

Cosmology and String Theory

The very large and the very small

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Overview

- Things in perspective

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- Things in perspective
- The expanding Universe

Cosmic Microwave Background Radiation (CMBR)

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- Friedman-Robertson-Walker model

Standard Model of Cosmology

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Standard Model of Cosmology
- Problems with the Standard Model of Cosmology
- Inflationary paradigm
- Uses of string theory

From Planck to PLANCK



Planck

We have been talking about the smallest of distance scales:

From Planck to PLANCK

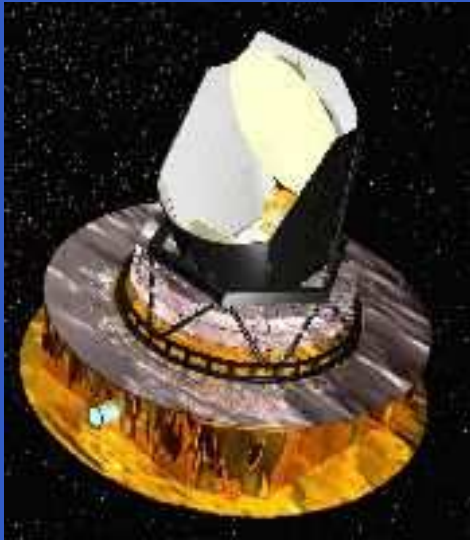


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$$\ell_{\text{Pl}} = \frac{G_N \hbar}{c^3} \sim 10^{-33} \text{ cm}$$

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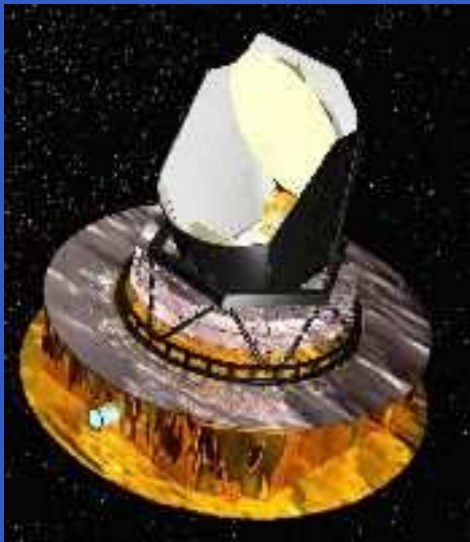
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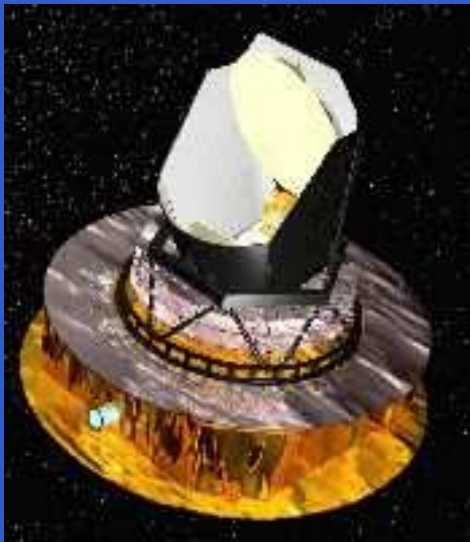
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$$\text{Size of the Universe} \sim 5 \times 10^{30} \text{ cm}$$

Our neighbourhood

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$$1 \text{ pc} = 3.26 \text{ ly} = 3.09 \times 10^{18} \text{ cm}$$

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The next galaxy is $50\text{kpc} \simeq 1.7 \times 10^5$ **ly** away.

Cosmic hierarchy

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Quasars are the farthest structures seen in the Universe $\sim$ **12–14 Gpc** away.

Distribution of galaxies

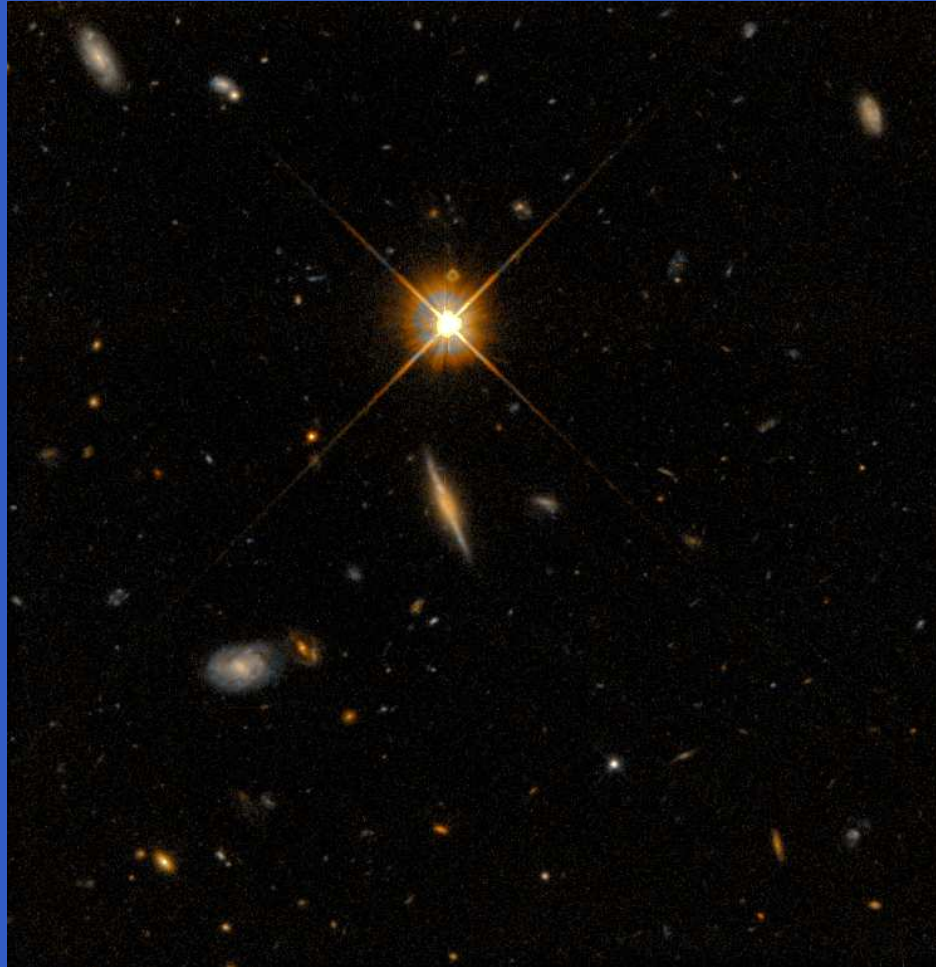
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Density of matter $\rho_{\text{matter}} \sim 10^{-31} \text{ gm/cm}^3$

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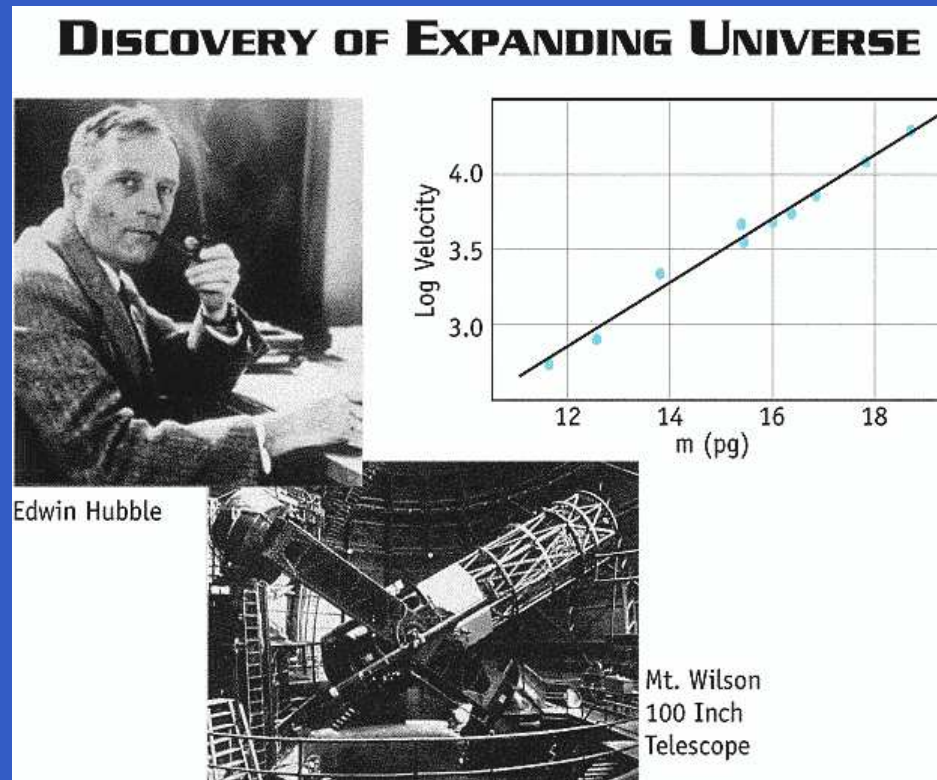
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Ours is an **expanding Universe**. Galaxies are moving away from each other.

Hubble's observation



• • • Hubble's observation

Hubble's law:

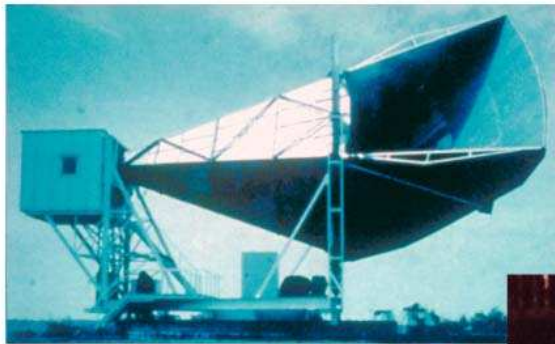
The velocity of recession v of a galaxy at a distance d is a linearly increasing function of d .

$$v = H_0 d$$

$H_0 = 72 \pm 7$ (km/s)/Mpc is the Hubble's constant.

Cosmic microwave radiation

DISCOVERY OF COSMIC BACKGROUND

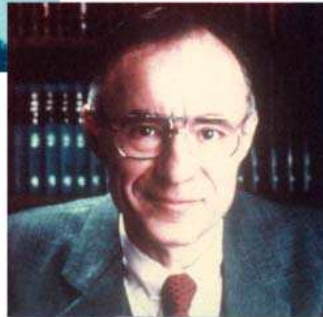


Microwave Receiver



MAP990045

Robert Wilson



Arno Penzias

Cosmic microwave radiation

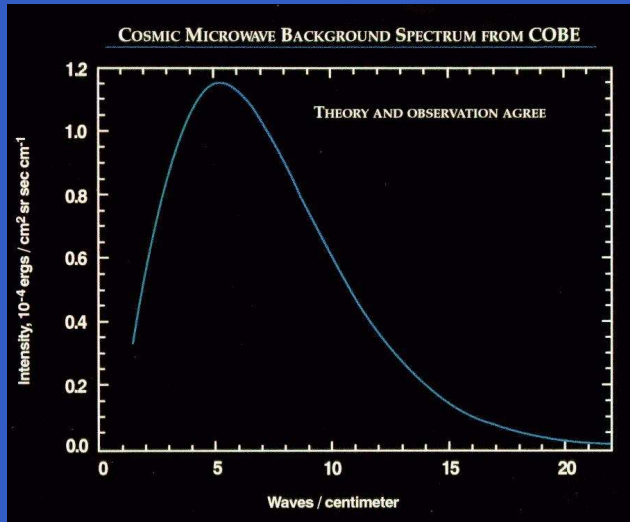
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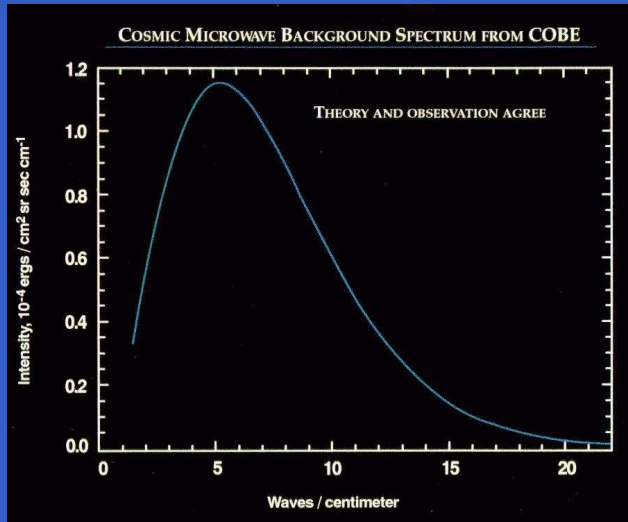


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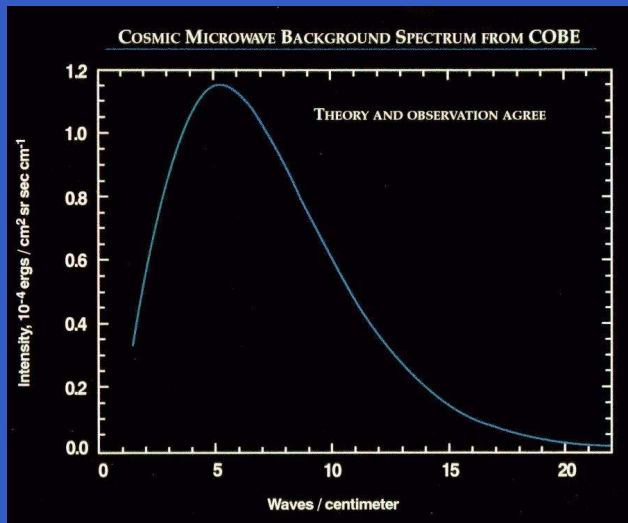
[animated] TV noise

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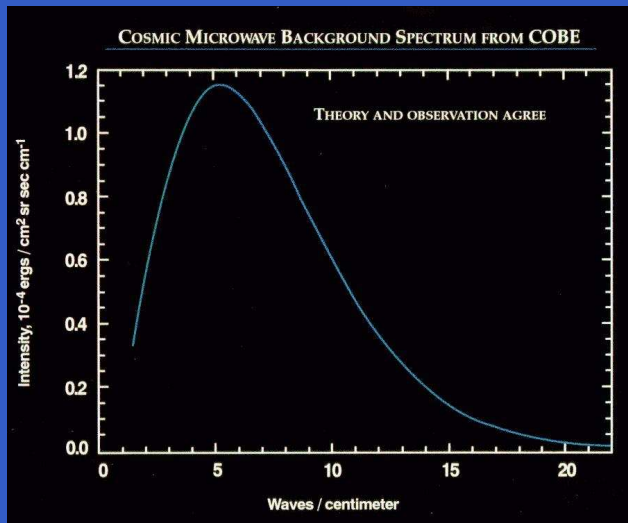
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A candidate is **vacuum energy**.

FRW cosmological model

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physical distance = $a(t)$ coordinate distance

(x, y, z) are called **comoving coordinates**.

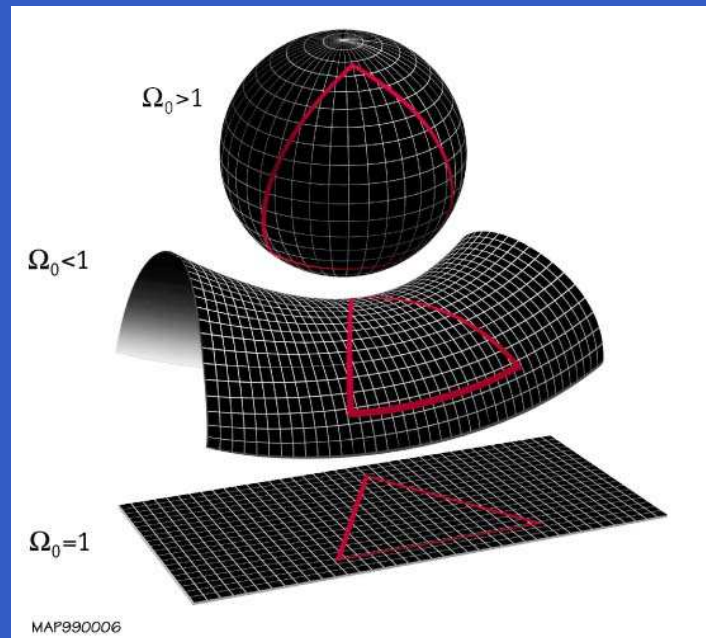
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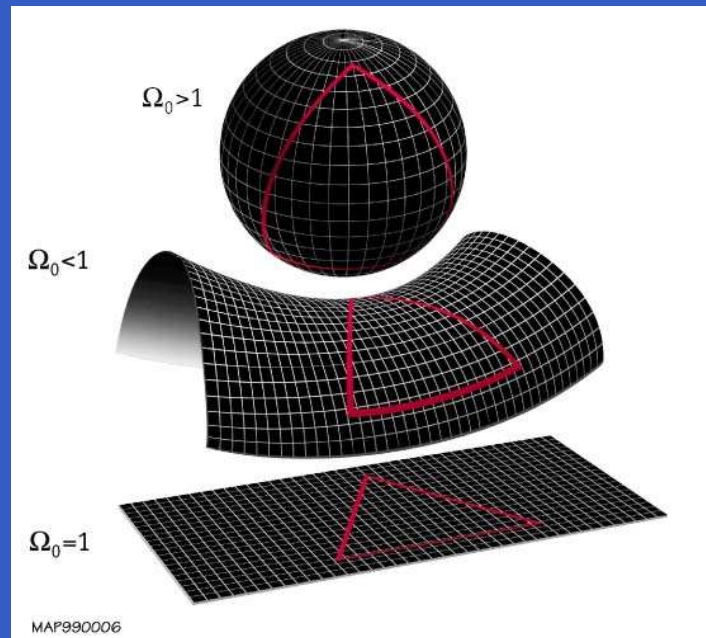
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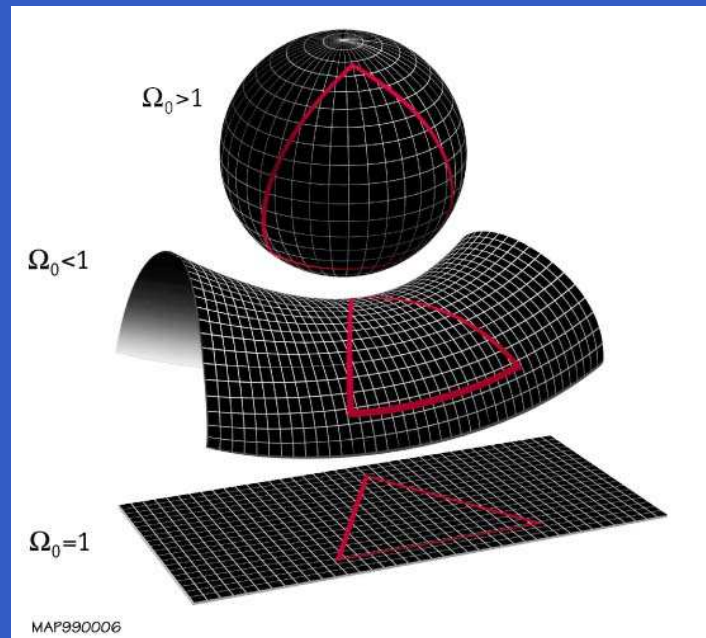


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Is the expansion **uni-**
form, **accelerated** or
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$z = \Delta\lambda/\lambda$ is also a measure of distance. Quasars have $z \sim 6.6$.

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$\rho_m(\text{now}) \sim 10^{-30} \text{g/cm}^3$ Visible matter is $\sim 10\%$ of this.

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Radiation density is falling off faster than matter density.

$\rho_r(\text{now}) \sim 10^{-34} \text{g/cm}^3 < \rho_m(\text{now})$. Matter dominates over radiation at present.

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Thermal history of the Universe

The Universe cooled as it expanded and the density of matter and radiation decreased.

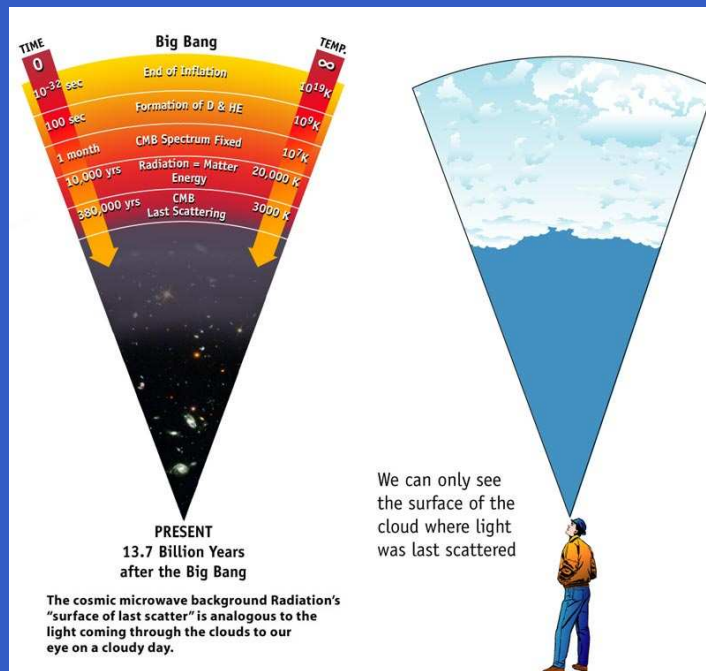
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$t = 3 \times 10^5 \text{ yrs}$, $T = 3000^\circ \text{K}$: Mat-

ter radiation decoupling.

Last scattering surface — CMBR originates.

Protons and electrons combine to form Hydrogen and Helium atoms shortly afterwards.

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$t = 10^2 \text{s}$, $T = 10^9 \text{K}$: Matter to radiation domination.
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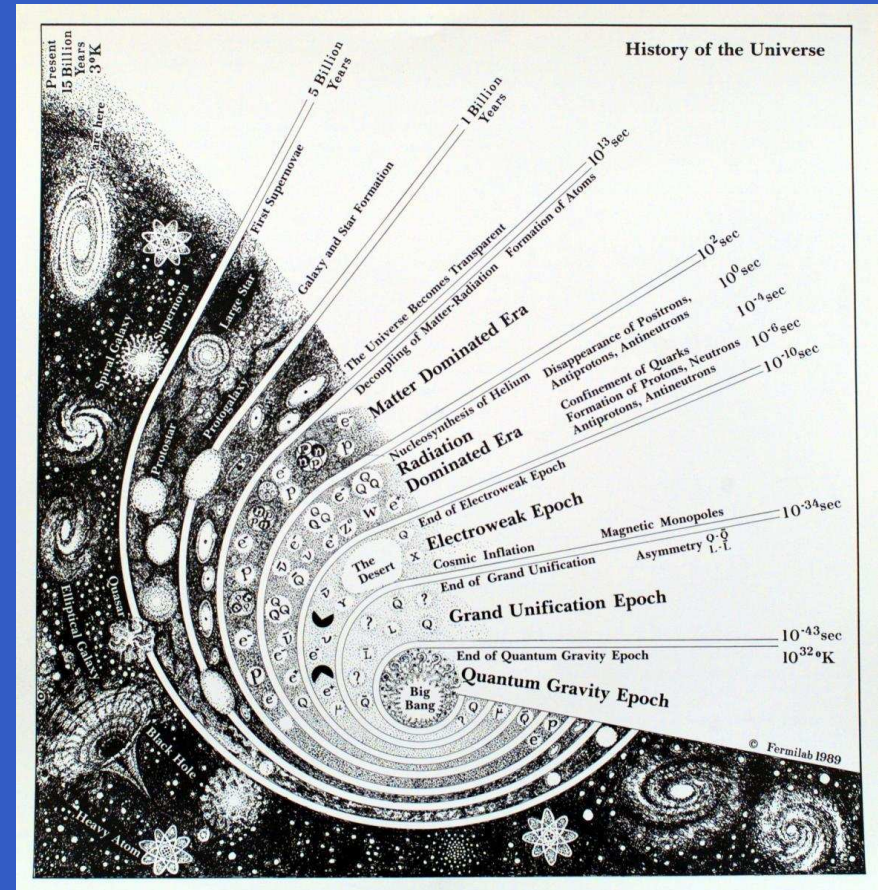
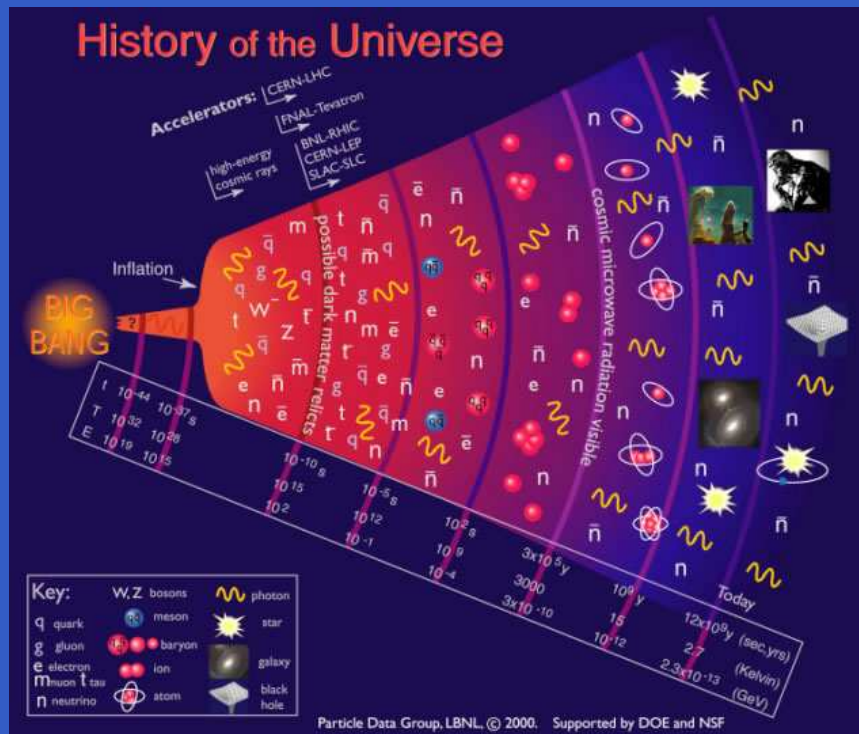
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$t = 10^{-43} \text{s}, T = 10^{31\circ} \text{K}$: Quantum gravity era

Thermal history... (iii)



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Einstein equations

Just one equation: $\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G_N}{3} \rho_{\text{tot}}$ Friedman
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Just one equation: $\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G_N}{3} \rho_{\text{tot}}$ **Friedman equation.** For spatially curved Universe:

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G_N}{3} \rho_{\text{tot}} - \frac{k}{a^2}$$

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$$\rho_{cr} = \frac{3H_0^2}{8\pi G_N} = 10^{-29} \text{g/cm}^3$$

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the **critical density**. Dimensionless densities:

$$\Omega_m = \rho_{m,0}/\rho_{cr}, \quad \Omega_r = \rho_{r,0}/\rho_{cr}, \quad \Omega_\Lambda = \rho_{v,0}/\rho_{cr}$$

$$(\Omega_m + \Omega_r + \Omega_\Lambda = 1).$$

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Energy condition for a (NR) particle in a potential.

Evolution of scale factor

Scale factor $a(t)$ grows as

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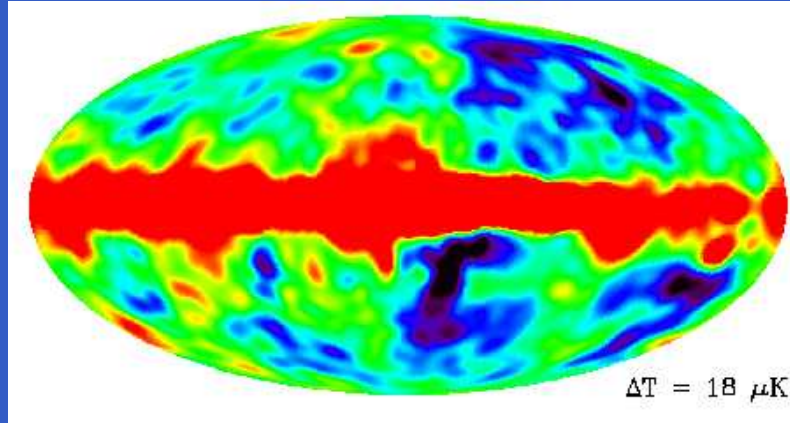
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Big Bang Singularity

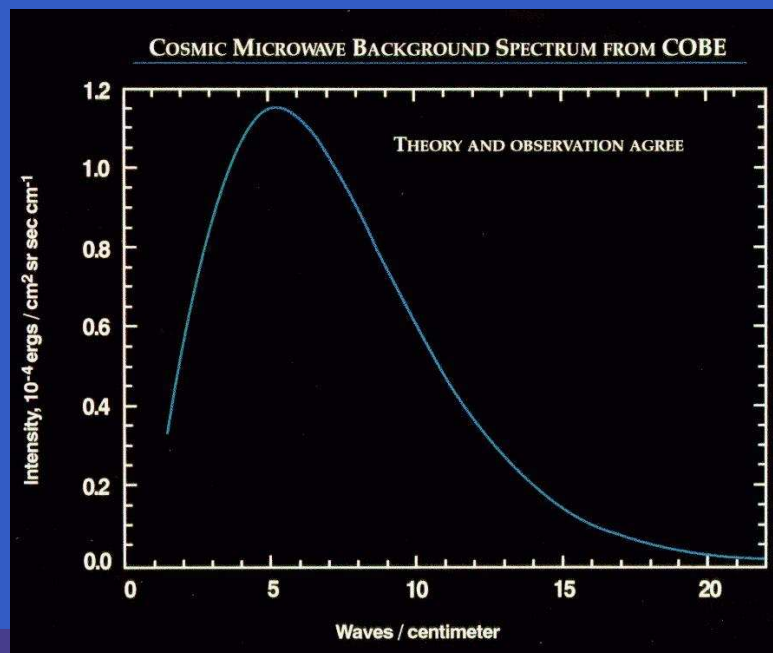
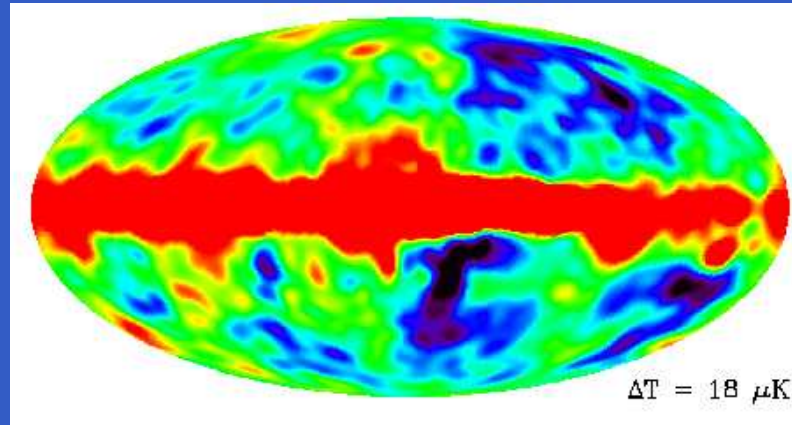
CMBR and COBE



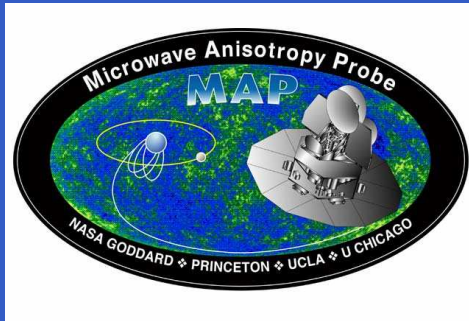
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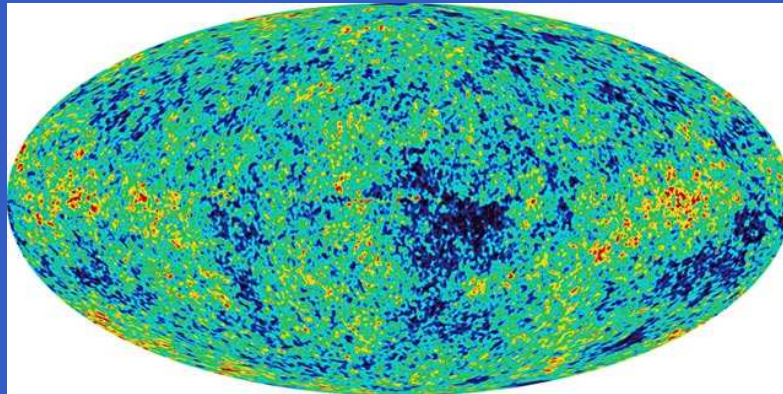
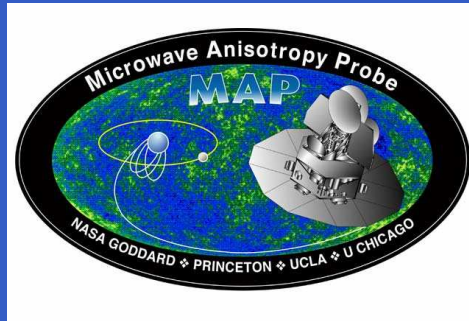
CMBR and COBE



WMAPping CMBR

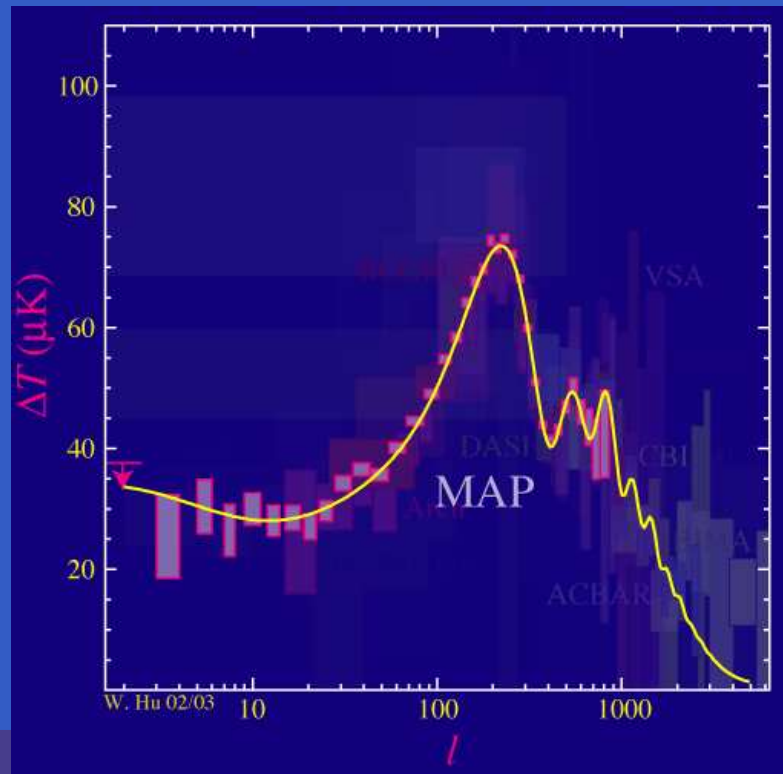
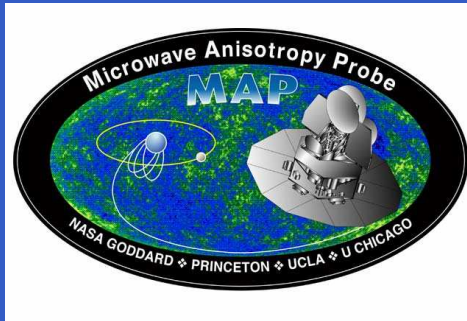


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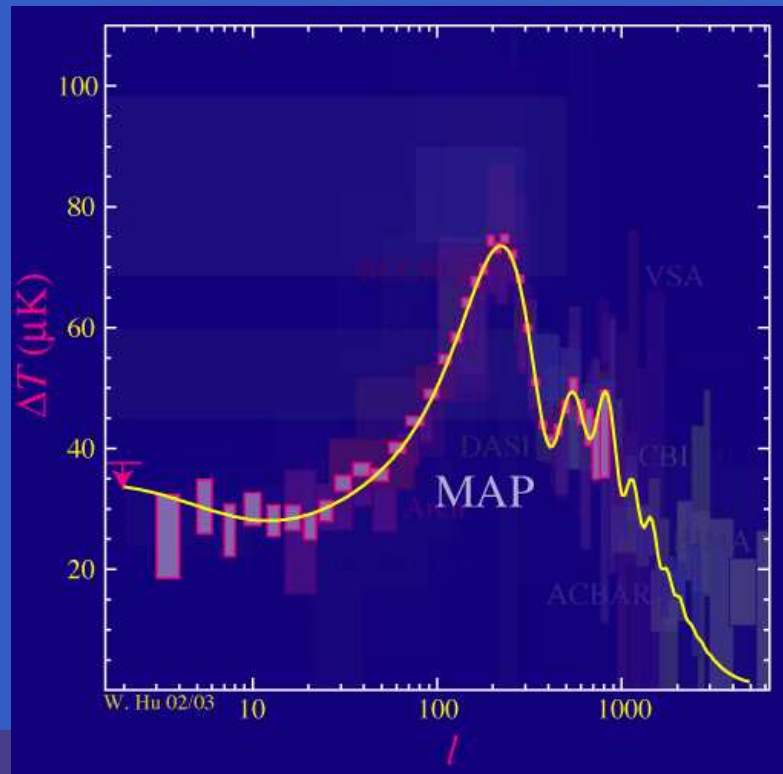
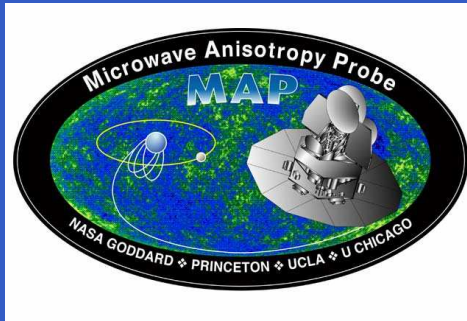


Fluctuations: 1 part in 10^5

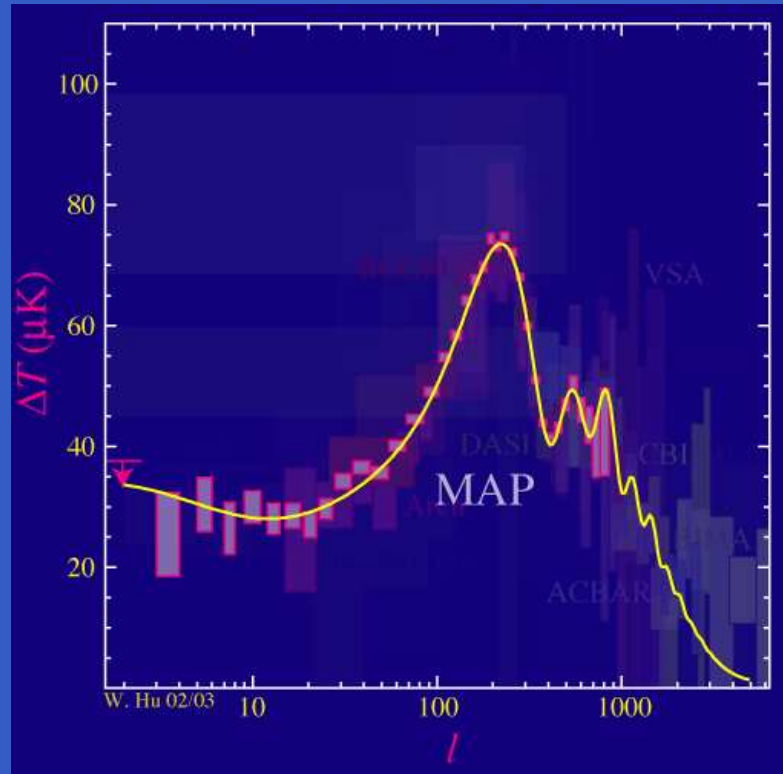
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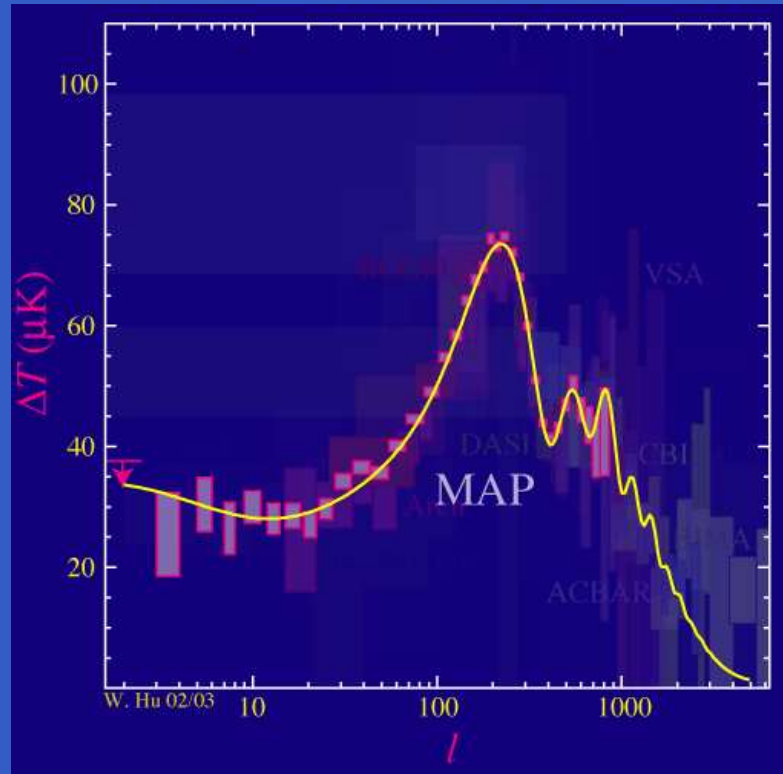


WMAPping CMBR... (ii)



Angular correlation of temperature fluctuations in μK .

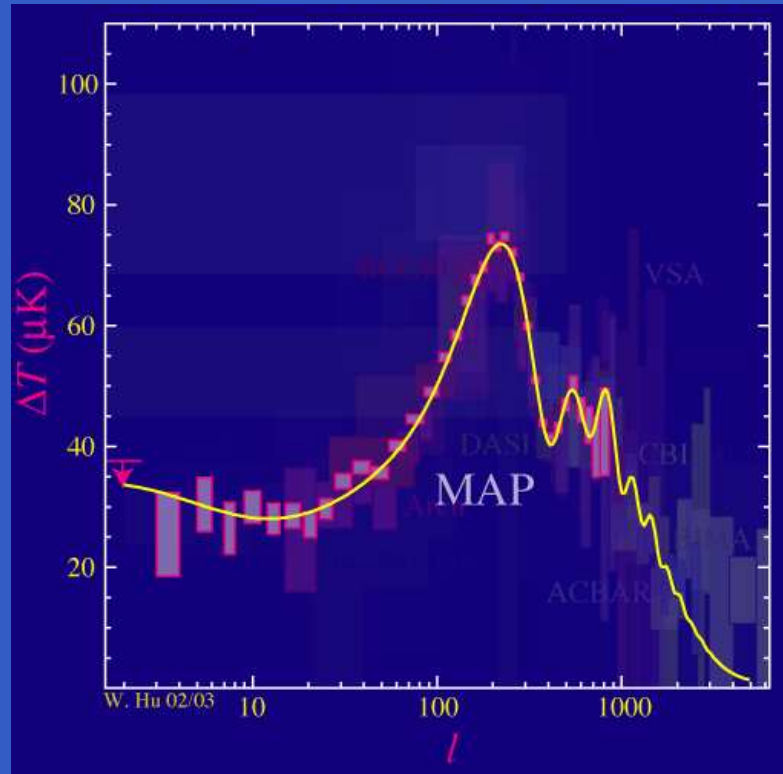
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Music from the primordial universe

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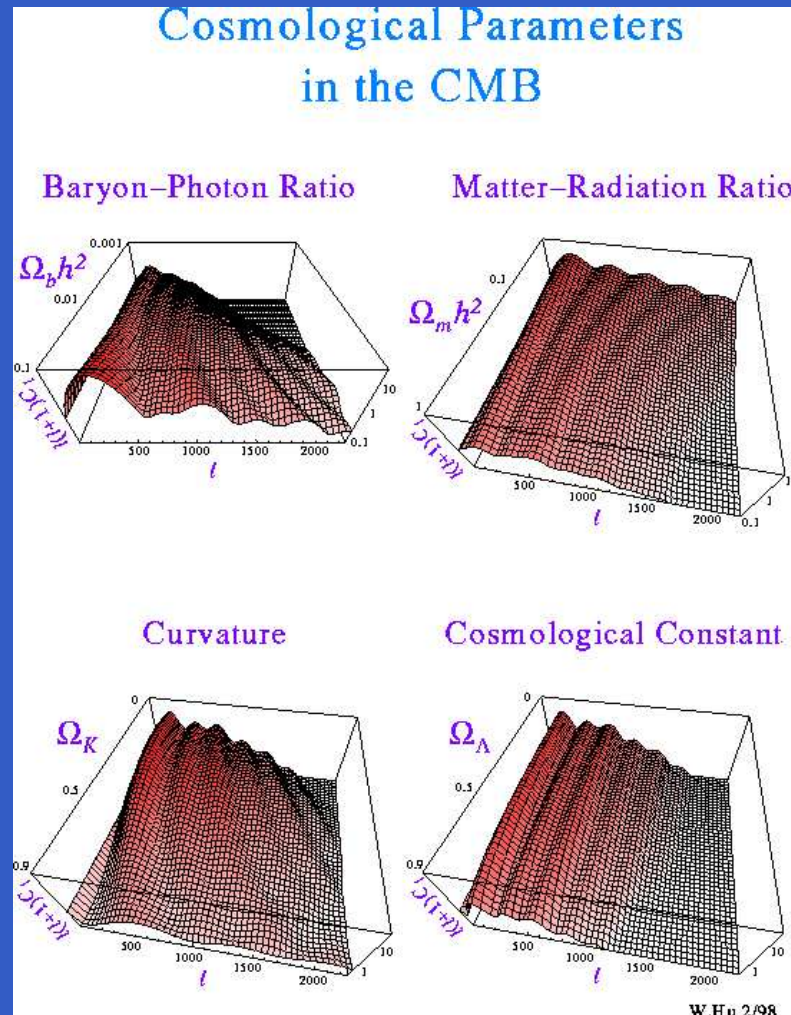
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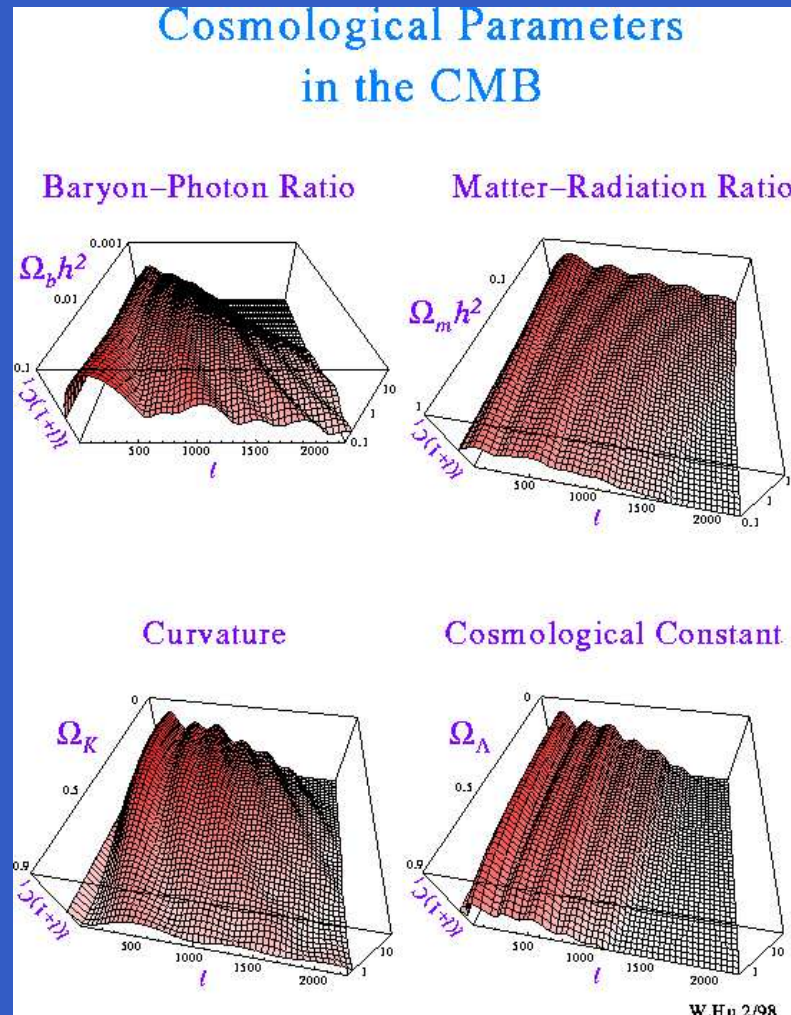
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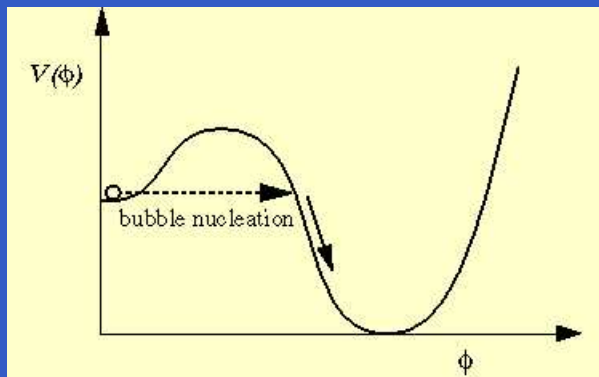
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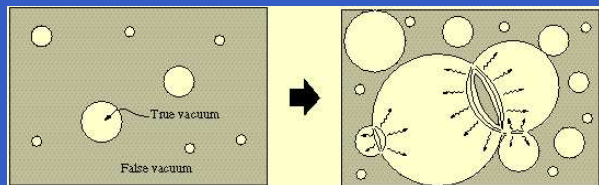
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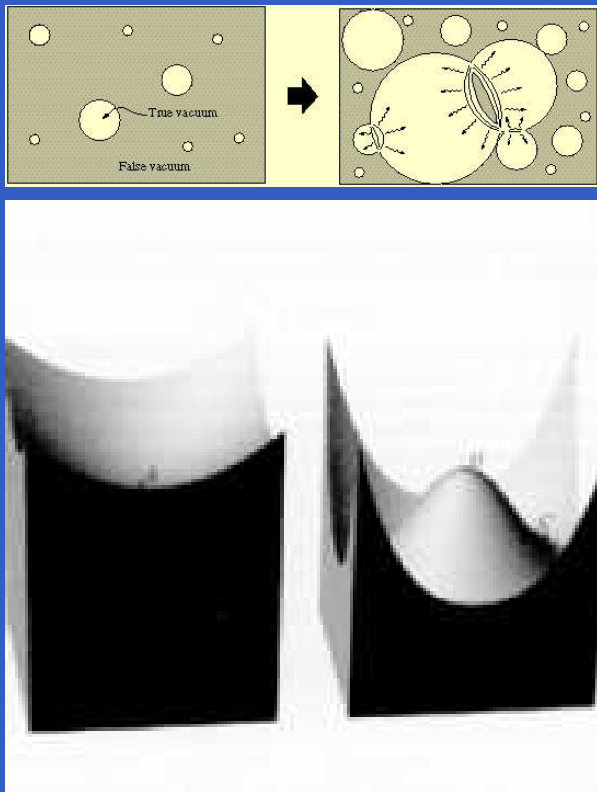


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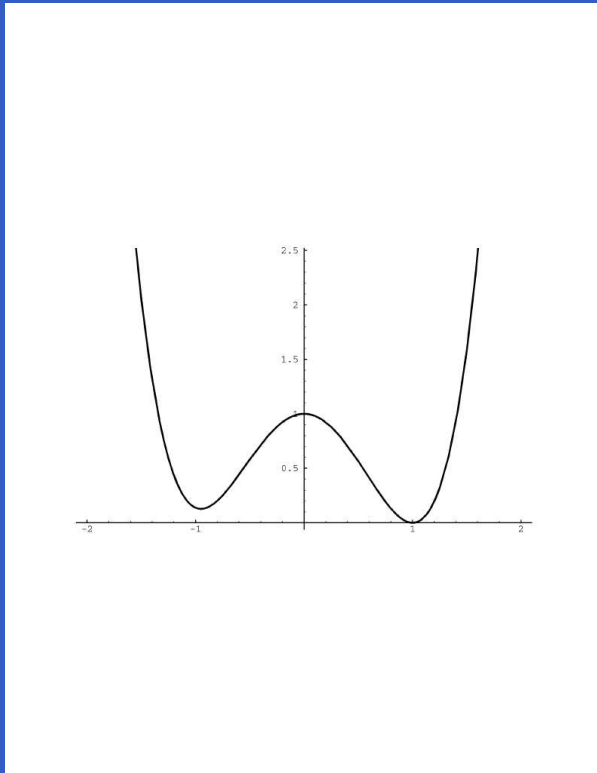
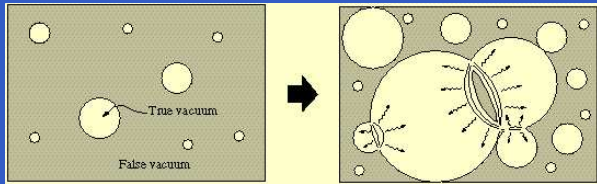
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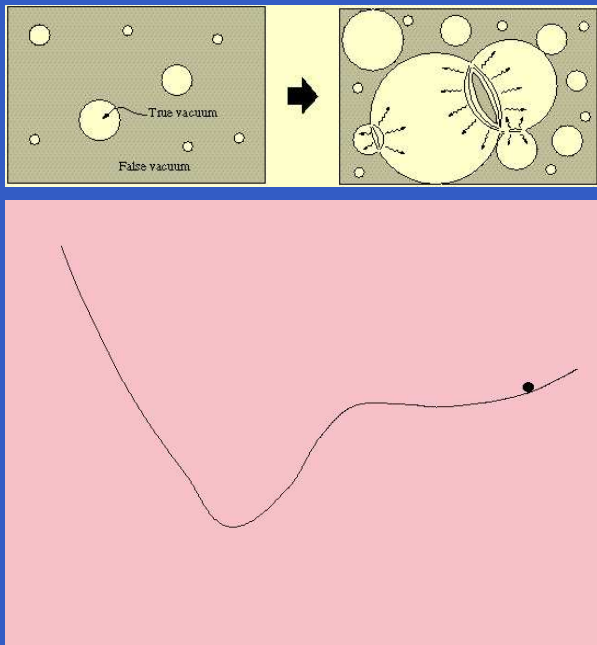


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Inflation... (ii)

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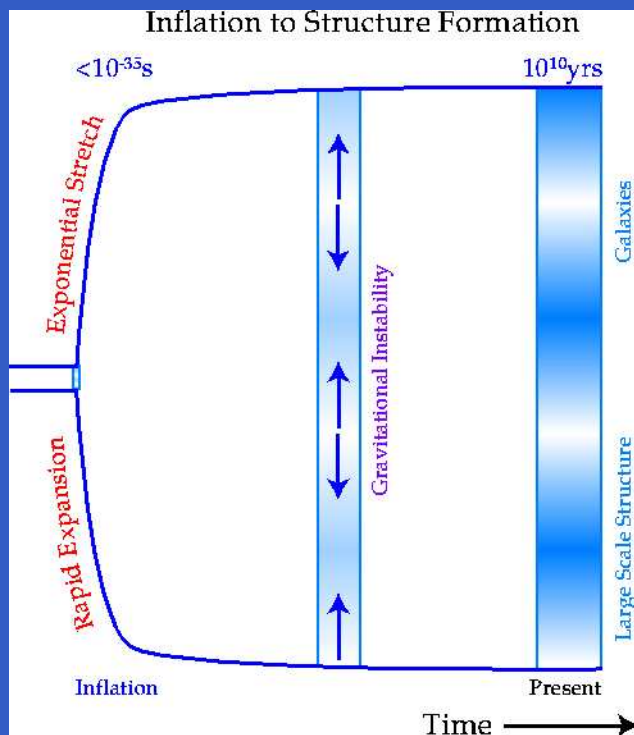
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In addition, most models predicts a *scale invariant spectrum* of **quantum fluctuations** which explain *structure formation*.

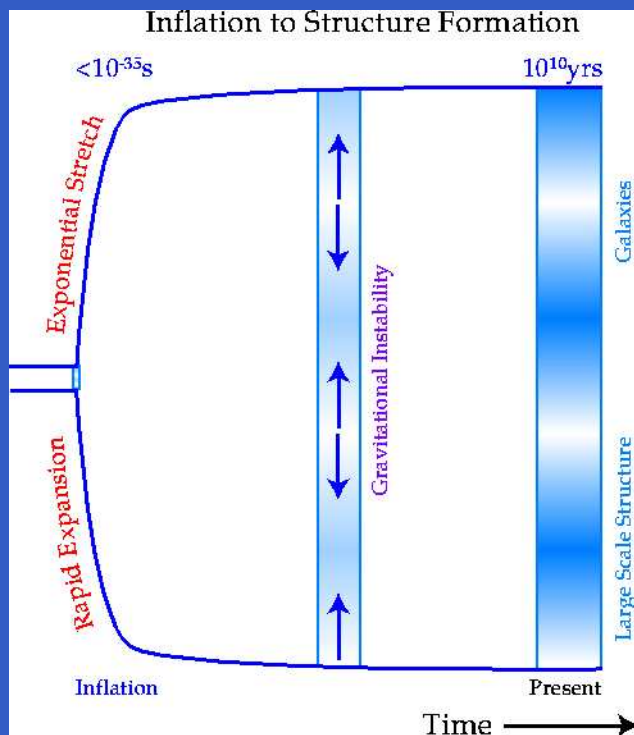
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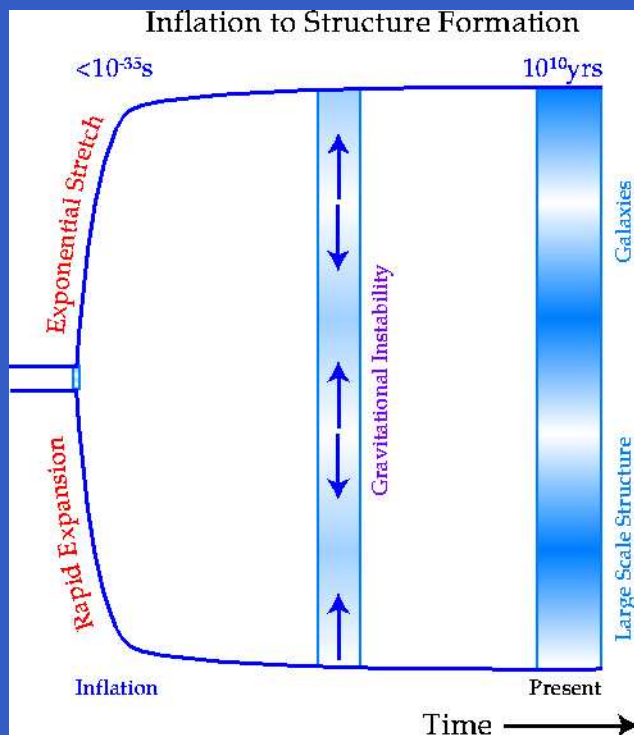
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Which model?

Is semiclassical treatment enough?

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Hybrid inflation

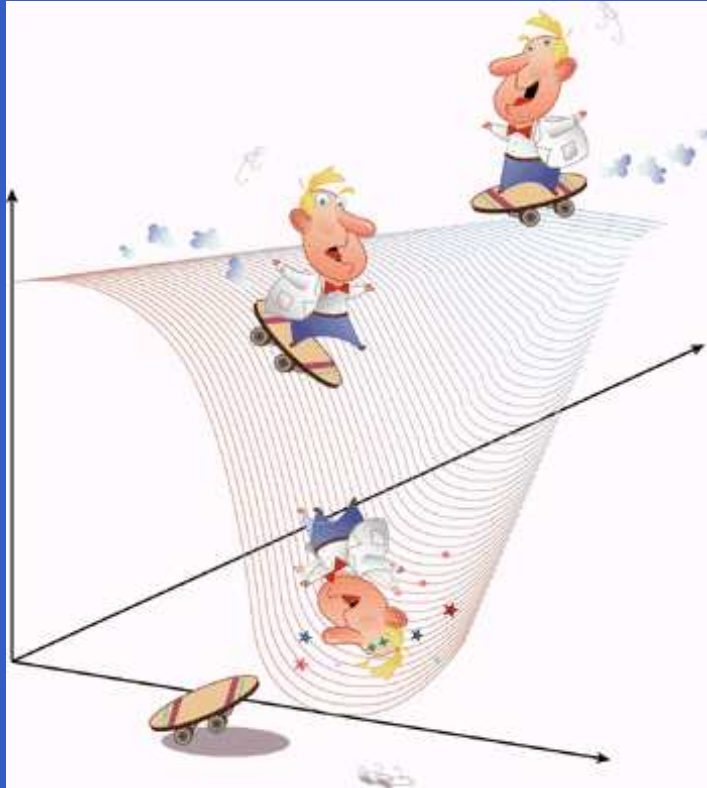
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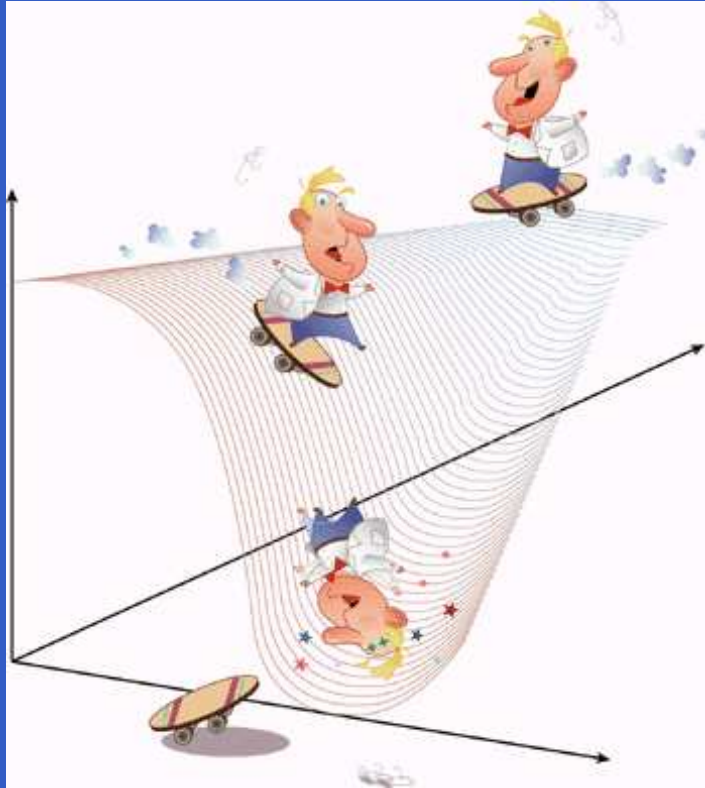
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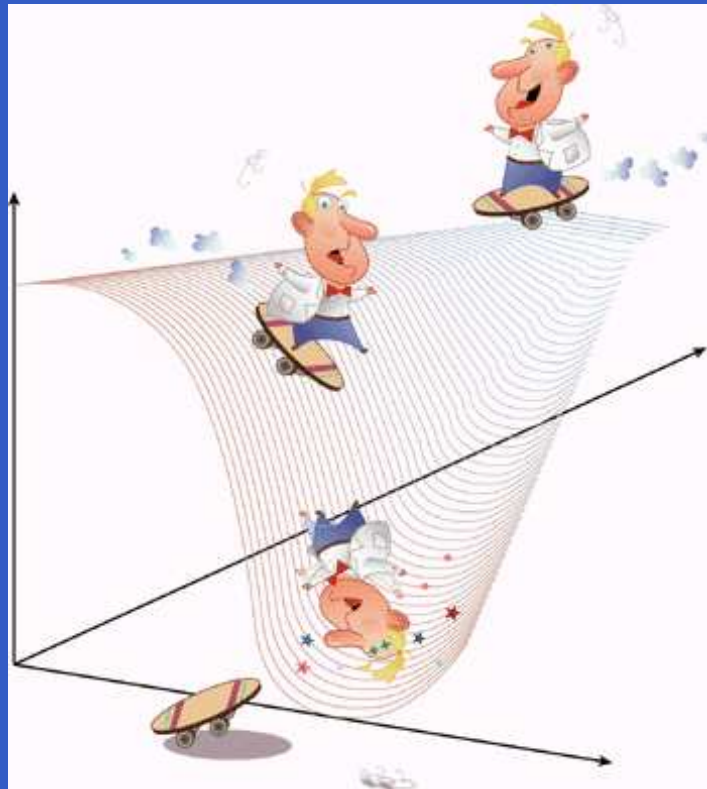


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Many other models...

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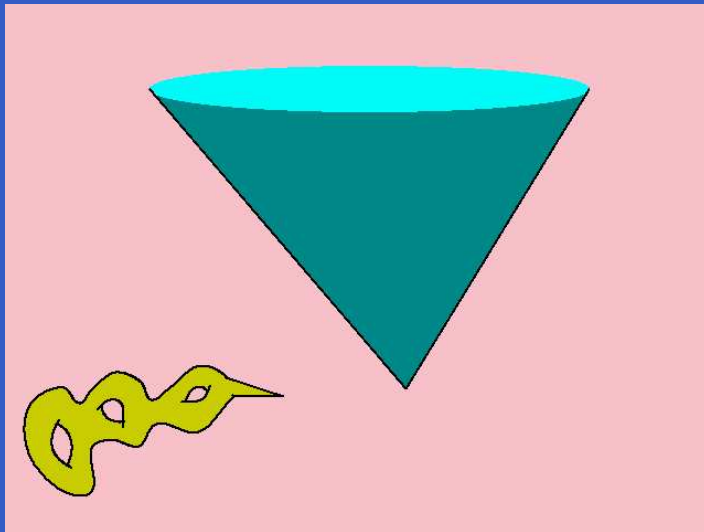
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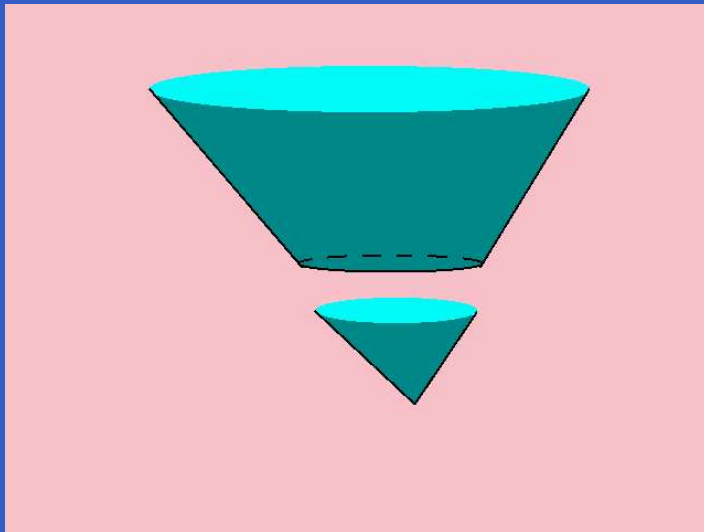
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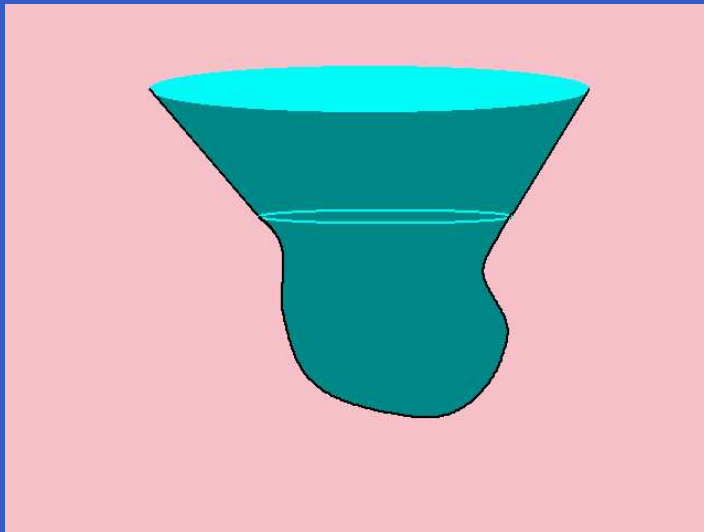
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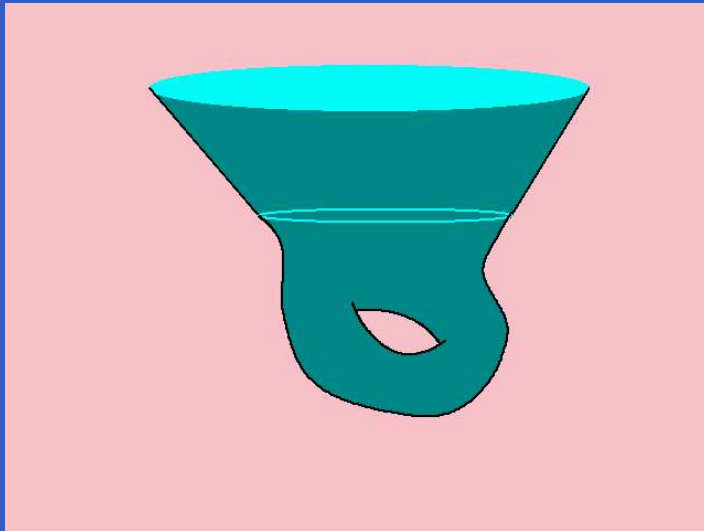
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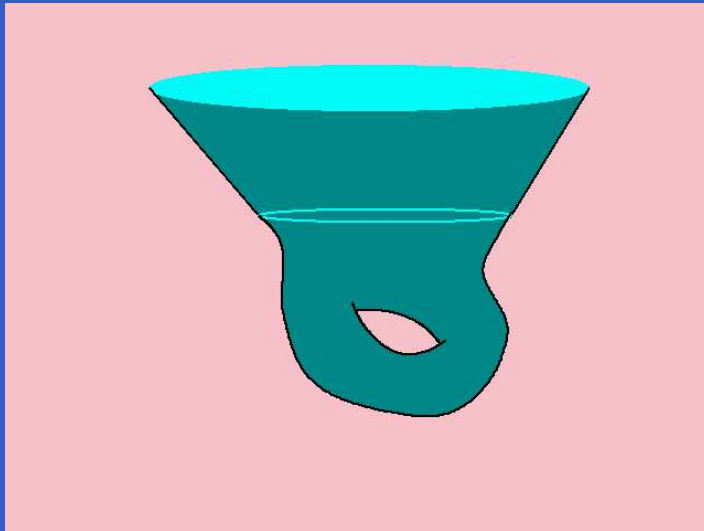
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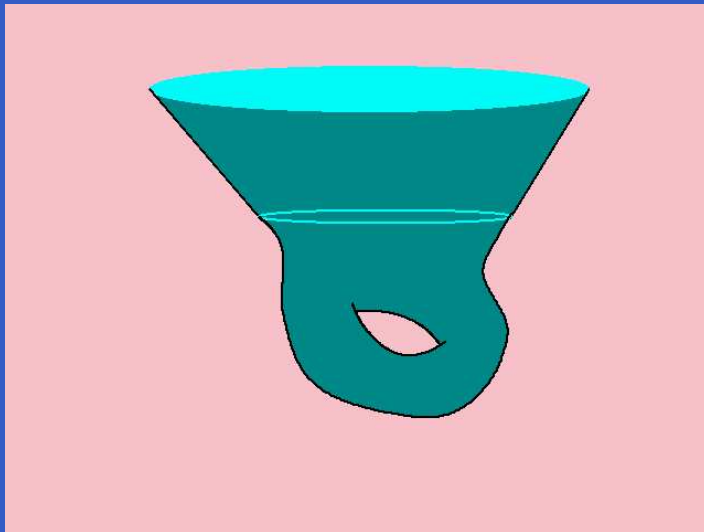


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Can string theory resolve the space-time singularity in **Big Bang**?

Can it explain **four** dimensions?

Whether string, whither string

If string theory describes nature, the confirmation may well come from the sky.

Acknowledgement

Wayne Hu's cosmology page:
background.uchicago.edu/~whu/

[NASA homepage](#)

[Cambridge Relativity Group:](#)

www.damtp.cam.ac.uk/user/gr/public/index.html

and many others via [google](#).