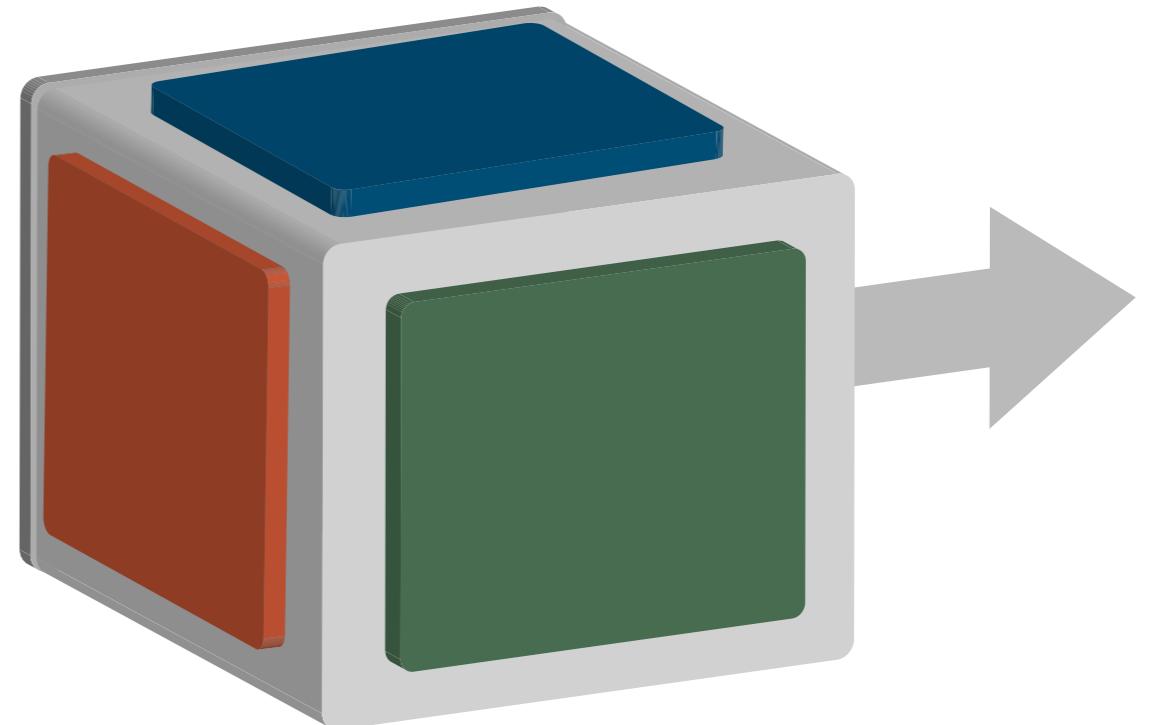
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For quantum science we require on-demand and long lived quantum resources.

Quantum resources should be:

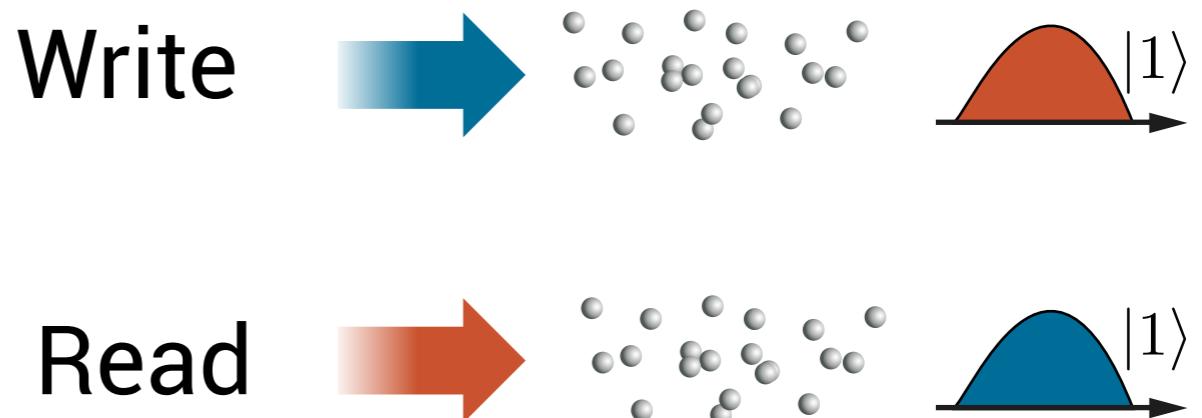
- On-demand.
- Distinct quantum.
- Long lived.



Atom light interfaces have been based on either discrete or continuous approach.

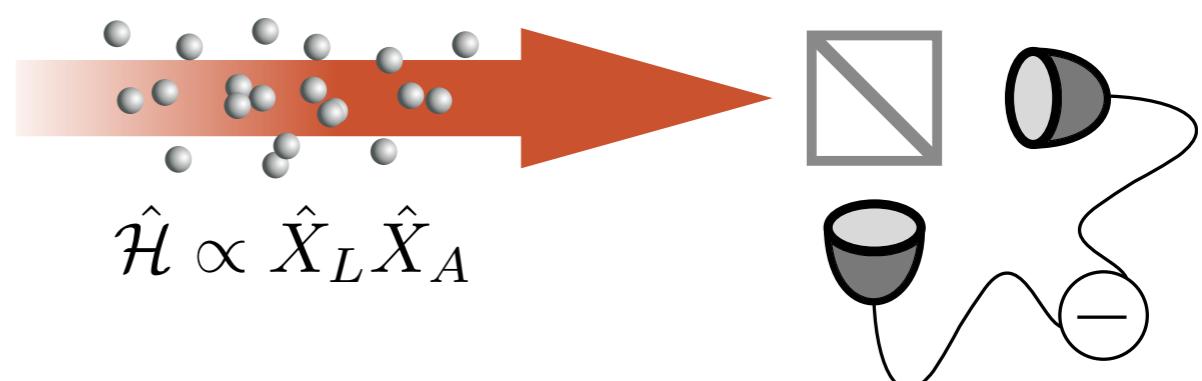
Discrete method uses:

- Fock states.
- Photon counting.



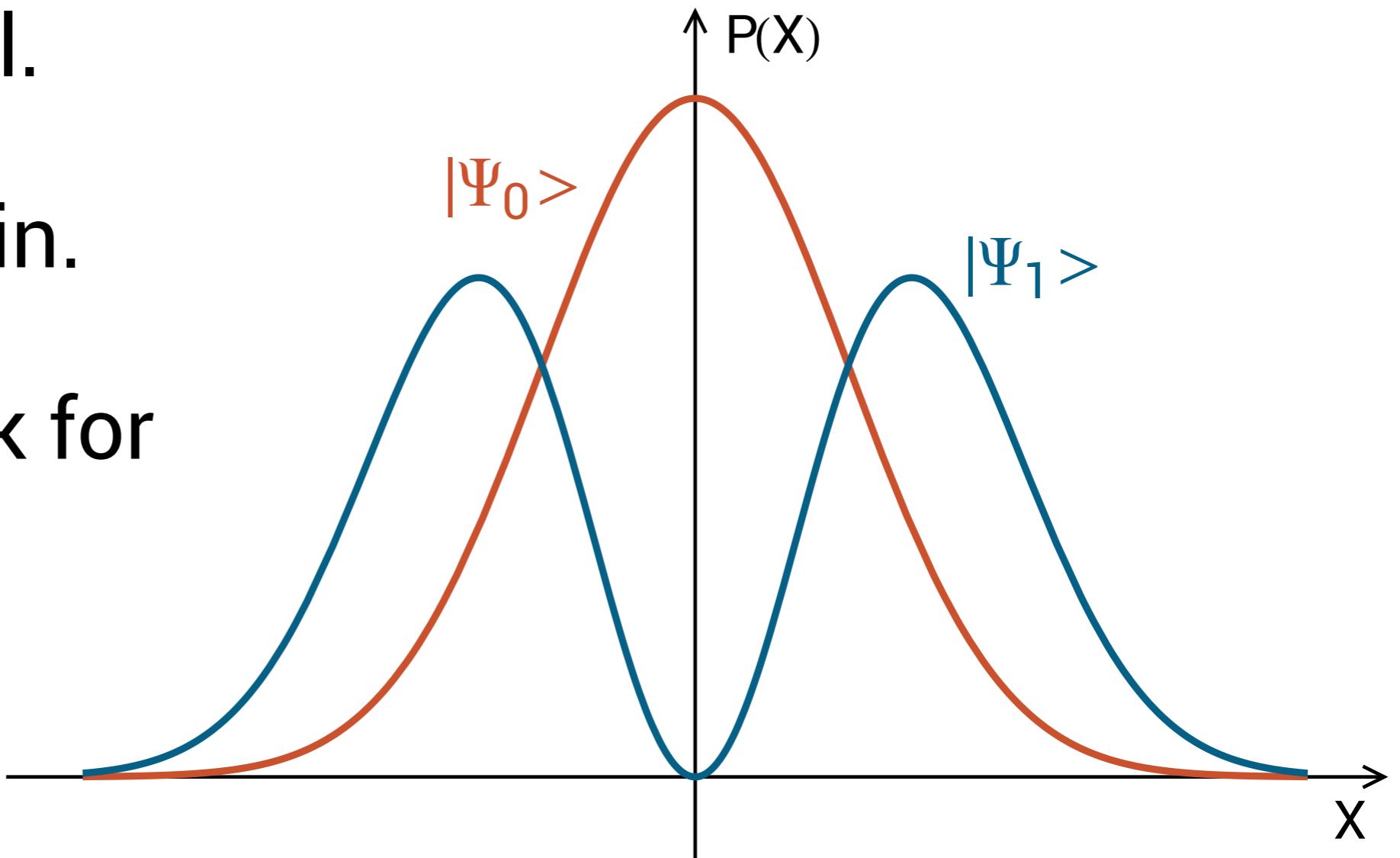
Continuous method uses:

- Gaussian states.
- Homodyne detection.



We will use a hybrid method combining discrete-continuous methods.

- Non-classical.
- Metrology gain.
- Building block for other states.



# Quantum state engineering in an atomic ensemble.



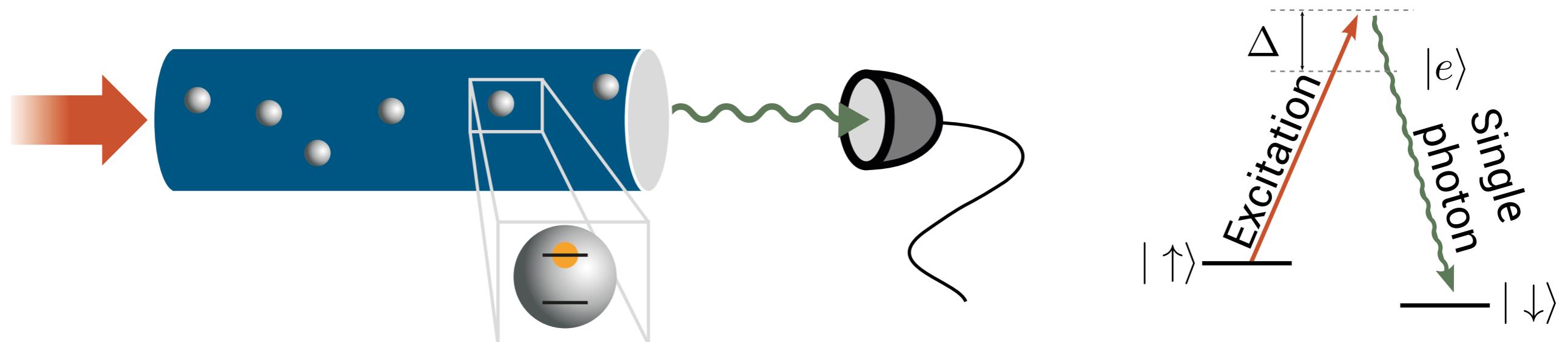
Collective single  
excitation state.

Atomic homodyne  
detection.

Experimental  
implementation.

Results and model.

The state of the atomic ensemble depends on the detection of a photon.



$$|\Psi_0\rangle \equiv |\uparrow\uparrow \dots \uparrow\uparrow\rangle \xrightarrow{\text{Click}} |\Psi_1\rangle \equiv \frac{1}{\sqrt{N_a}} \sum_{l=1}^{N_a} |\underbrace{\uparrow\uparrow \dots \uparrow\downarrow \uparrow\dots \uparrow\uparrow}_{l\text{-th atom}}\rangle$$

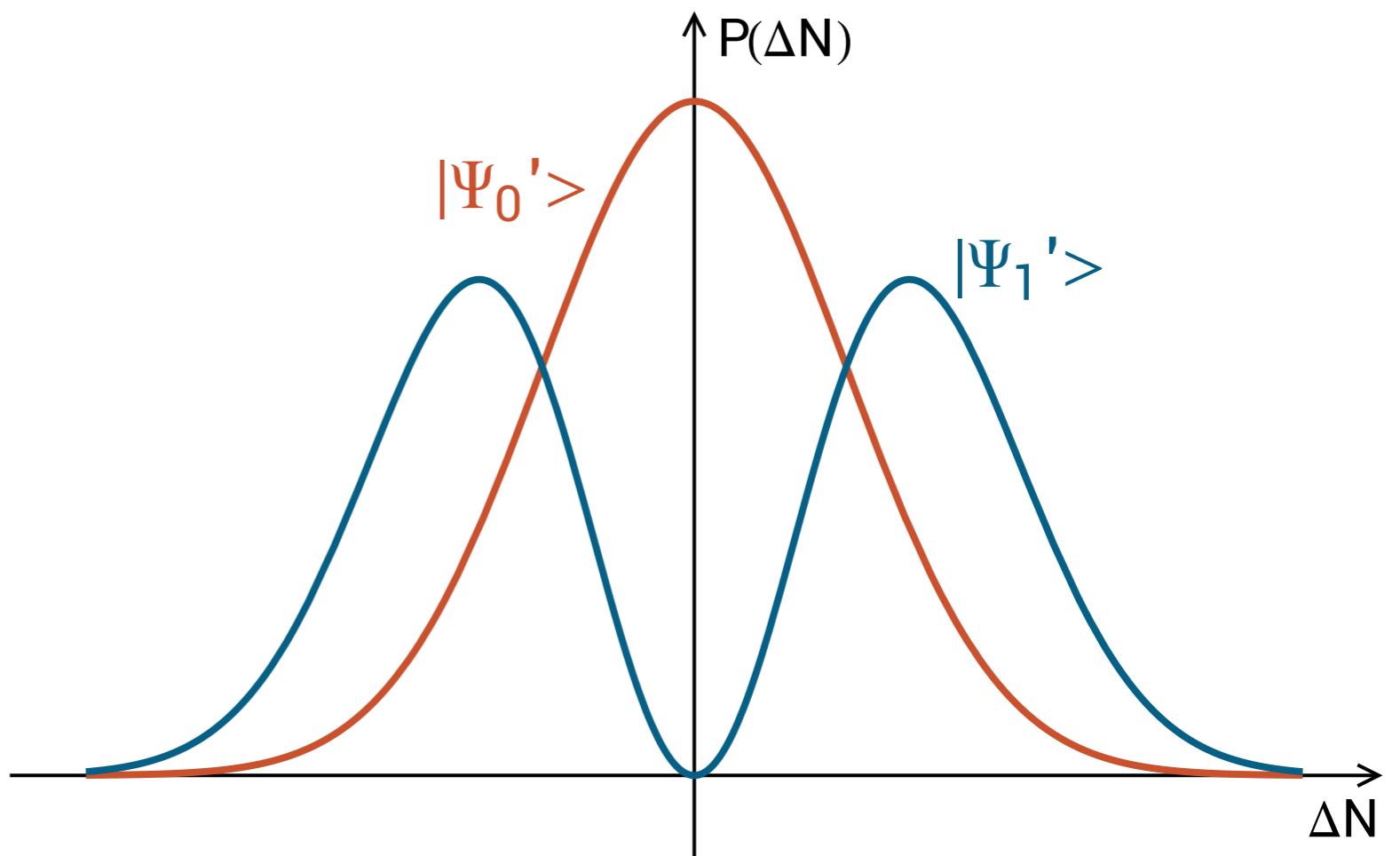
L. Duan et al., Nature (2001)  
S. Christensen et al, NJP (2013)

Rotating the states and measure the population difference.

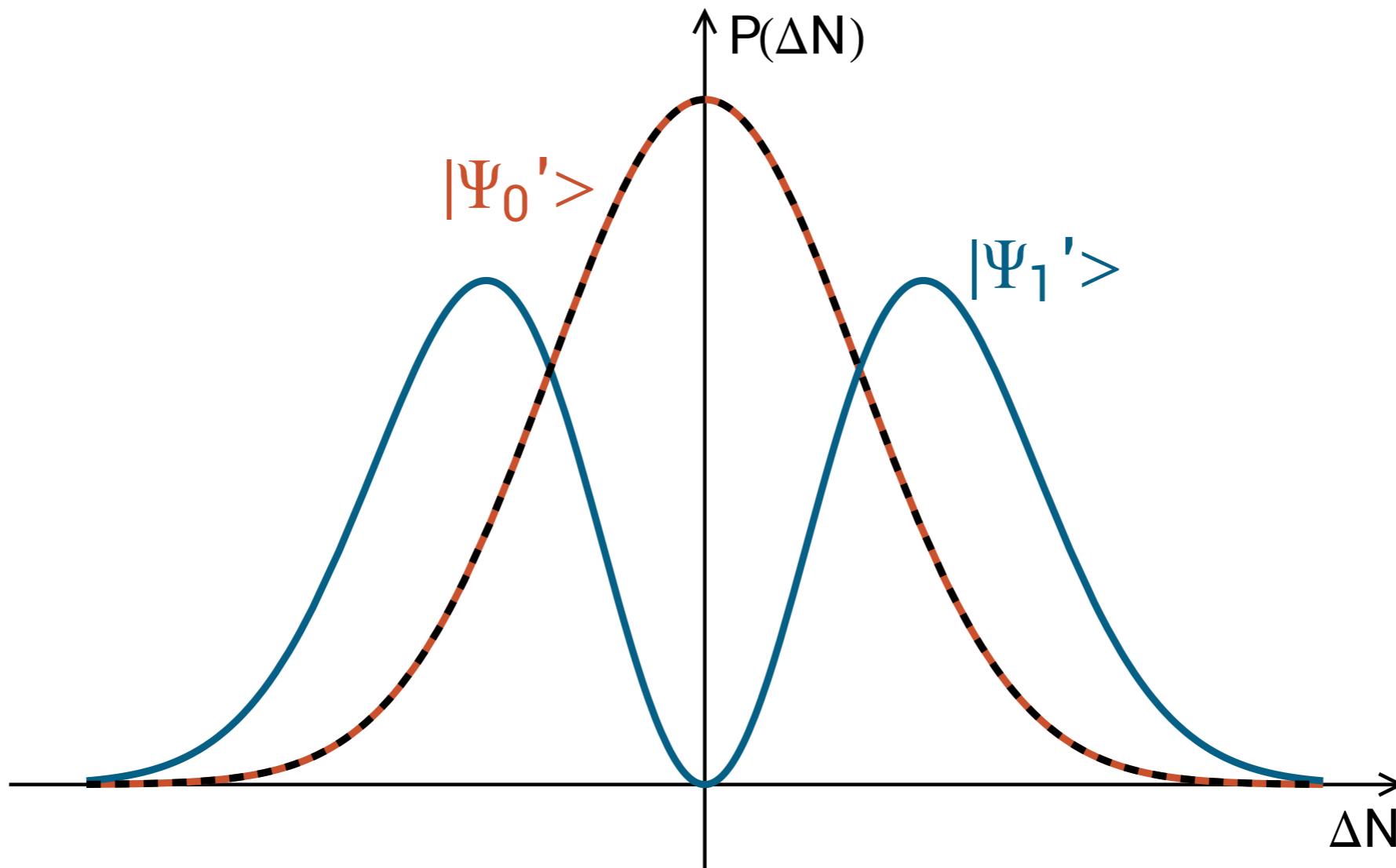
No click:  $|\Psi'_0\rangle \equiv |\leftarrow\leftarrow\dots\leftarrow\leftarrow\rangle$

Click:  $|\Psi'_1\rangle \equiv \frac{1}{\sqrt{N_a}} \sum_{l=1}^{N_a} |\leftarrow\leftarrow\dots\overbrace{\leftarrow\rightarrow\leftarrow\dots\leftarrow\leftarrow}^{\text{$l$-th atom}}\rangle$ .

- Non-Classical.
- Non-Gaussian
- Variance increase by a factor of 3.



If a **specific** atom is flipped,  
no interference effect is observed.



Homodyne detection allows to infer the quantum state.

Describing a state:

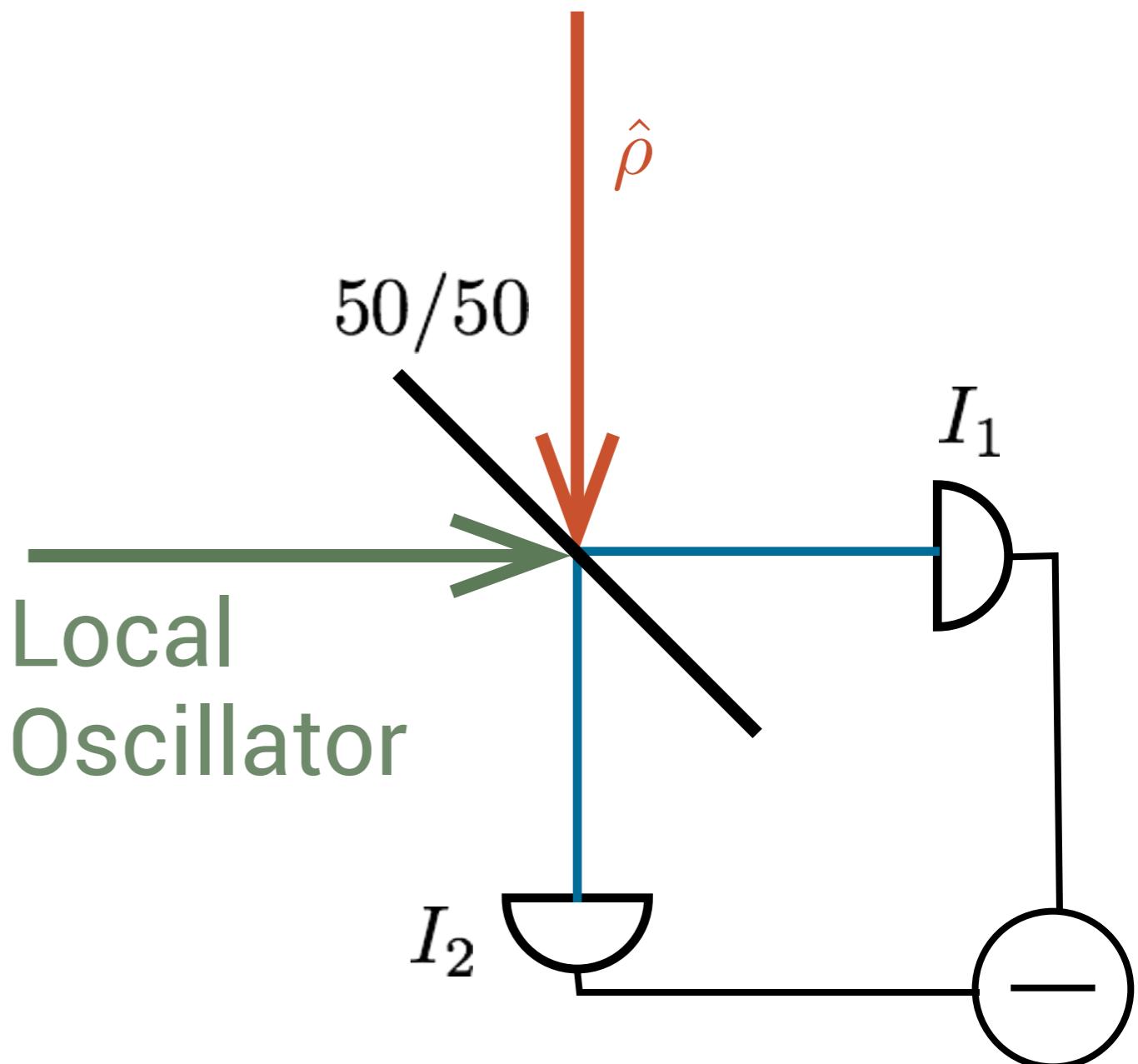
$$\hat{\rho} = ?$$

$$\hat{X}_L^\theta = \sin(\theta)\hat{X}_L + \cos(\theta)\hat{P}_L$$

$$[\hat{X}_L, \hat{P}_L] = i$$

Detection of a state:

$$\Delta I = I_1 - I_2 \propto \hat{X}_L^\theta \rightarrow \hat{\rho}$$



The atomic ensemble can be described by quadrature operators.

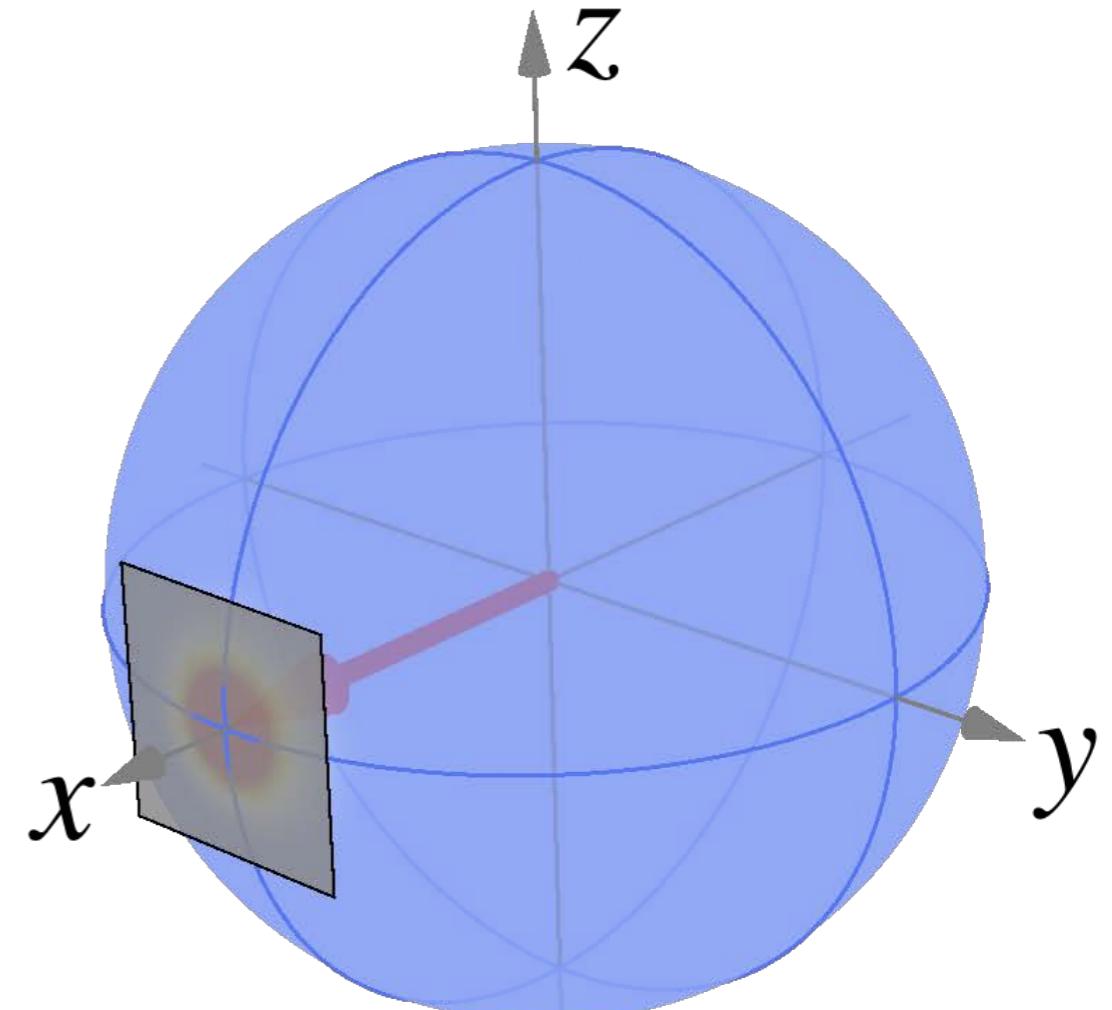
Adding each individual spin gives the total ensemble spin.

$$\hat{J} = \sum_{l=1}^{N_a} \hat{j}^{(l)}, \quad [\hat{J}_y, \hat{J}_z] = i\hat{J}_x$$

Large spin aligned to x-axis

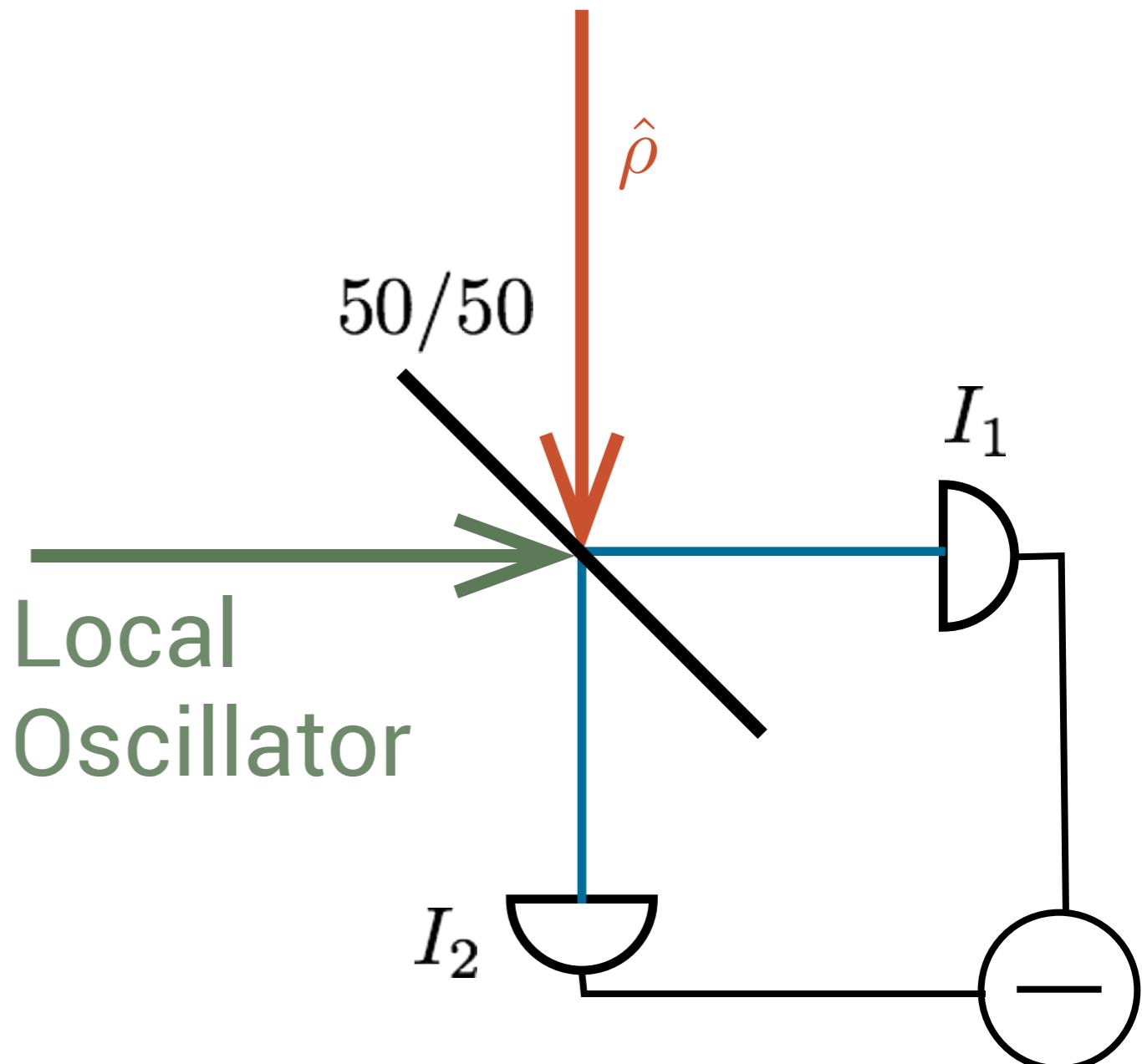
$$\hat{X}_A = \frac{\hat{J}_y}{\sqrt{\langle J_x \rangle}}, \quad \hat{P}_A = \frac{\hat{J}_z}{\sqrt{\langle J_x \rangle}} \propto \Delta N,$$

$$[\hat{X}_A, \hat{P}_A] = i$$



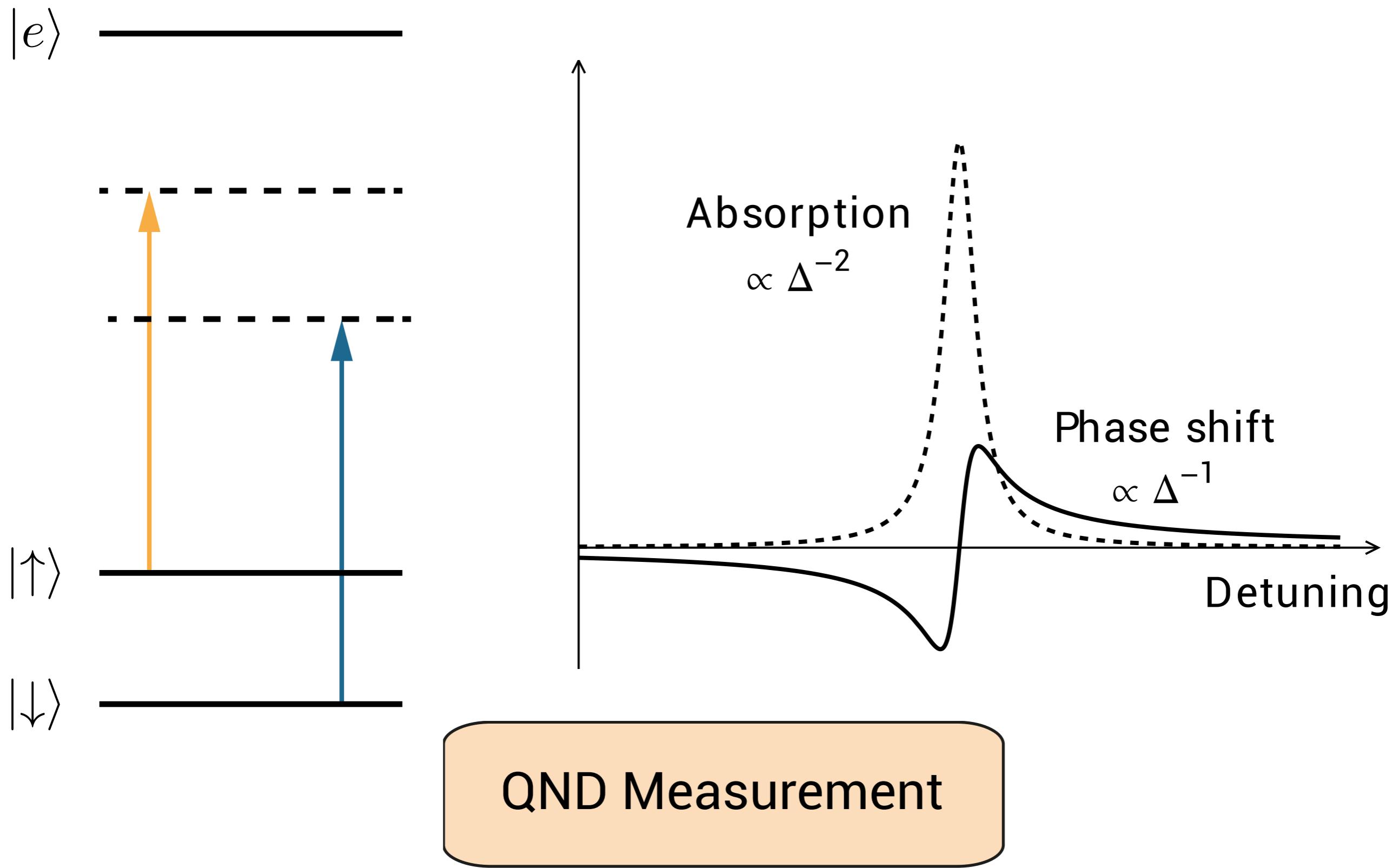
Homodyne detection can also be done with atoms.

- LO: Atoms in  $|\uparrow\rangle$
  - Signal: Atom in  $|\downarrow\rangle$
  - 50/50: Microwave
$$|\downarrow\rangle \rightarrow |\rightarrow\rangle = \frac{|\uparrow\rangle - |\downarrow\rangle}{\sqrt{2}}$$
$$|\uparrow\rangle \rightarrow |\leftarrow\rangle = \frac{|\uparrow\rangle + |\downarrow\rangle}{\sqrt{2}}$$
  - Measure:  $\Delta N = N_\uparrow - N_\downarrow$

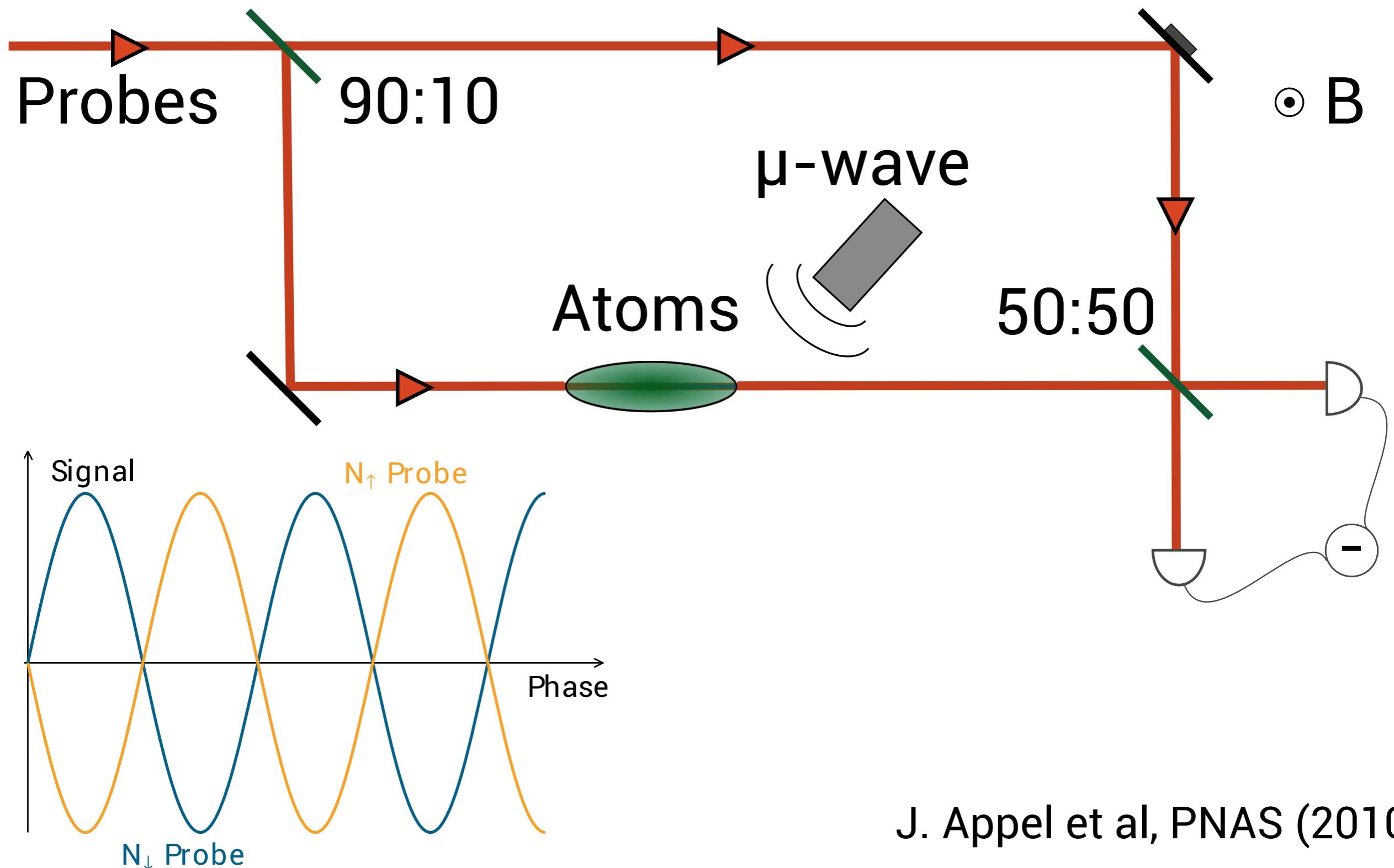


B. Juulsgaard et al., Nature (2001)  
J. Appel et al, PNAS (2010)

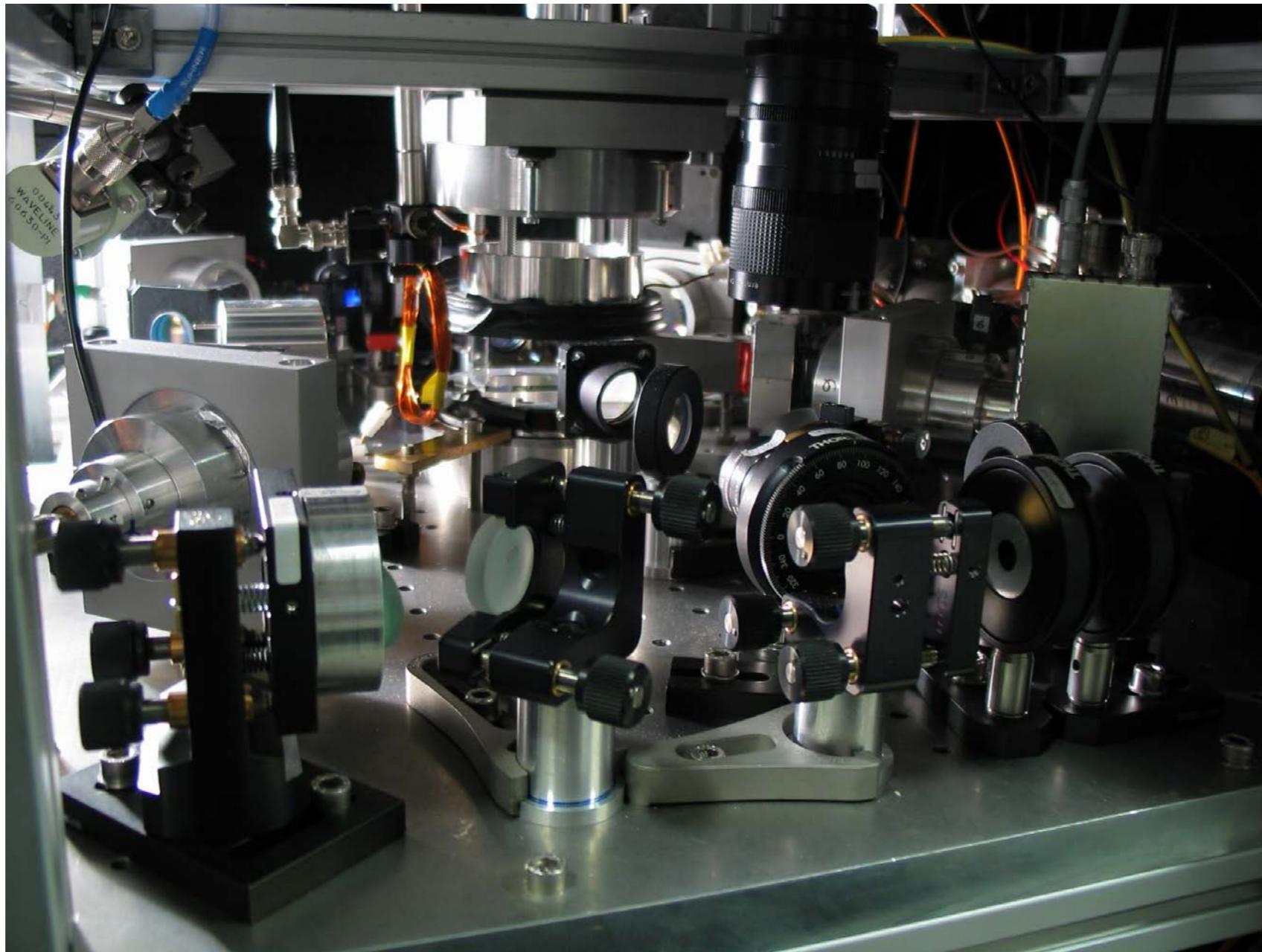
Inferring the population from the phase allows to measure non-destructively.



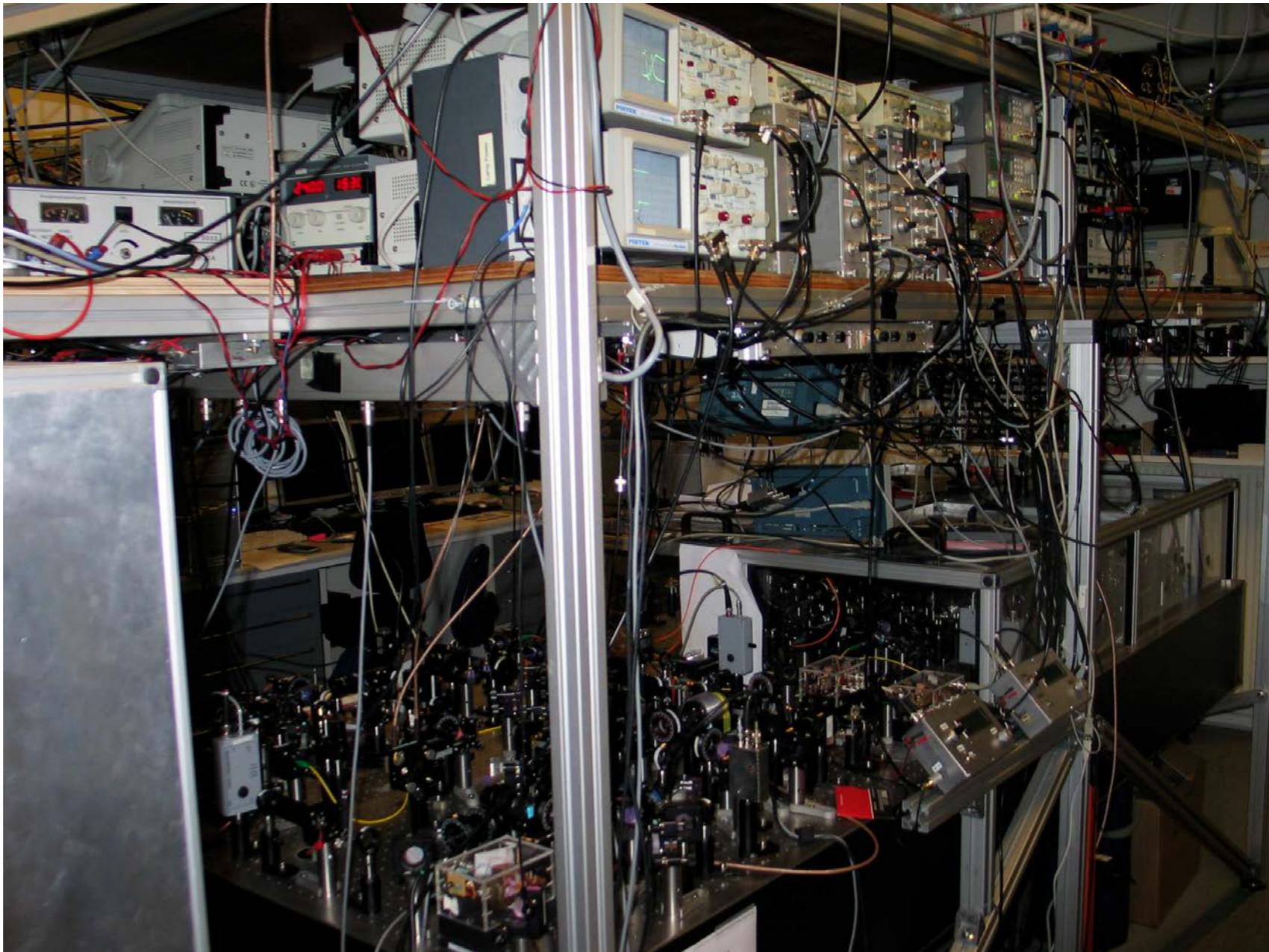
The state dependent phase shift is measured with an interferometer.



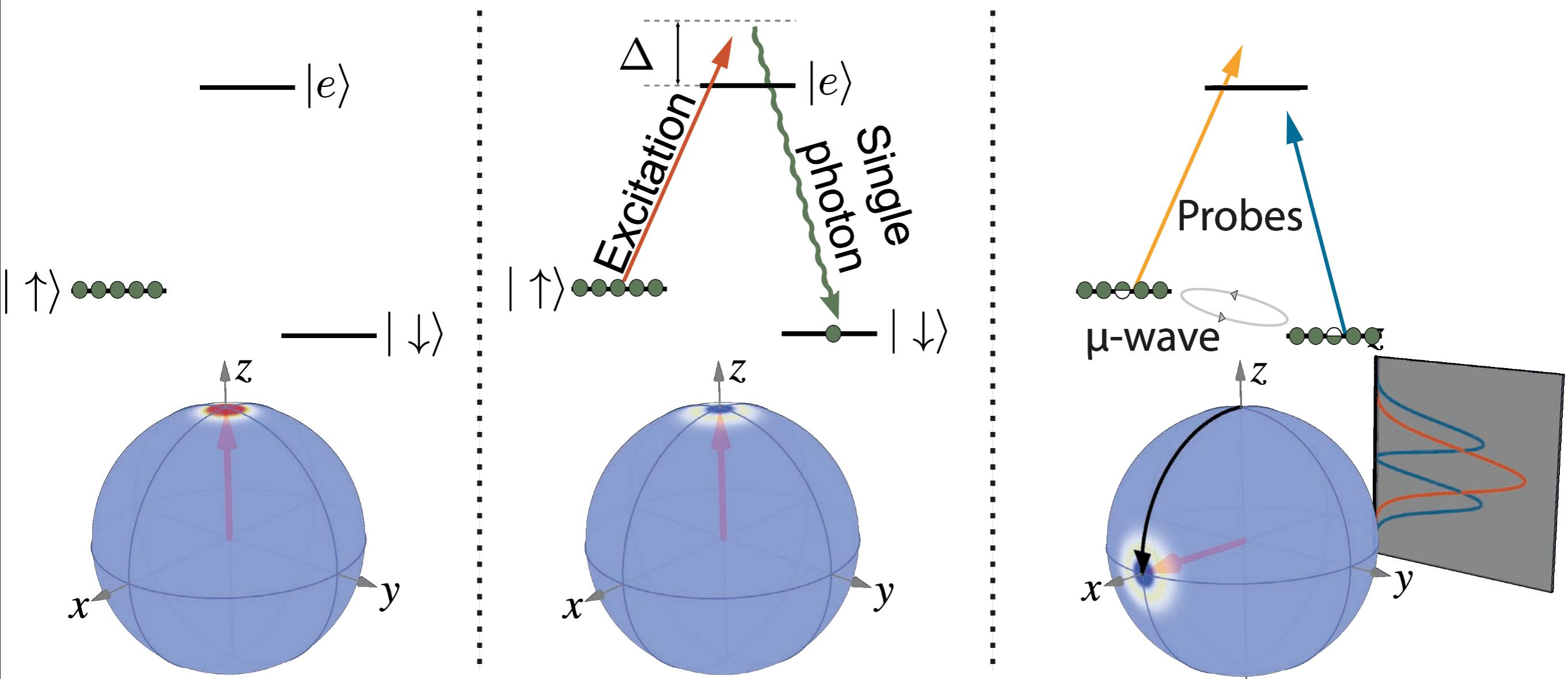
And it actually looks like this.



And it actually looks like this.

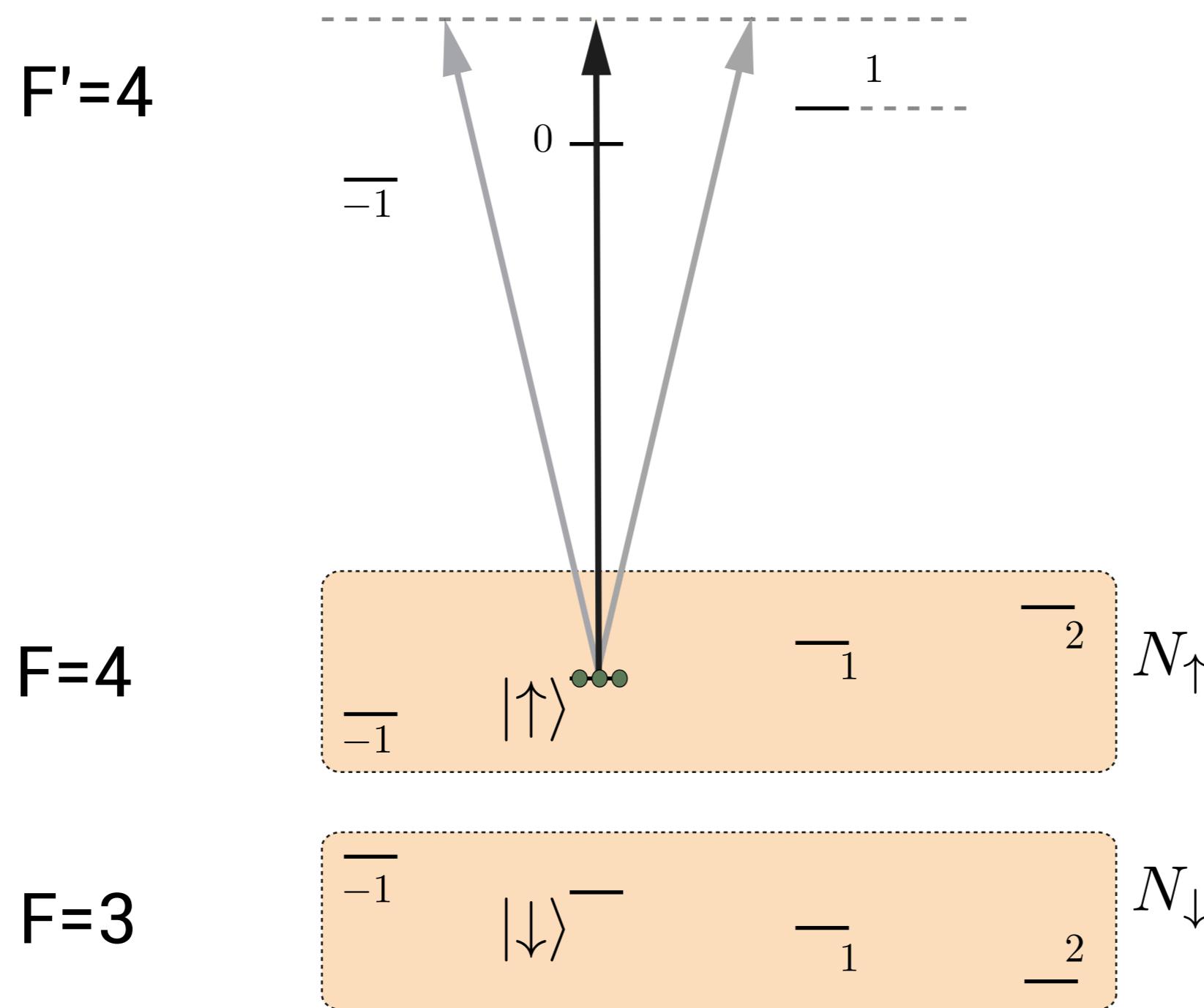


# Single excitation state created via DLCZ protocol and detected by atomic homodyne.

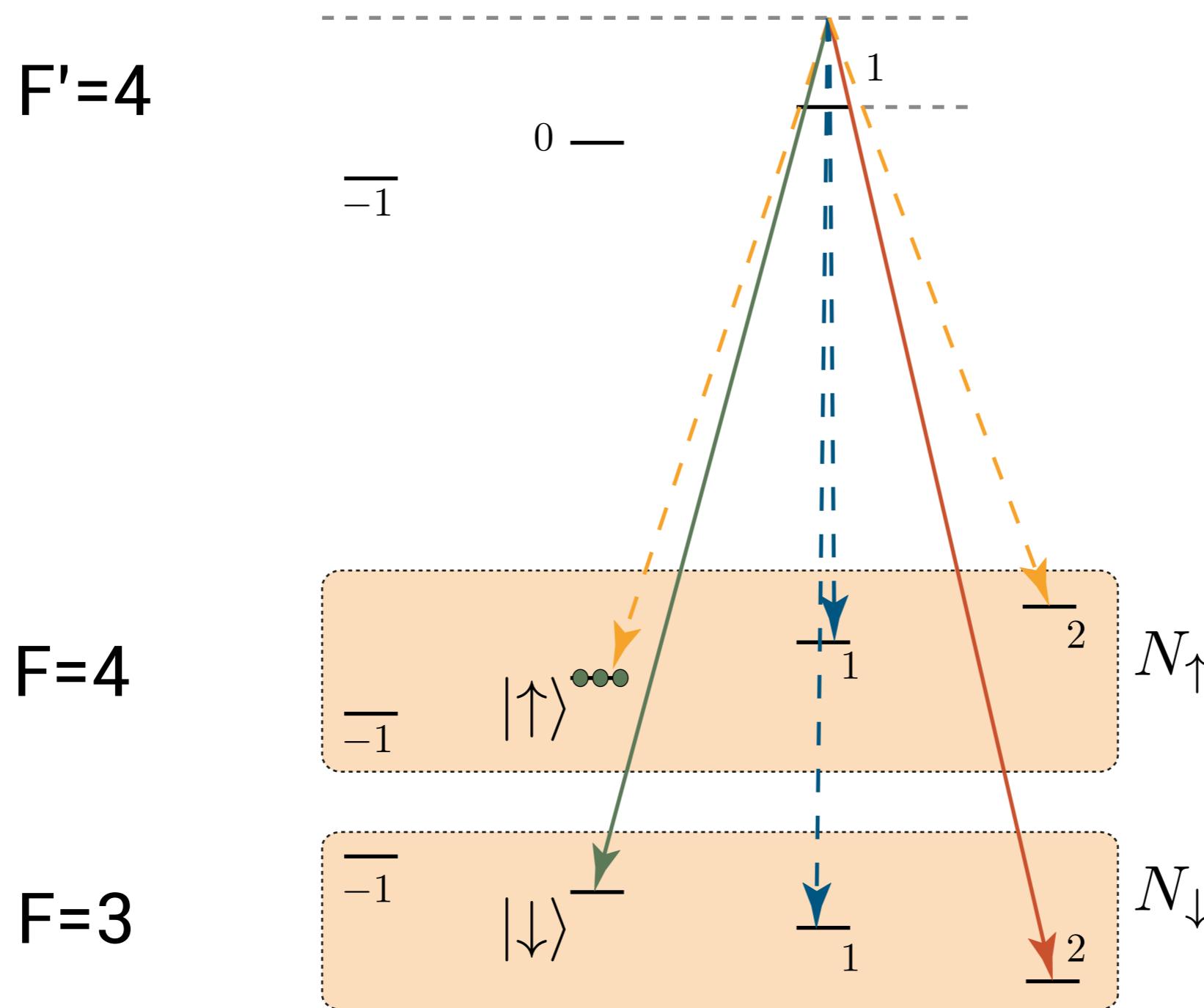


L. Duan et al, Nature (2001)  
S. Christensen et al, NJP (2013)

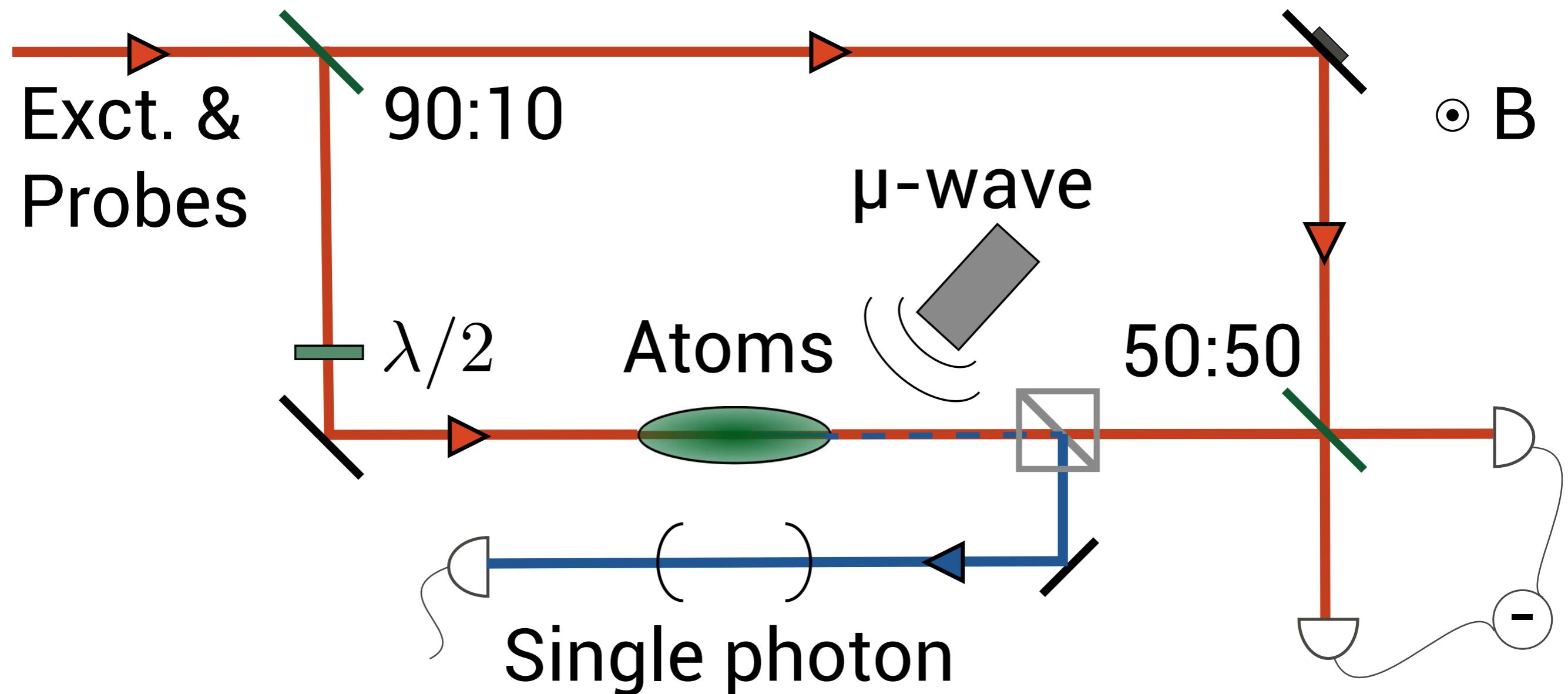
A high magnetic bias field, polarisation and frequency filtering required.



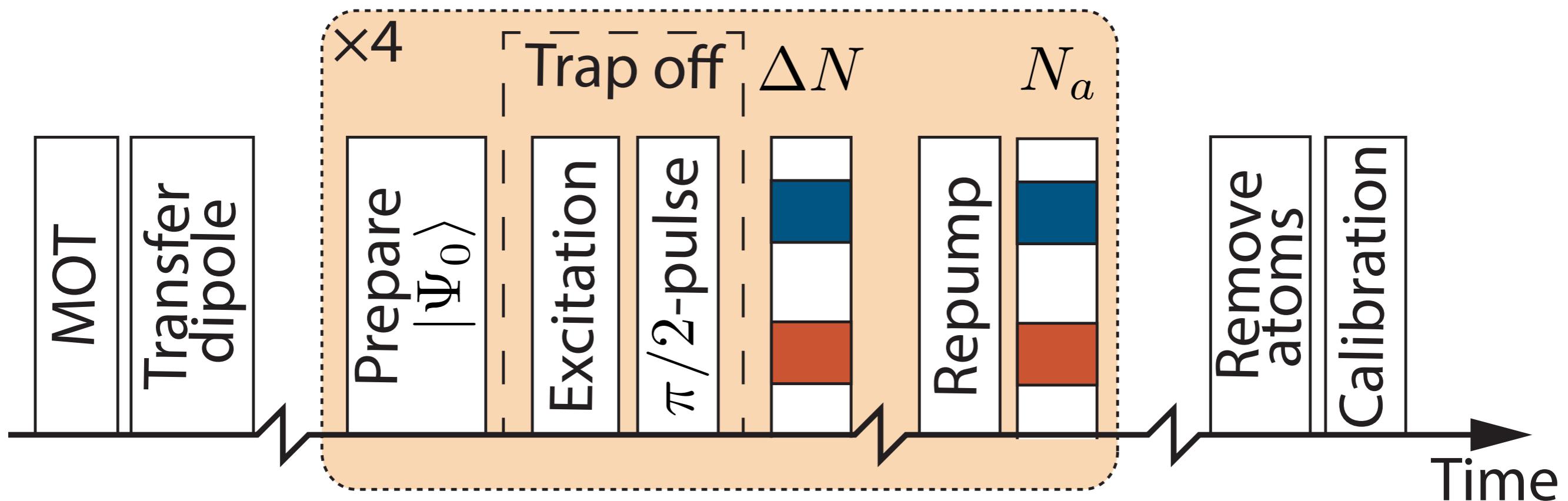
A high magnetic bias field, polarisation and frequency filtering required.



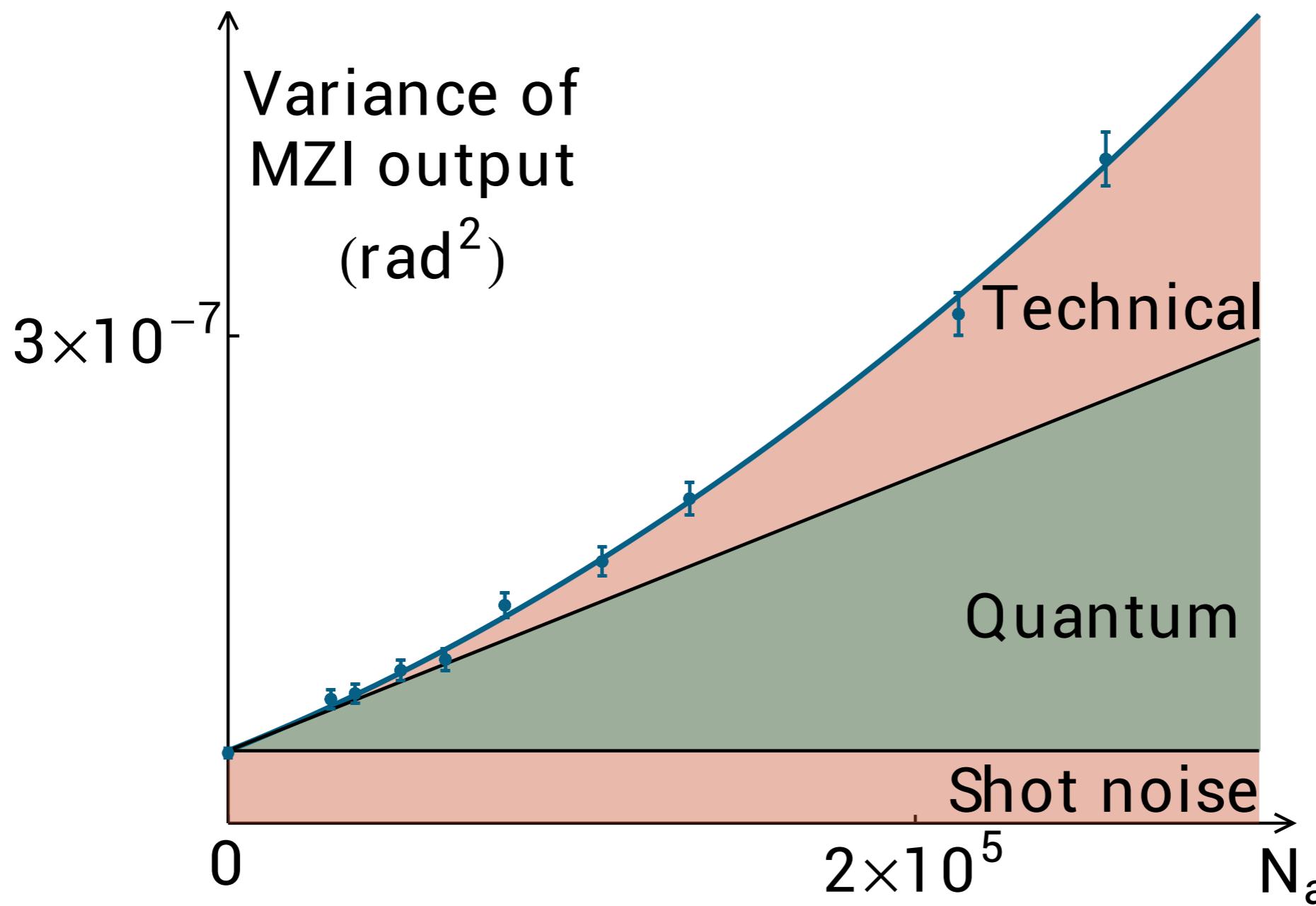
We implement cavities and a polarising beam splitter to filter unwanted decays.



Reusing each MOT four times allows to measure for different atom numbers.

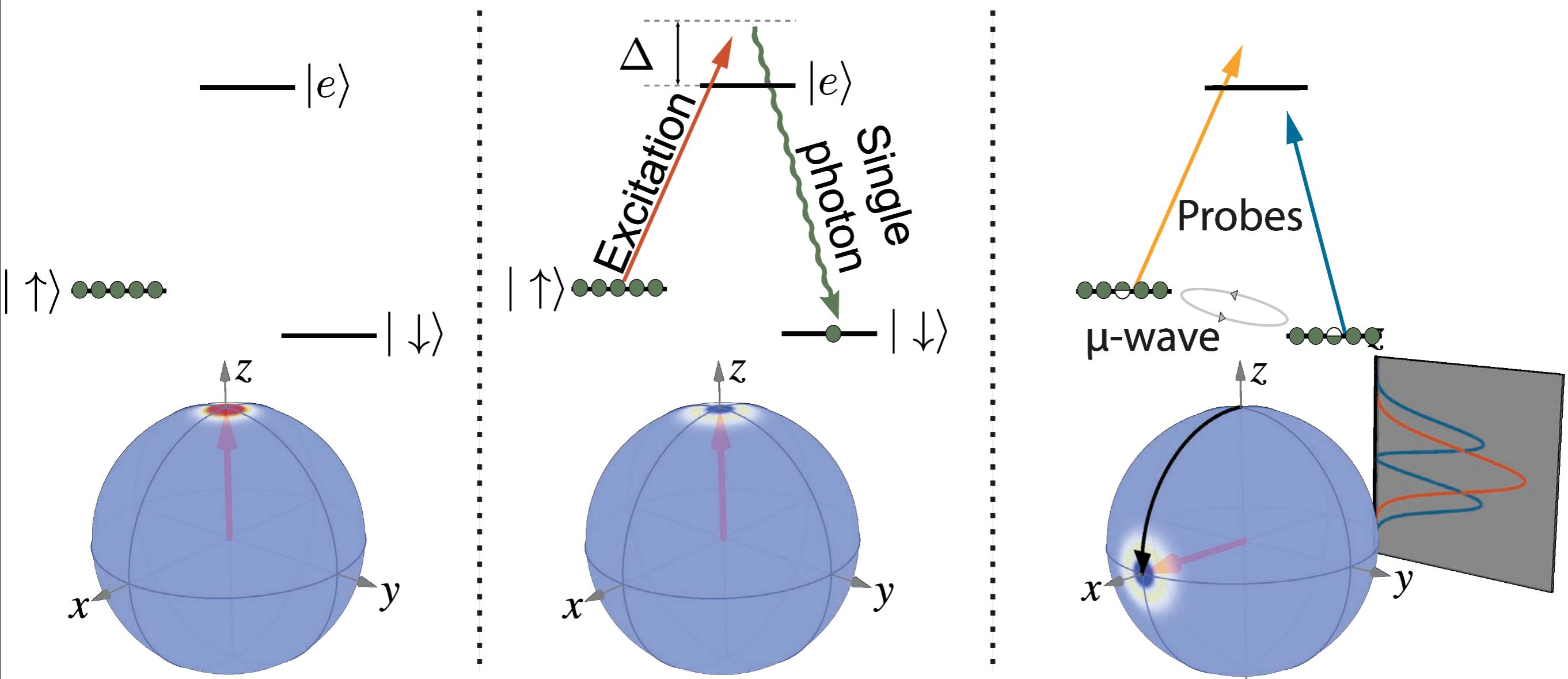


The atomic tomography method has a sensitivity beyond the projection noise.



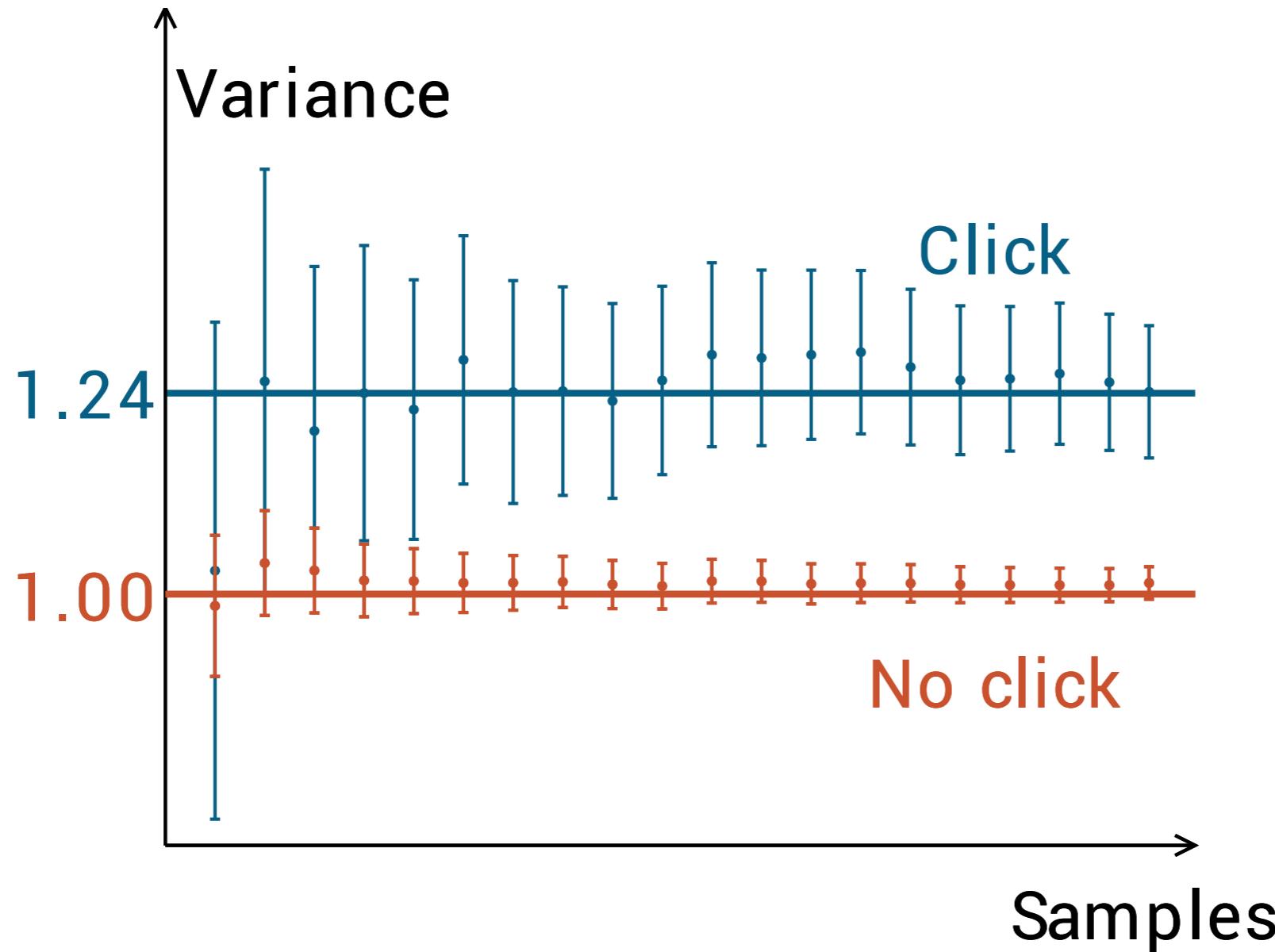
J. Appel et al, PNAS (2010)  
S. Christensen et al, arXiv (2013)

Resolving the quantum noise we now turn to distinguishing the states of interest.



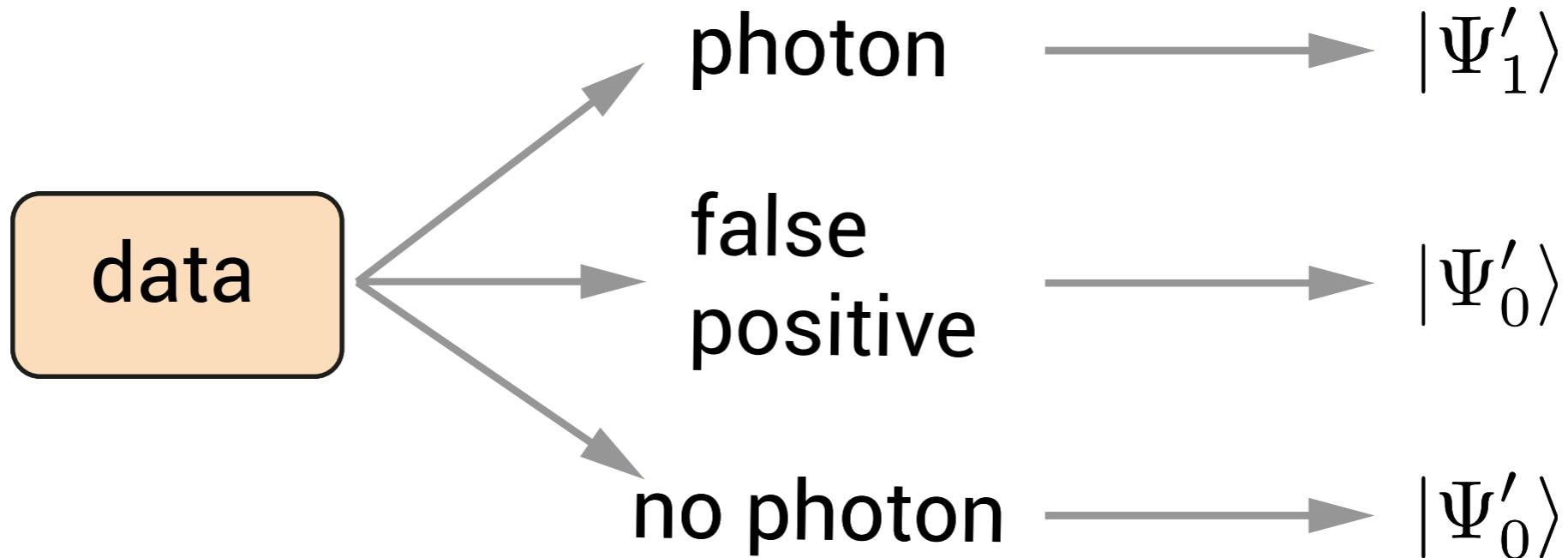
L. Duan et al, Nature (2001)  
S. Christensen et al, NJP (2013)

Conditioned on a click, a statistical significant variance increase is observed.



For pure state variance differ by a factor of three.

False positive events  
decrease the state purity.



False positives:

- Dark counts
- Bad decay
- Leakage photons

$$\hat{\rho} = p |\Psi'_1\rangle \langle \Psi'_1| + (1 - p) |\Psi'_0\rangle \langle \Psi'_0|$$

$$p = p_{\text{state}} = 0.38$$

Model and experiment  
are in agreement.

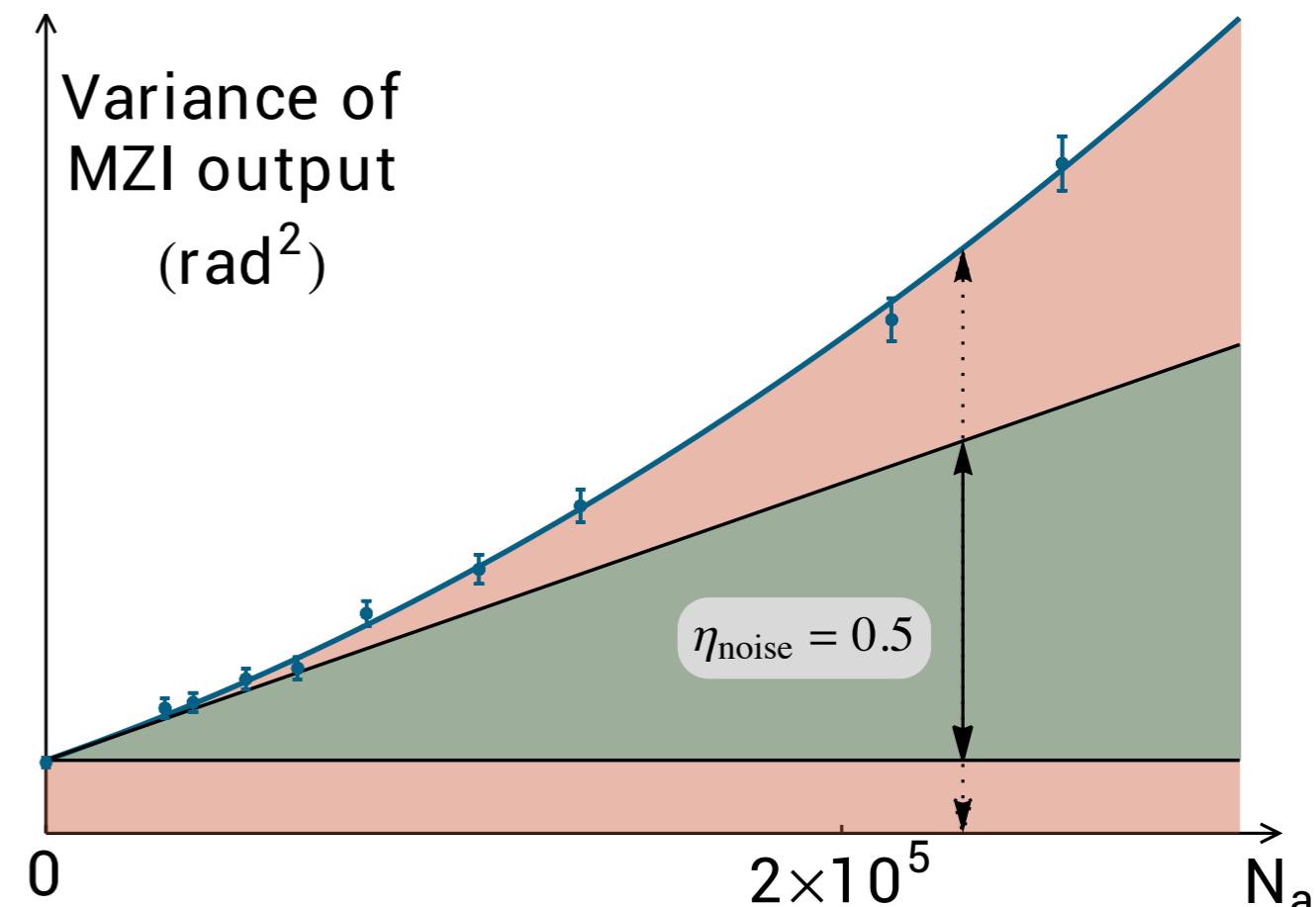
Detection efficiency:

$$\eta_Q = \eta_{\text{noise}} \eta_{\text{other}} = 0.27$$

Mix with vacuum:

$$p_{\text{model}} = p_{\text{state}} \eta_Q = 0.10$$

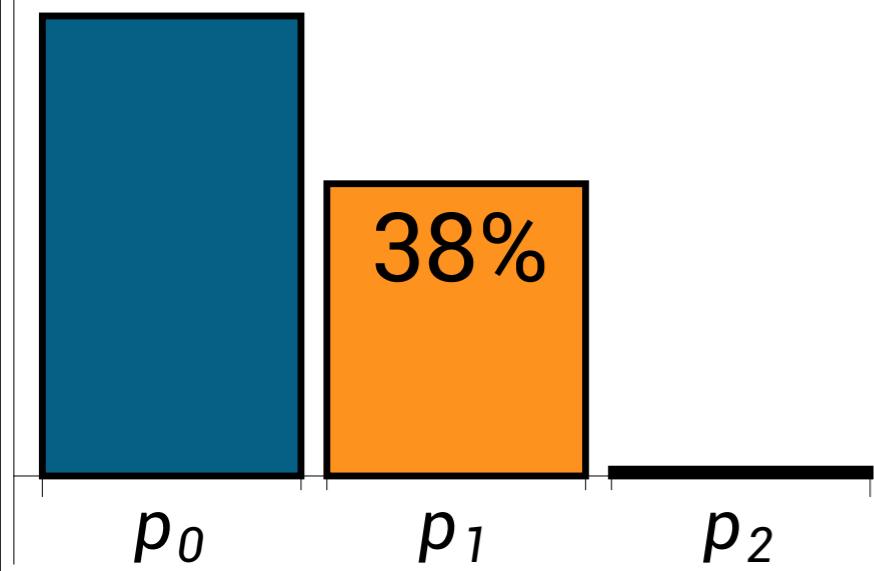
$$\hat{\rho} = p |\Psi'_1\rangle \langle \Psi'_1| + (1 - p) |\Psi'_0\rangle \langle \Psi'_0|$$



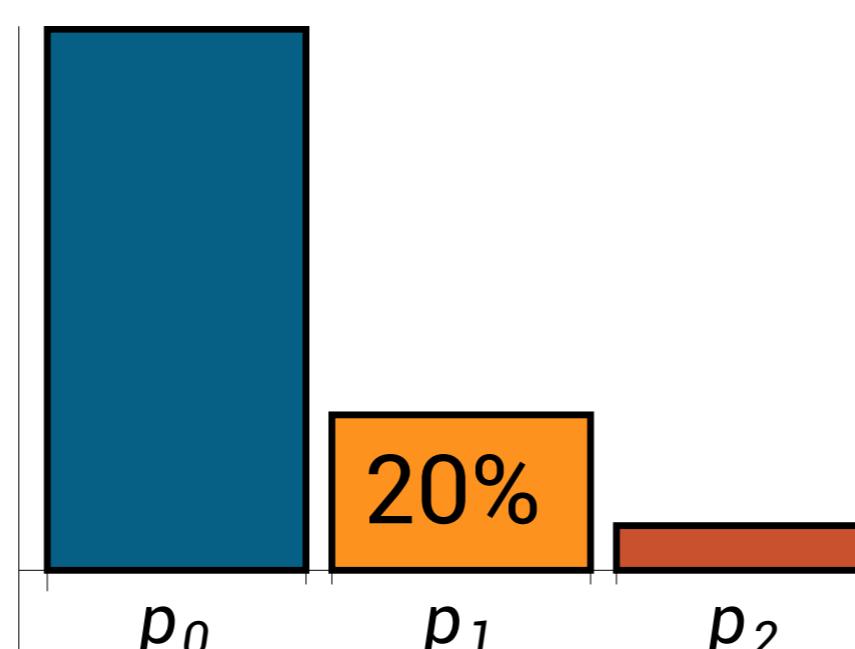
Model : 1.20  
Observed : 1.24 ± 0.08

The probability of having one excitation is incompatible with other states.

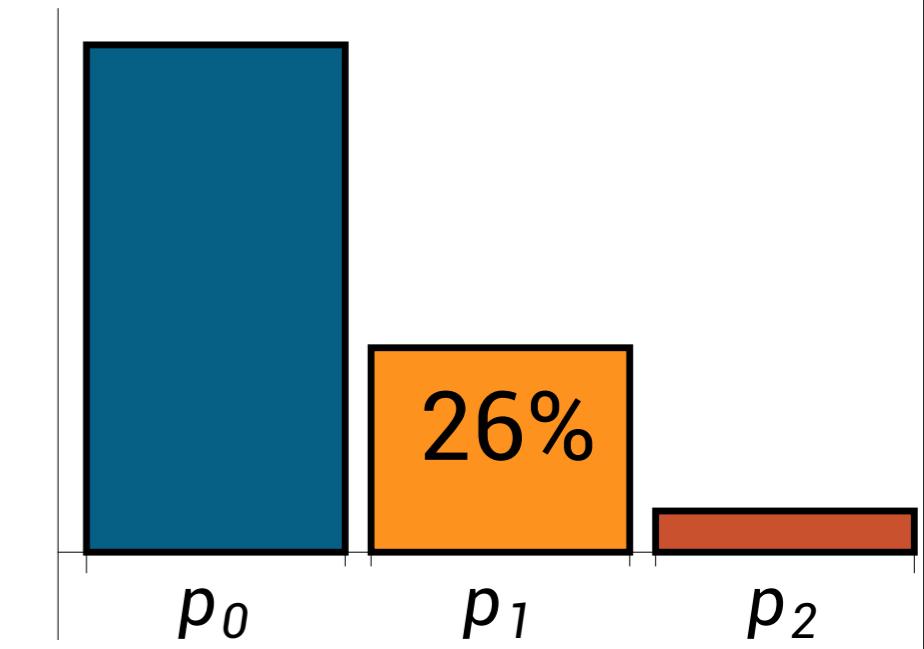
Created state



Thermal state



Coherent state



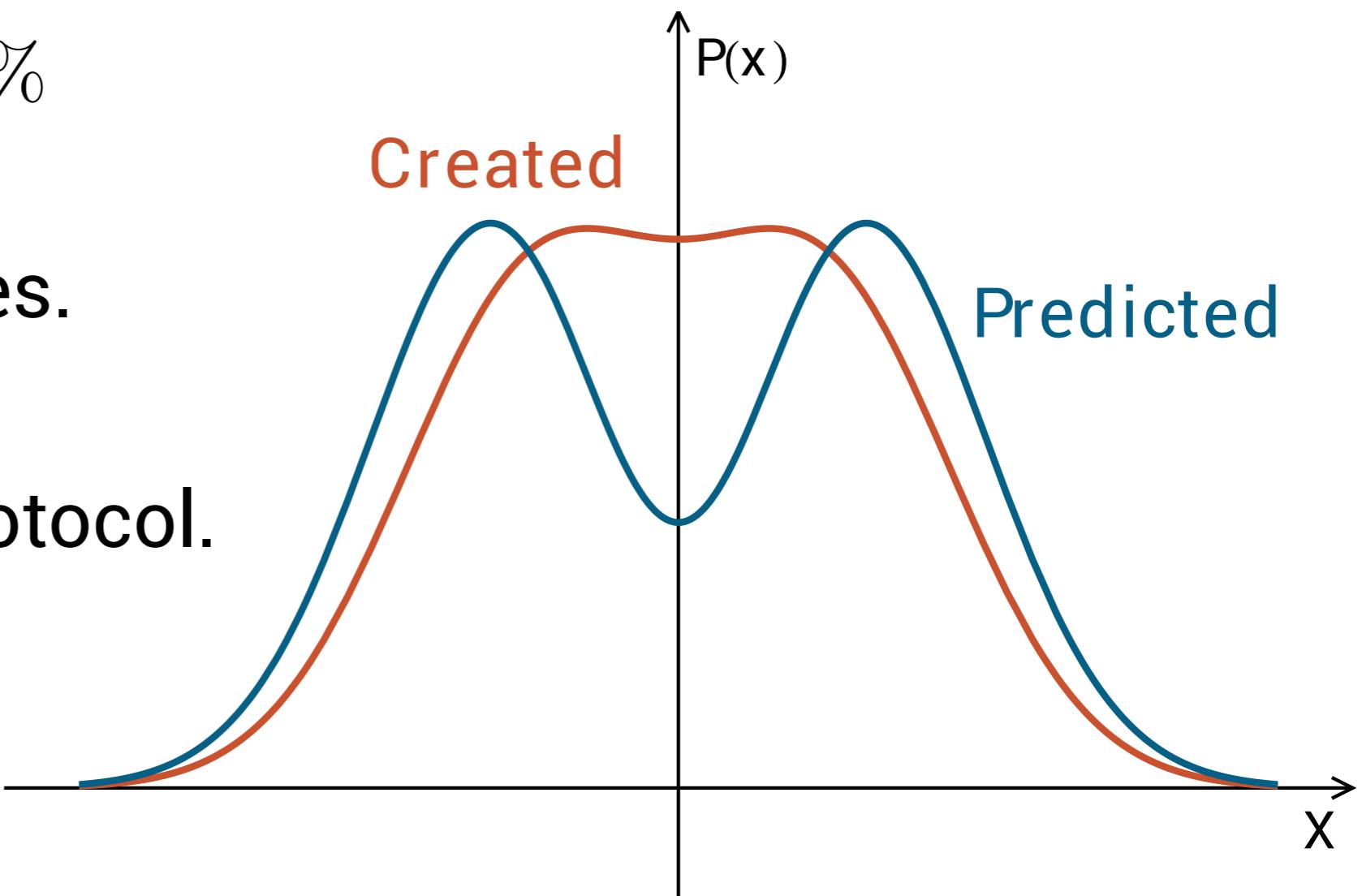
With technical improvements the creation of a non-classical states could be claimed.

- Improve filtering:

$$p_{\text{state}} = 38\% \rightarrow 70\%$$

- Schrödinger Cat states.

- Quantum repeater protocol.



# Quantum state engineering in an atomic ensemble.

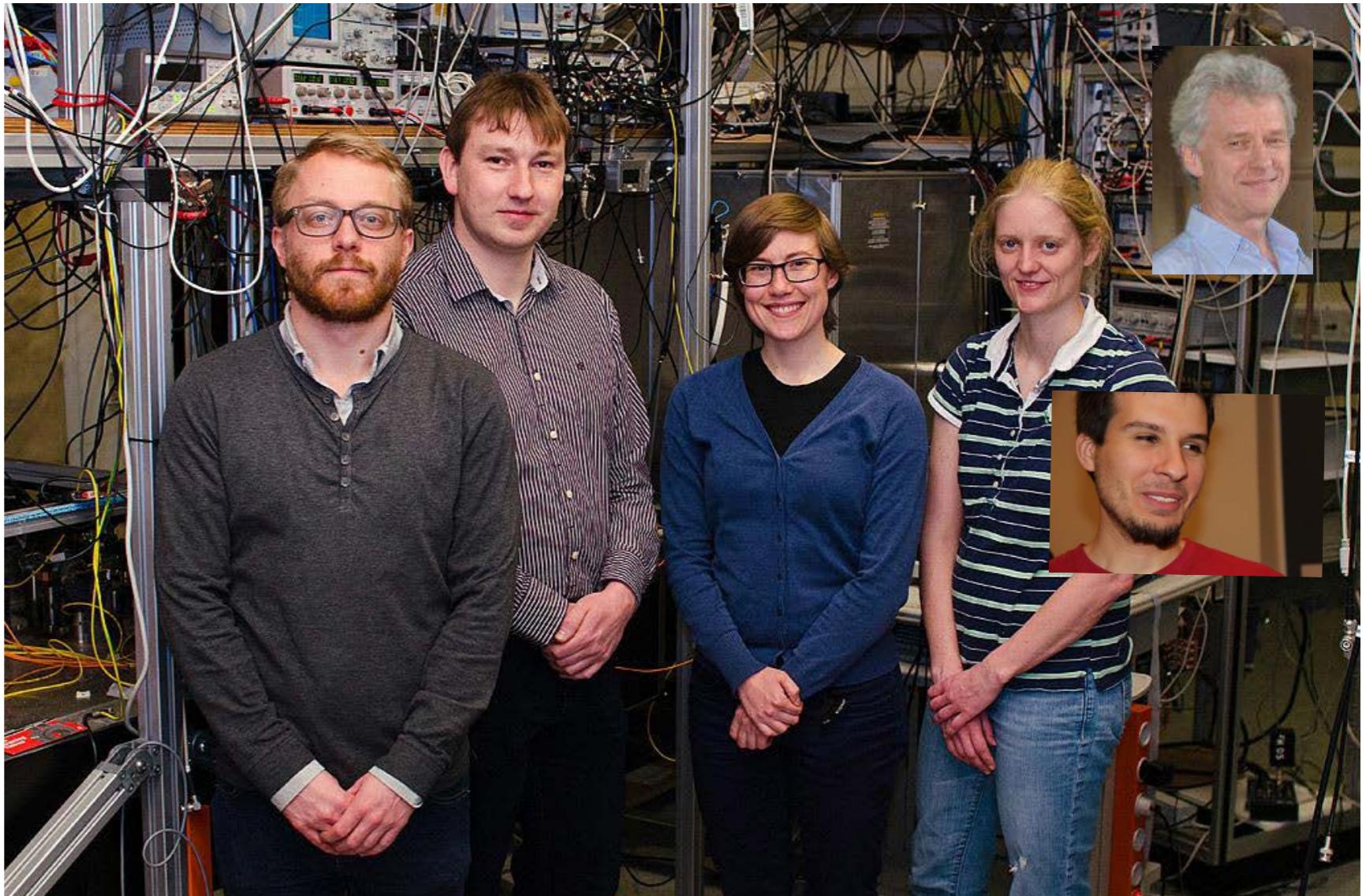


Hybrid discrete-continuous  
method.

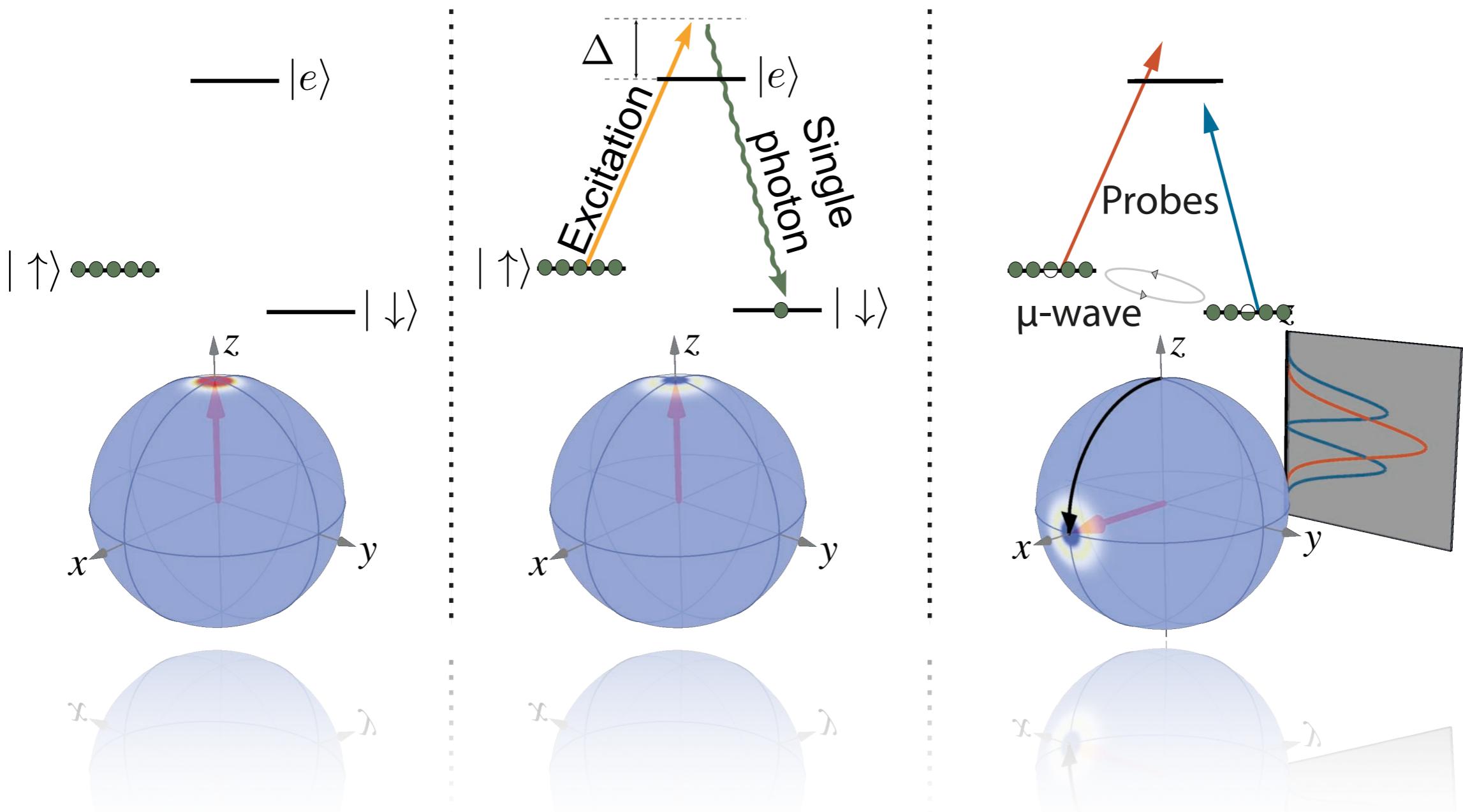
Atomic homodyne detection,  
for state characterisation.

A photon click leads to macroscopic  
alteration of a quantum state.

**J. B. Beguin**  
**H. L. Sørensen**  
**E. Bookjans**  
**J. H. Müller**  
**J. Appel**  
**E. Polzik**



*Niels Bohr Institute, University of Copenhagen*



# Thank you.

- S. Christensen et al., NJP 15 015002 (2013)
- S. Christensen et al. arxiv:1309.2514 (2013)
- R. McConnell et al., PRA 88 063802 (2013)

