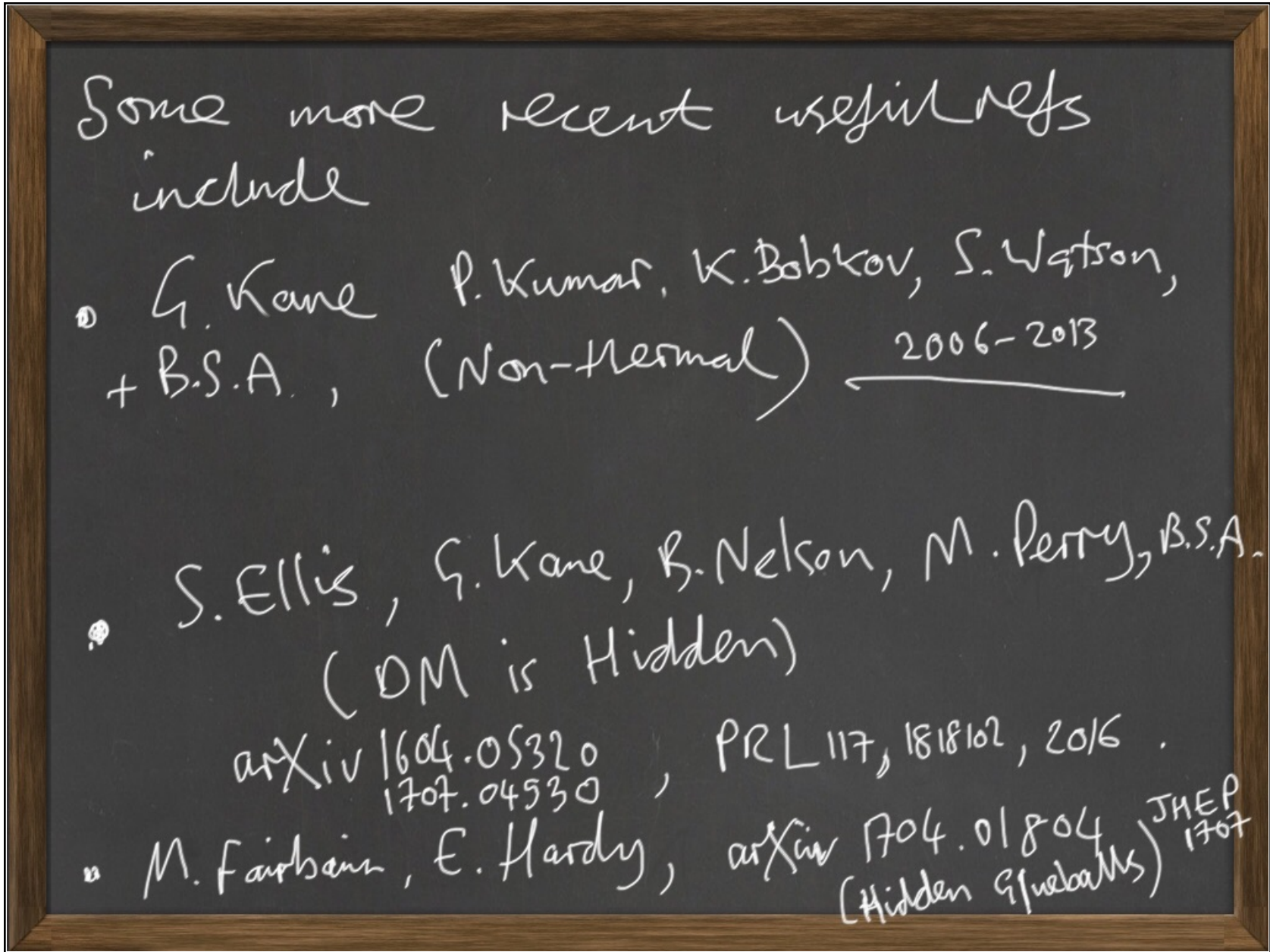
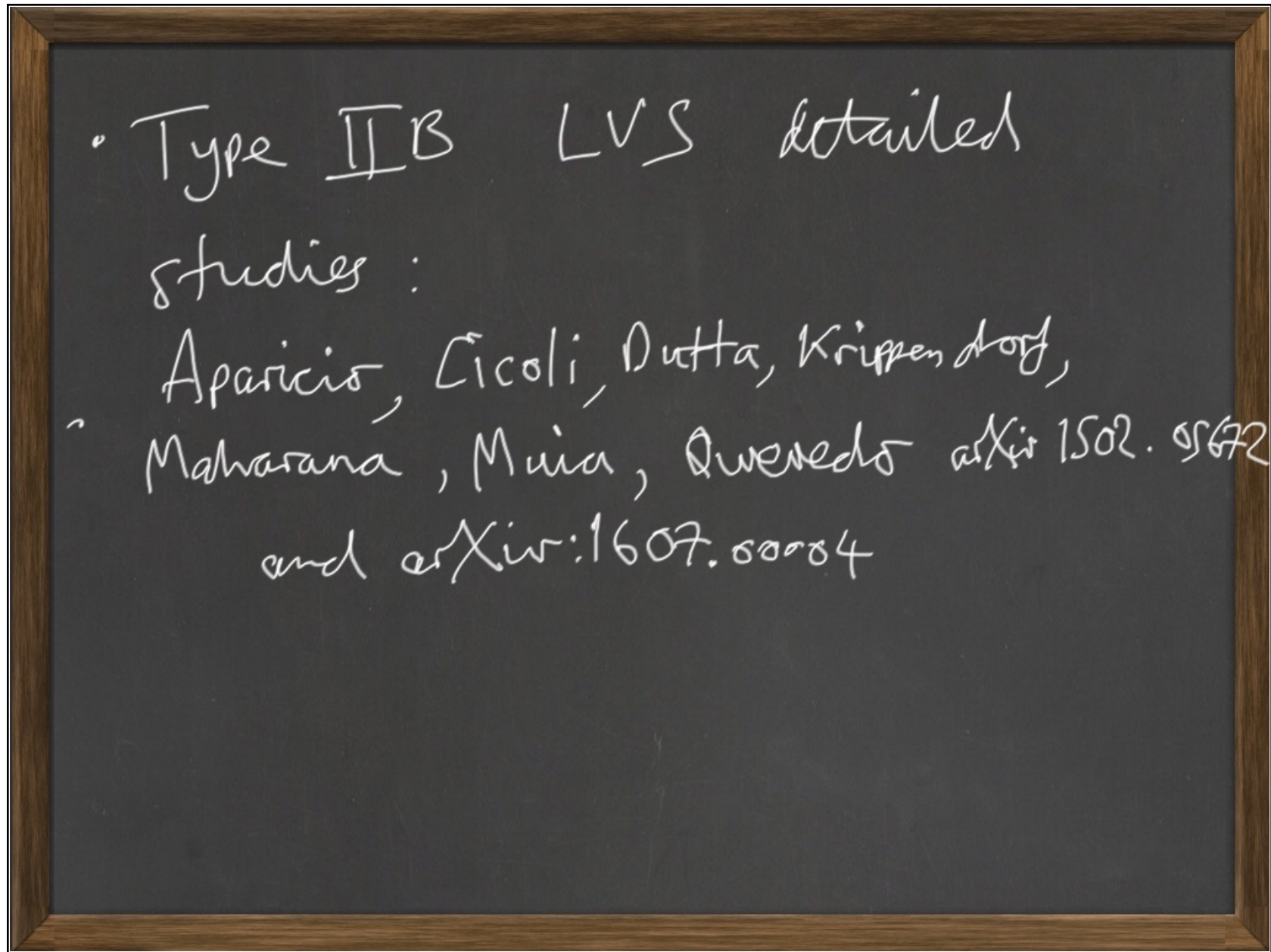


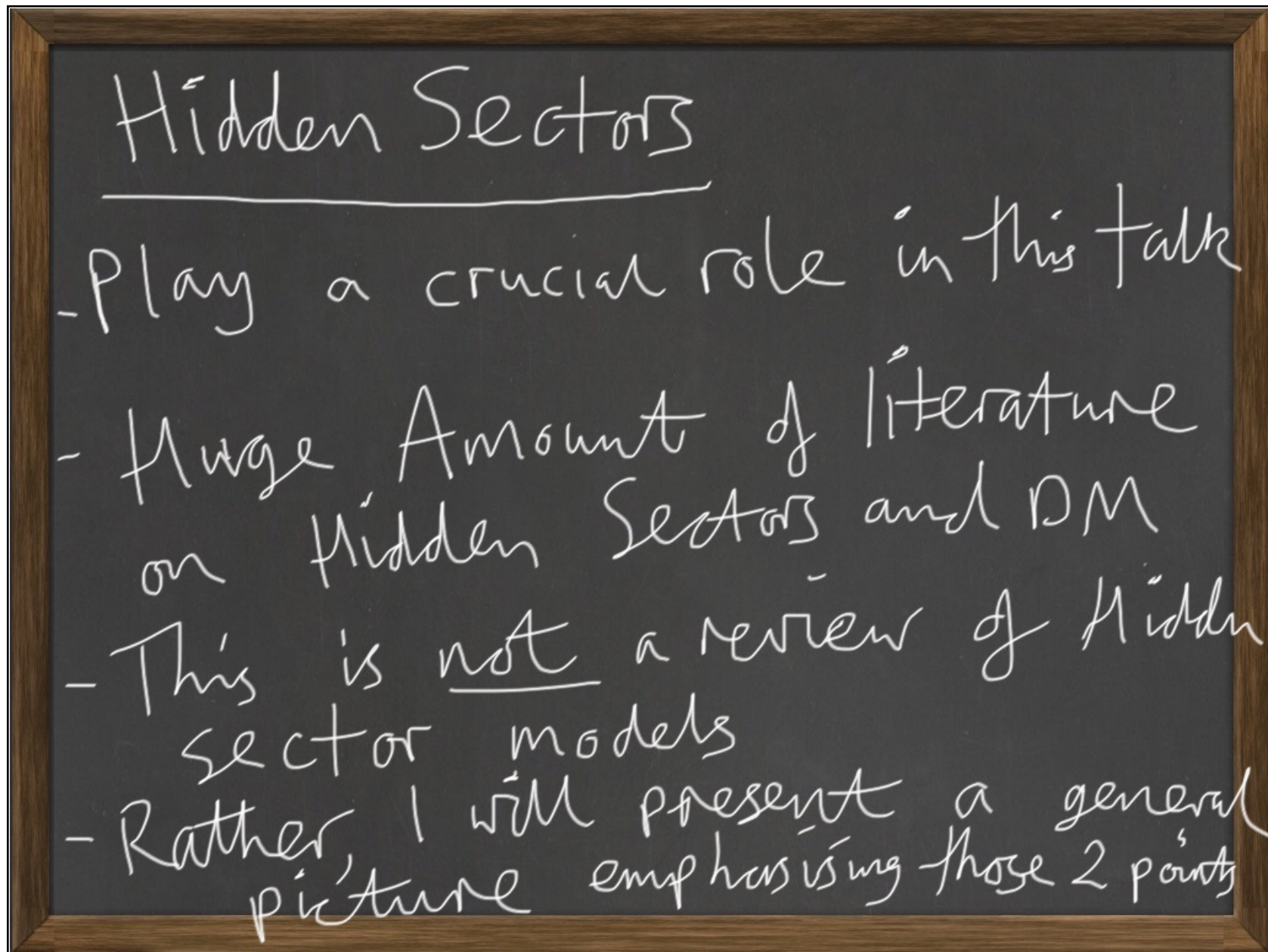
• Cosmological Moduli dynamics
will be extremely important
in the story.

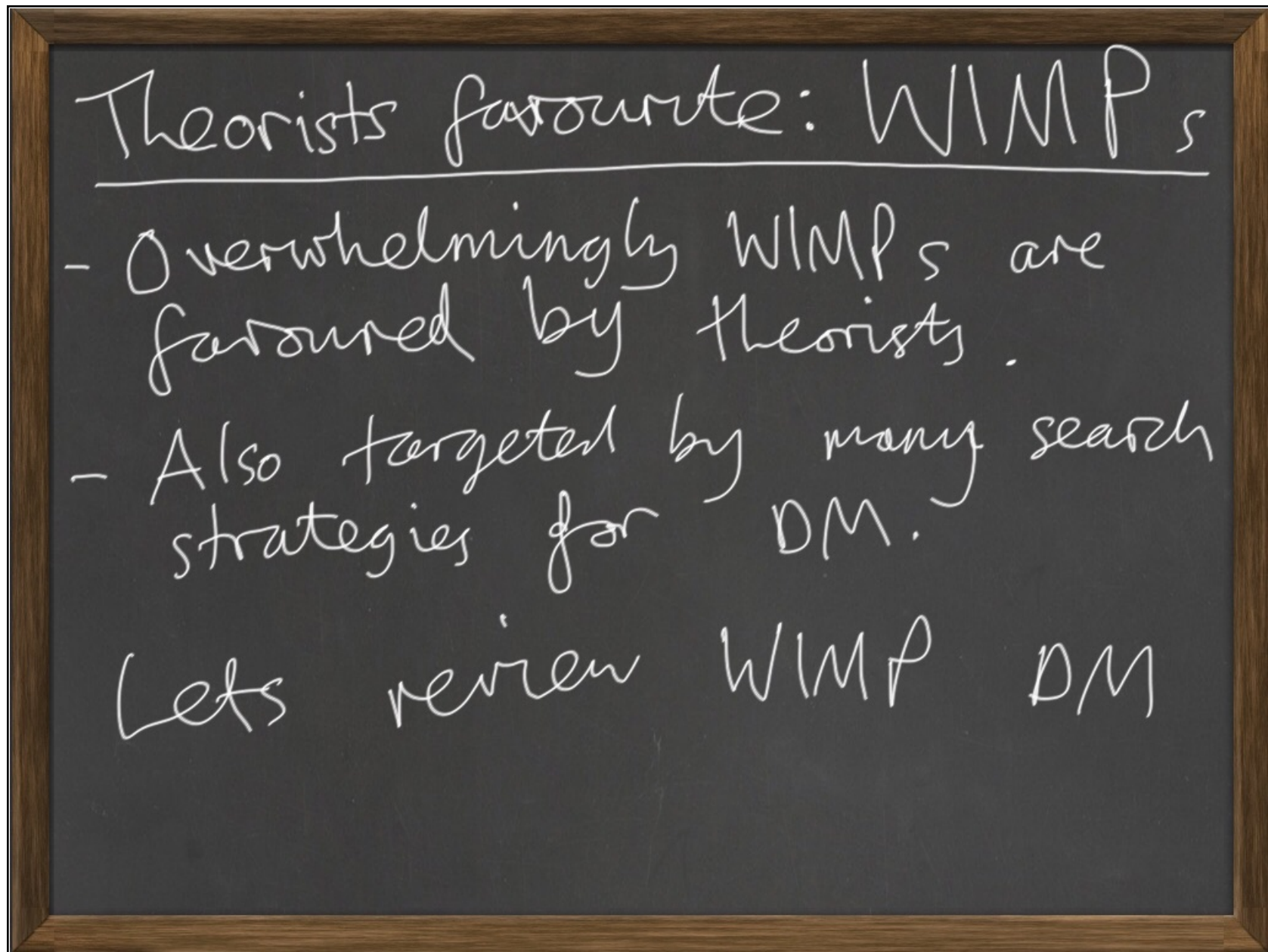
* Carlos, Casas, Quevedo, Roulet 93

also Banks, Kaplan, Nelson 93



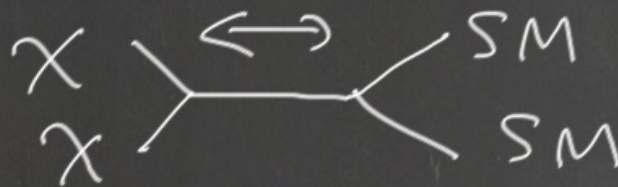






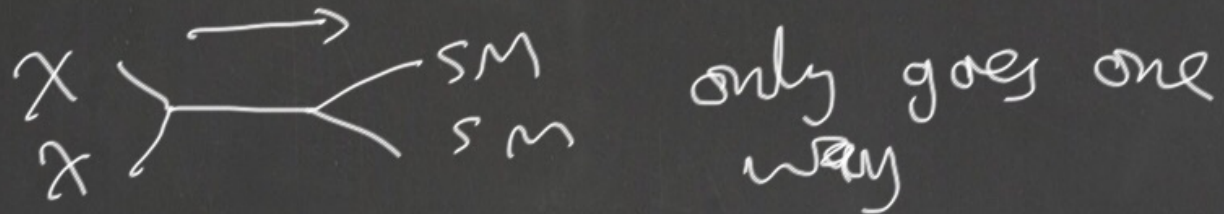
At the end of inflation (or whatever solves the horizon, flatness probs and seeds the CMB!):

- Assume Universe is radiation dominated with a high $T \gg \underline{M_{EW} \sim 100 \text{ GeV}}$
- Standard Model particles are in equilibrium with WIMPs, X



X is a stable, electrically neutral particle charged under $SU(2) \times U(1)_Y$.

As Universe expands, T drops.
 When T falls below m_x ,




And x particles freeze out with

$$H \Big|_{T \sim \frac{m_x}{\text{few}}} \sim n_x$$

$$\langle \sigma v \rangle_{xx \rightarrow SM} < 6 \mu$$

$$H \sim \frac{T^2}{m_{Pl}}$$

$$G_U \approx \frac{\alpha^2}{M_x^2}$$



so $\nu_x \approx \frac{T^2 M_x^2}{\alpha^2 m_{Pl}}$

$$\frac{\rho}{S} \approx \frac{M_x^3}{g_* \alpha^2 T m_{Pl}}$$

$$(S \sim g_* T^3)$$

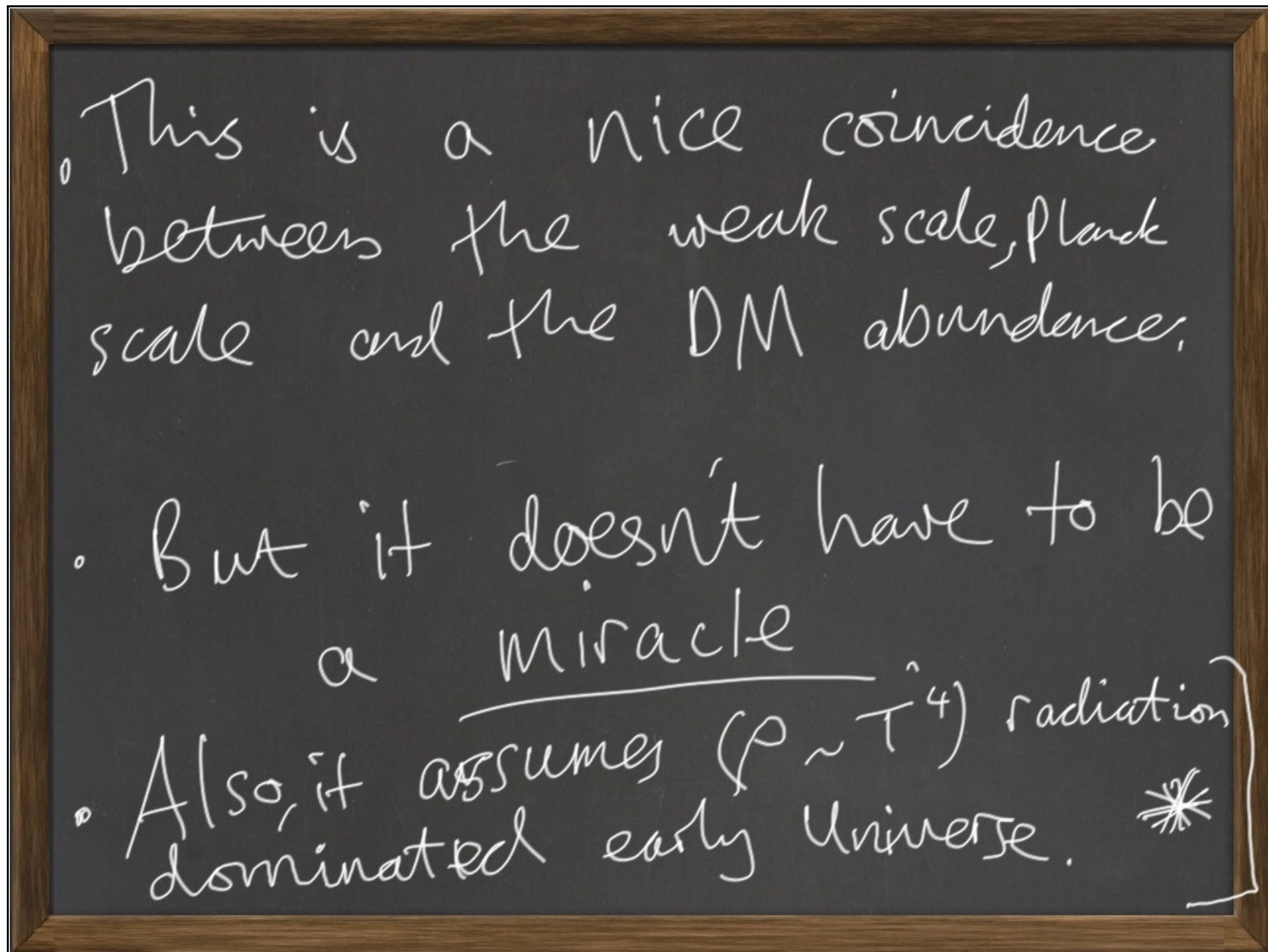
If $T \sim \frac{M_x}{10^2 g_*}$ *

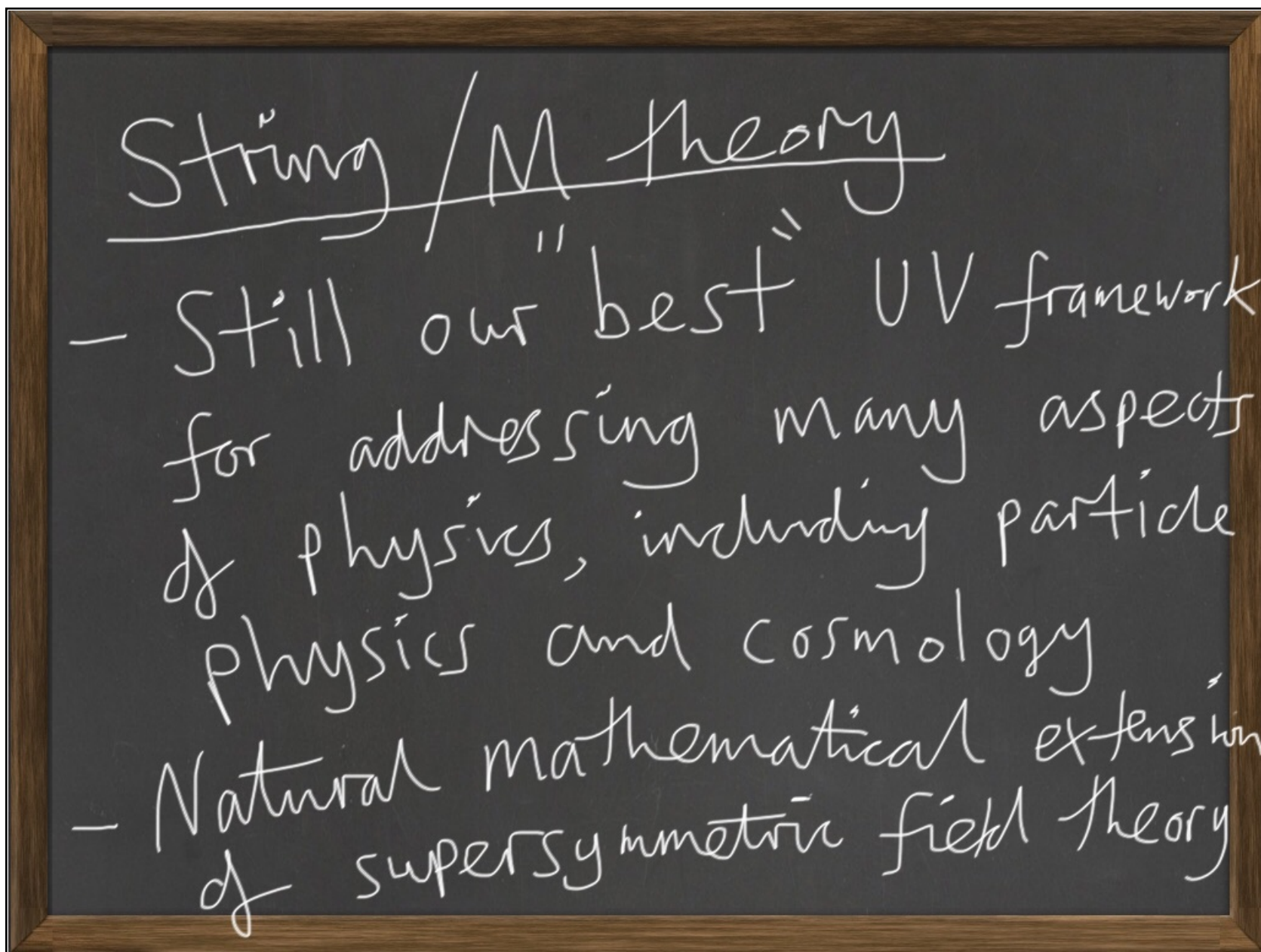
$$\frac{\rho}{S} \sim 10^5 \frac{M_x^2}{m_{Pl}} \sim$$

$$\sim 10^{-10} \text{ GeV}$$

$$\frac{\rho}{s} \approx \frac{M_{\text{X}}^2}{g_* \alpha^2 m_{\text{Pl}}^2}$$

WIMP miracle or coincidence? ②





We will consider the low energy limits of solutions of string/M-theory

\exists many solutions of the form:

$$M^{9,1} = \underbrace{\mathbb{Z}^6}_{\text{compact, small}} \times \underbrace{M^{3,1}}_{\text{large}}$$

or

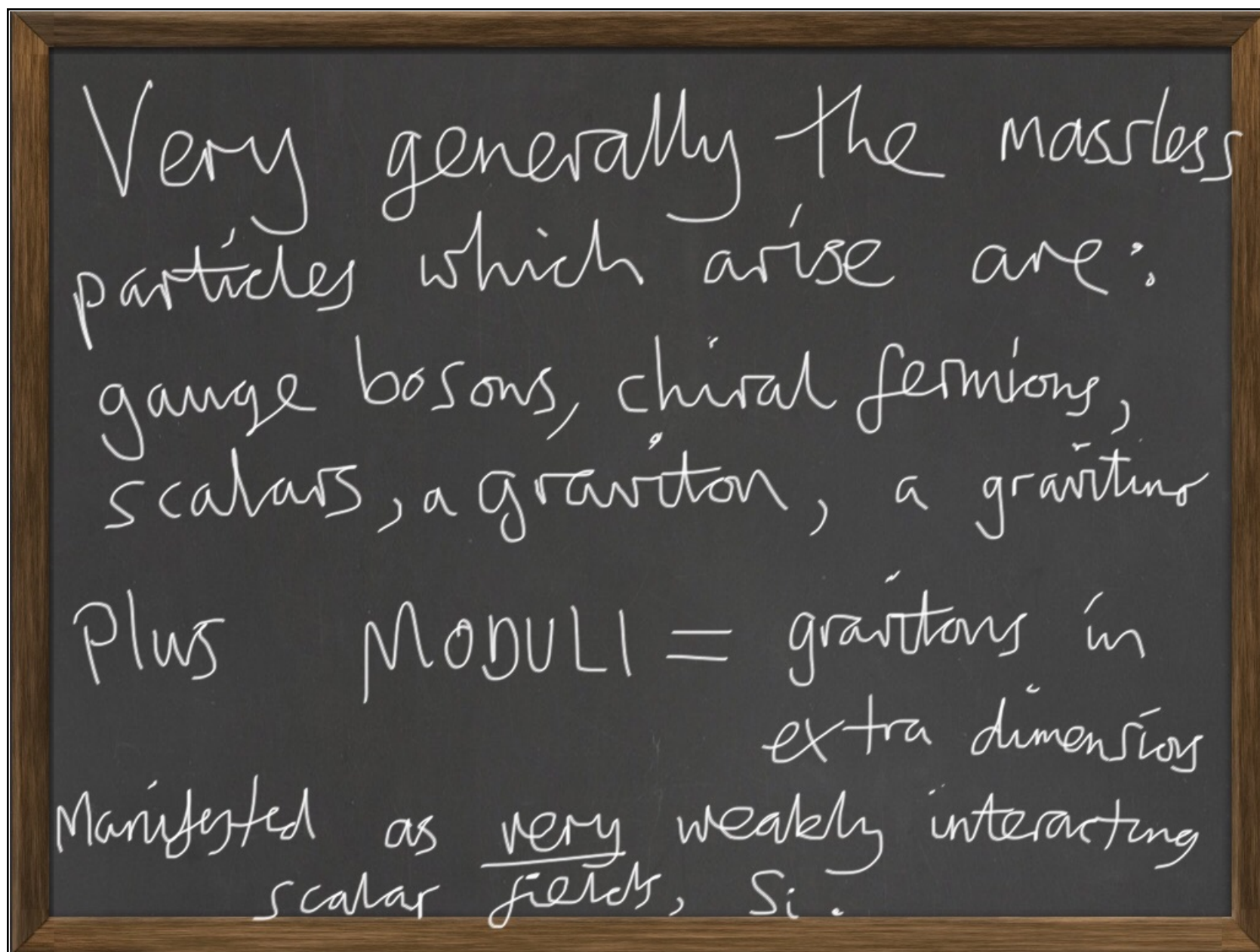
$$M^{10,1} = X^7 \times M^{3,1}$$

$$g(M^{10,1}) \cong g(X) + g(M^{3,1})$$

$\text{Hol}(g(X)) = G_2!$

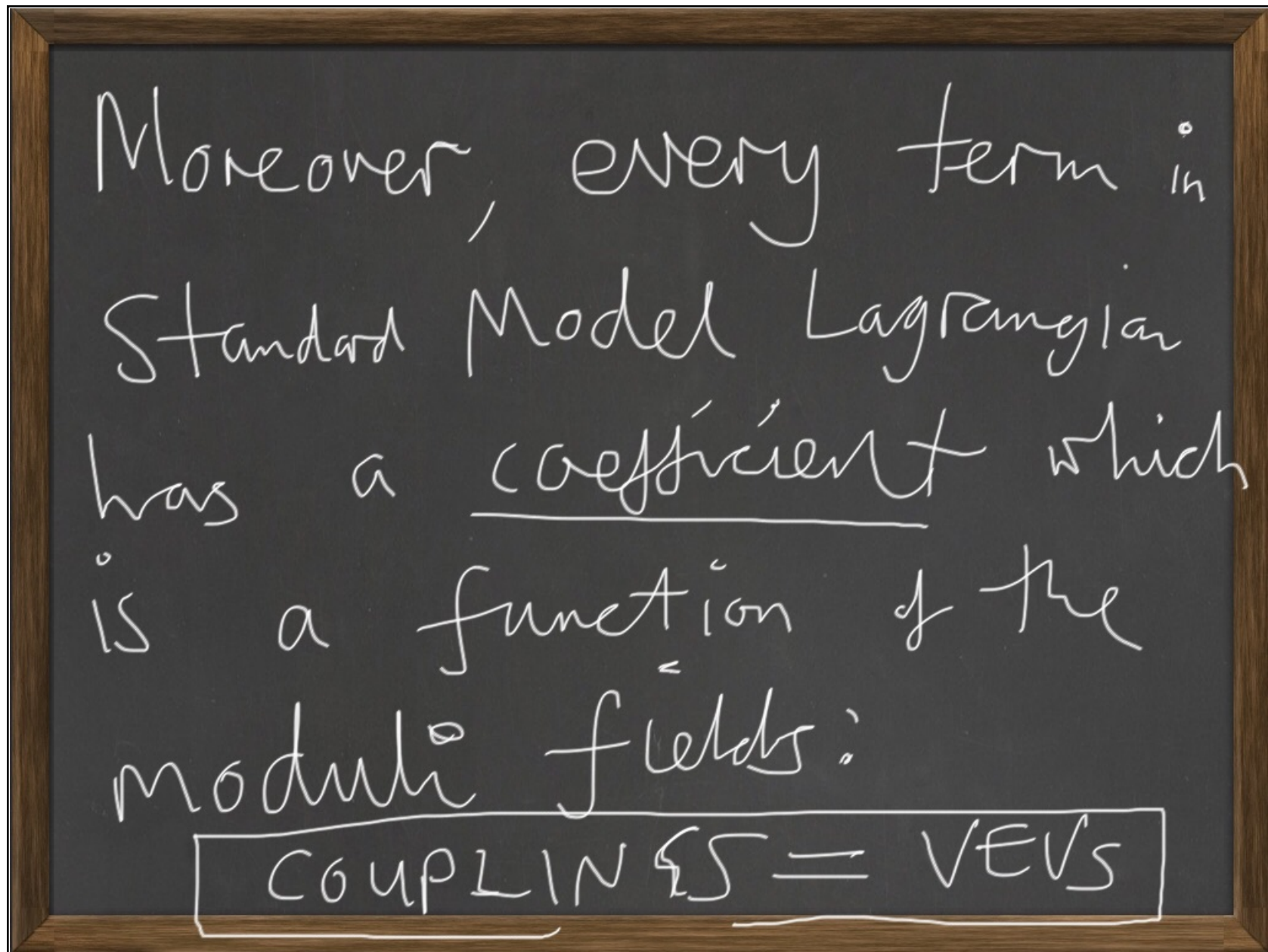
EXTRA

SUSY-D



Low energy, $d=3+1$ Lagrangian is of the form, schematically,

$$\begin{aligned}
 - \int_{\text{matter} + \text{gravity}} &= \frac{1}{16\pi G_N} \sqrt{-g_{3+1}} R_{3+1} + \frac{1}{g^2} \underline{F_{\mu\nu}^2} \\
 &+ i \bar{\Psi} \not{\partial} \Psi + \lambda H \bar{\Psi} \Psi \\
 &+ \underline{|\mathcal{D}H|^2} - \underline{V(H, H^\dagger)} \\
 + \\
 \underline{\underline{\int_{\text{moduli}}}} &= \underline{\kappa^{ij}(s_j)} \left(\underline{d_\mu s_i d^\mu s_j} + \underline{\kappa^{ij}(s)} \underline{d_\mu a_i d^\mu a_j} \right) \\
 &\quad - \underline{V(s_i, a_j)} \\
 s_i &= \text{moduli} \quad a_i = \text{axions} \quad + \dots
 \end{aligned}$$



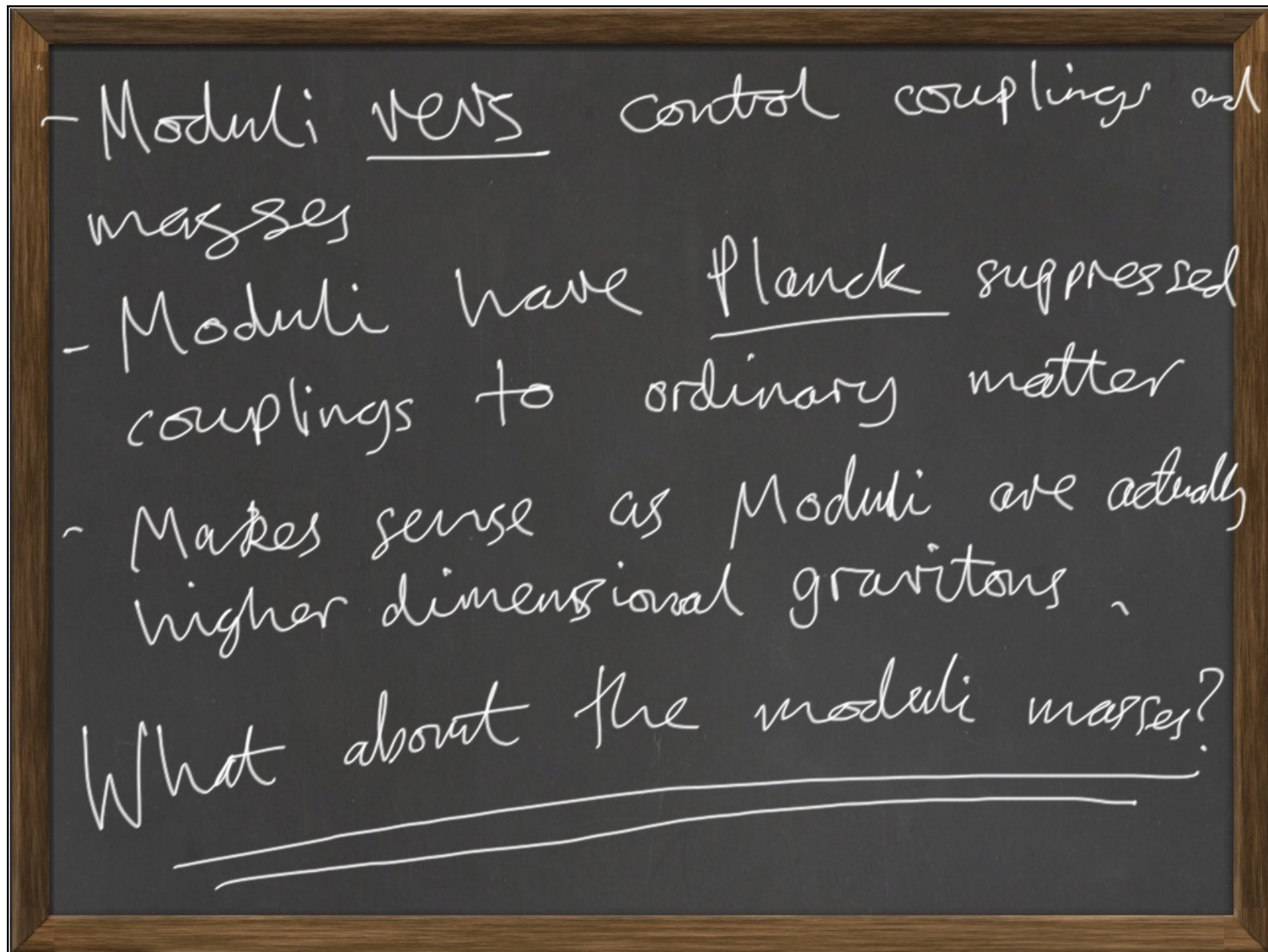
e.g. $\frac{1}{g^2} F_{\mu\nu}^2$ is really

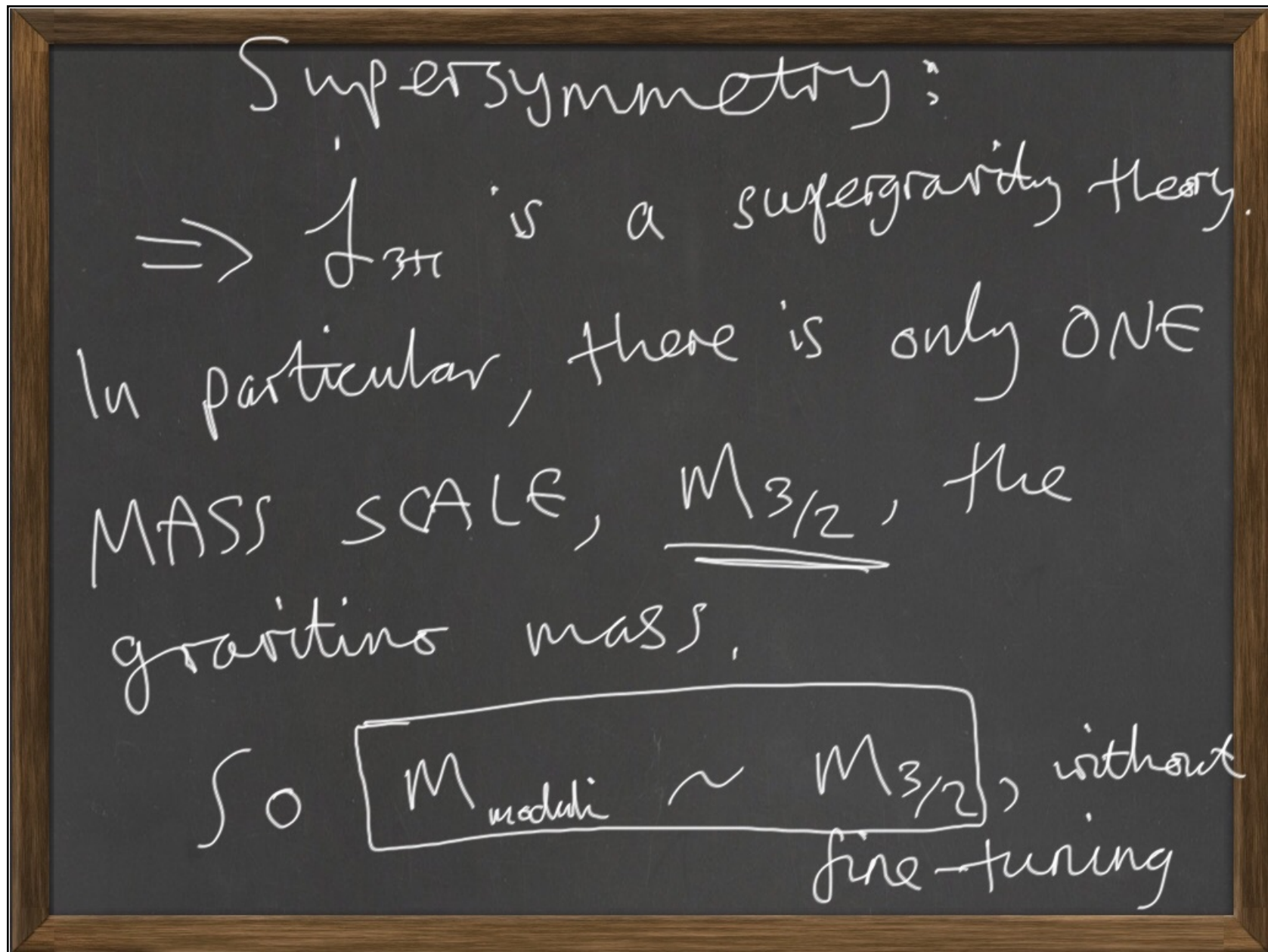
$S \sqrt{G_N} F_{\mu\nu}^2$ $\frac{N_i S_i F_{\mu\nu}^2}{M_{Pl}^2}$, a dim-5 operator.

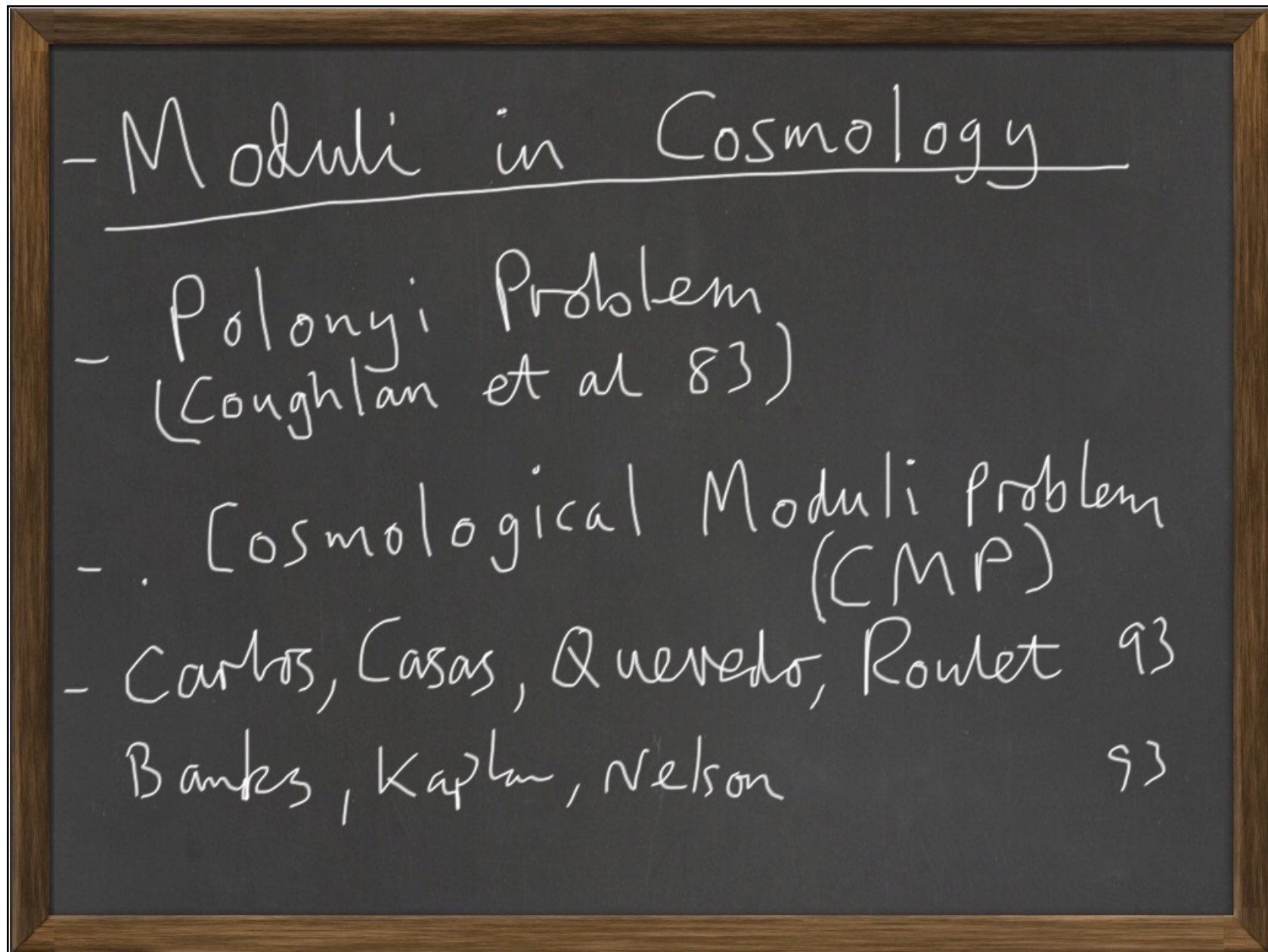
Similarly $\frac{\Lambda}{M_{Pl}} \psi_L \psi_R$ is really

$\psi \rightarrow e^{-\frac{d_i s_i}{M_{Pl}}} e^{\frac{i d_i a_i}{f}} \psi_L \psi_R$

* The moduli dependence of Λ varies from theory to theory.







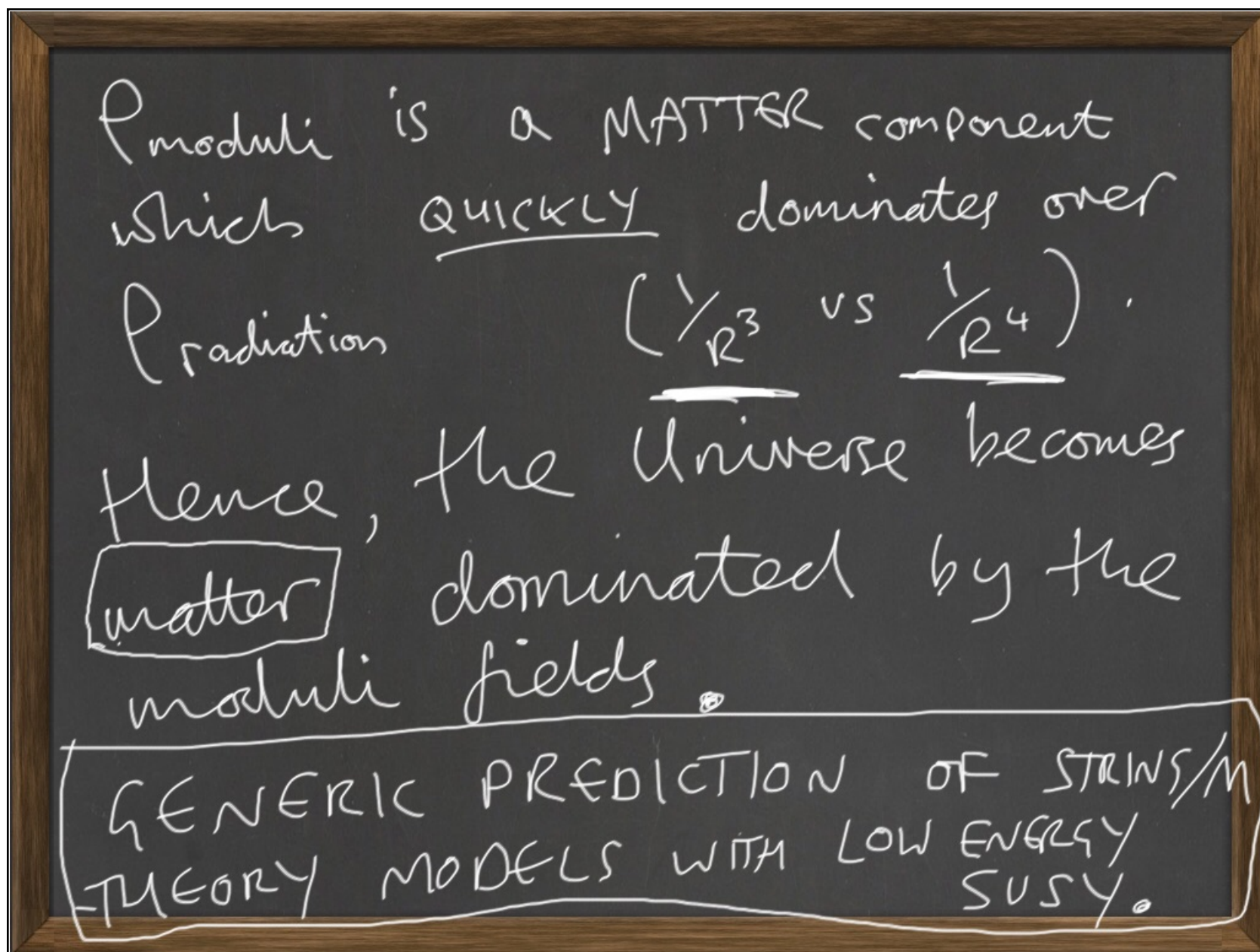
Cosmology of This Theory

At the end of inflation (or whatever.....)

If $H \gg m_{3/2} \sim m_{\text{moduli}}$, the moduli will be stuck at some $O(1) m_{\text{pl}}$ place in its potential.

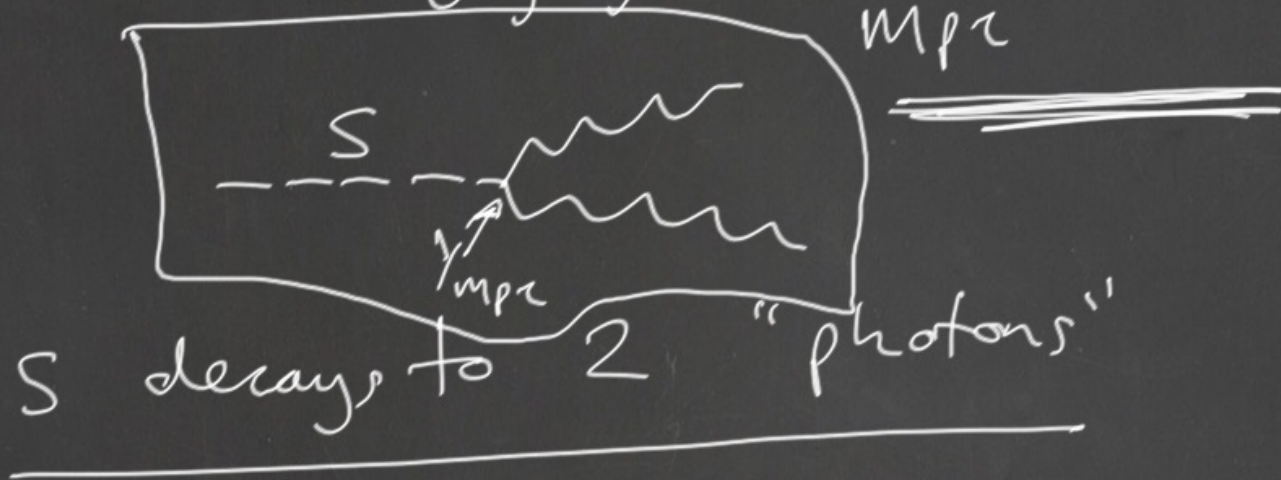
Later, $H \sim O(m_{\text{moduli}})$ and s_{mod} oscillates:

The top diagram shows a potential energy curve $V(s)$ versus s . The curve has a minimum. A point on the curve is marked with a dot and labeled "mp" with a double-headed arrow. The word "Early" is written to the right of the curve. The bottom diagram shows a similar potential energy curve $V(s)$ versus s . A point on the curve is marked with a dot and labeled "H ~ O(m_mod)" with a double-headed arrow.



The moduli are unstable particles.
 (They couple to matter particles fairly
 'generically' and 'uniformly'.)

(Consider, e.g., $\mathcal{L}_{\text{gauge}} \sim \frac{S}{M_{\text{pl}}^2} F_{\mu\nu}^2$



Decay width (or probability) is

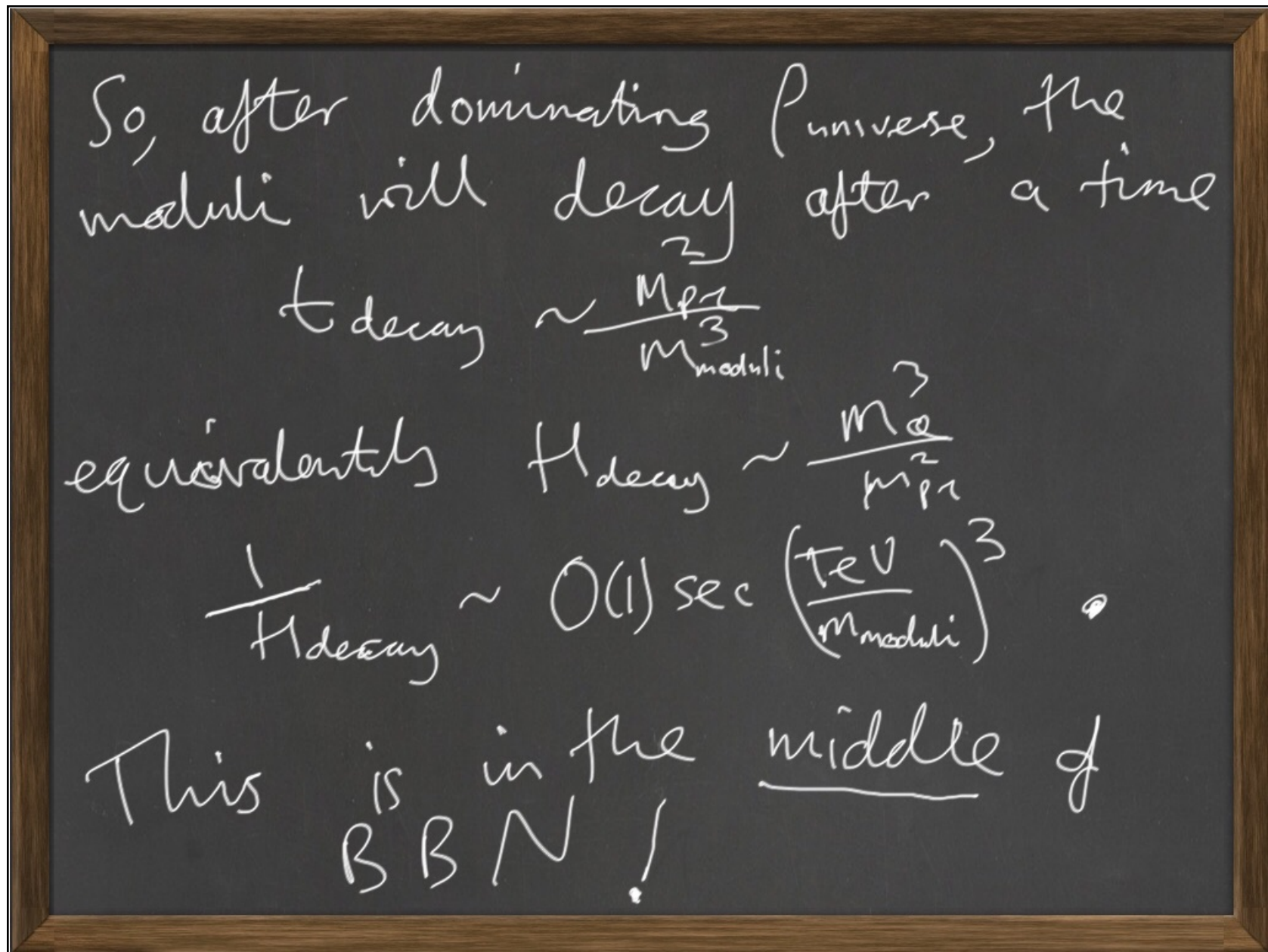
$$\Gamma(s \rightarrow \gamma\gamma) \propto |M|^2$$

$$M \sim \frac{1}{M_{Pl}}$$

$$\Gamma \sim O\left(\frac{1}{M_{Pl}^2}\right) \sim G_N$$

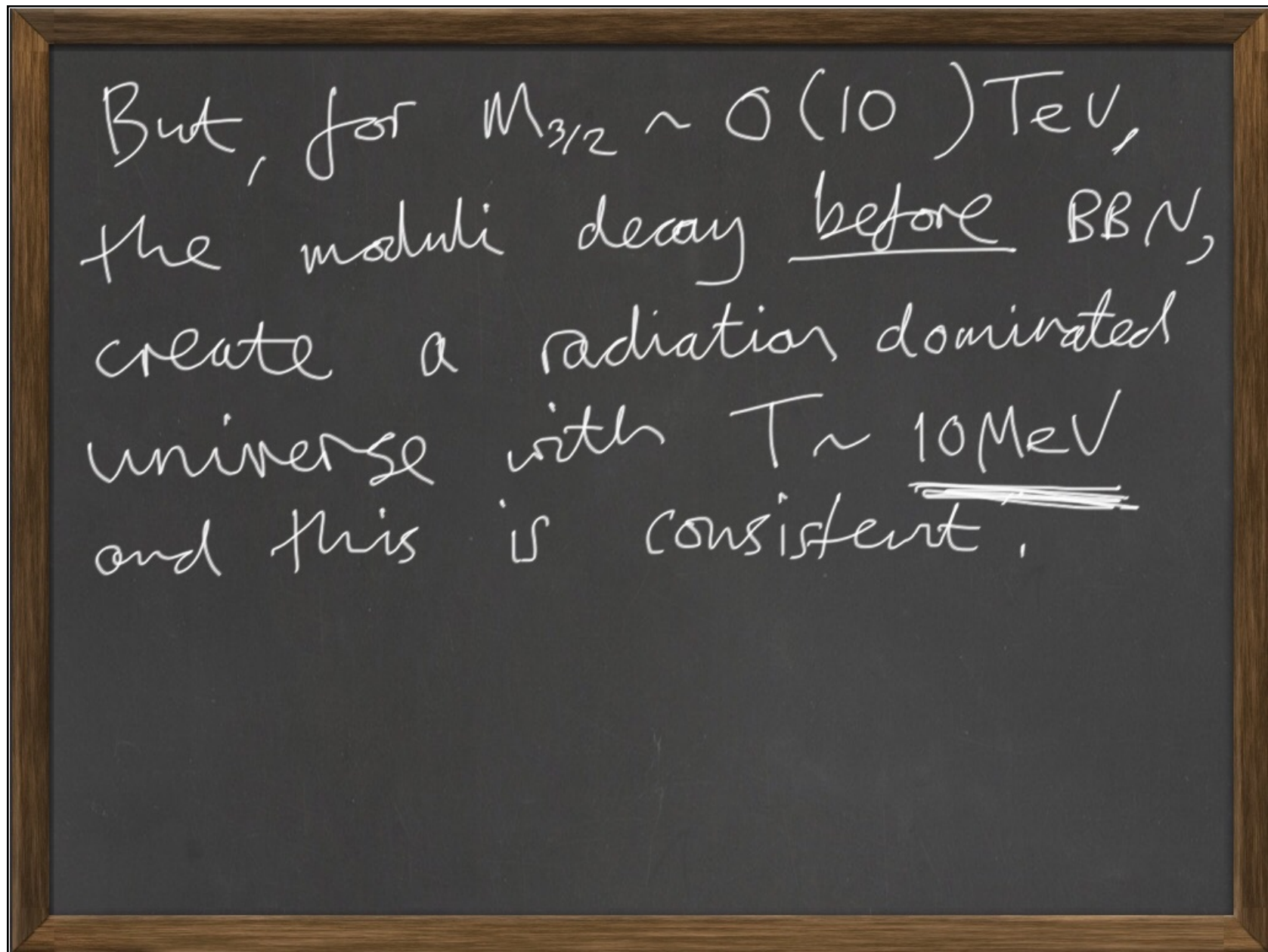
$$\therefore \Gamma(s \rightarrow \gamma\gamma) \approx \frac{M_{moduli}^3}{2 M_{Pl}^2} \times$$

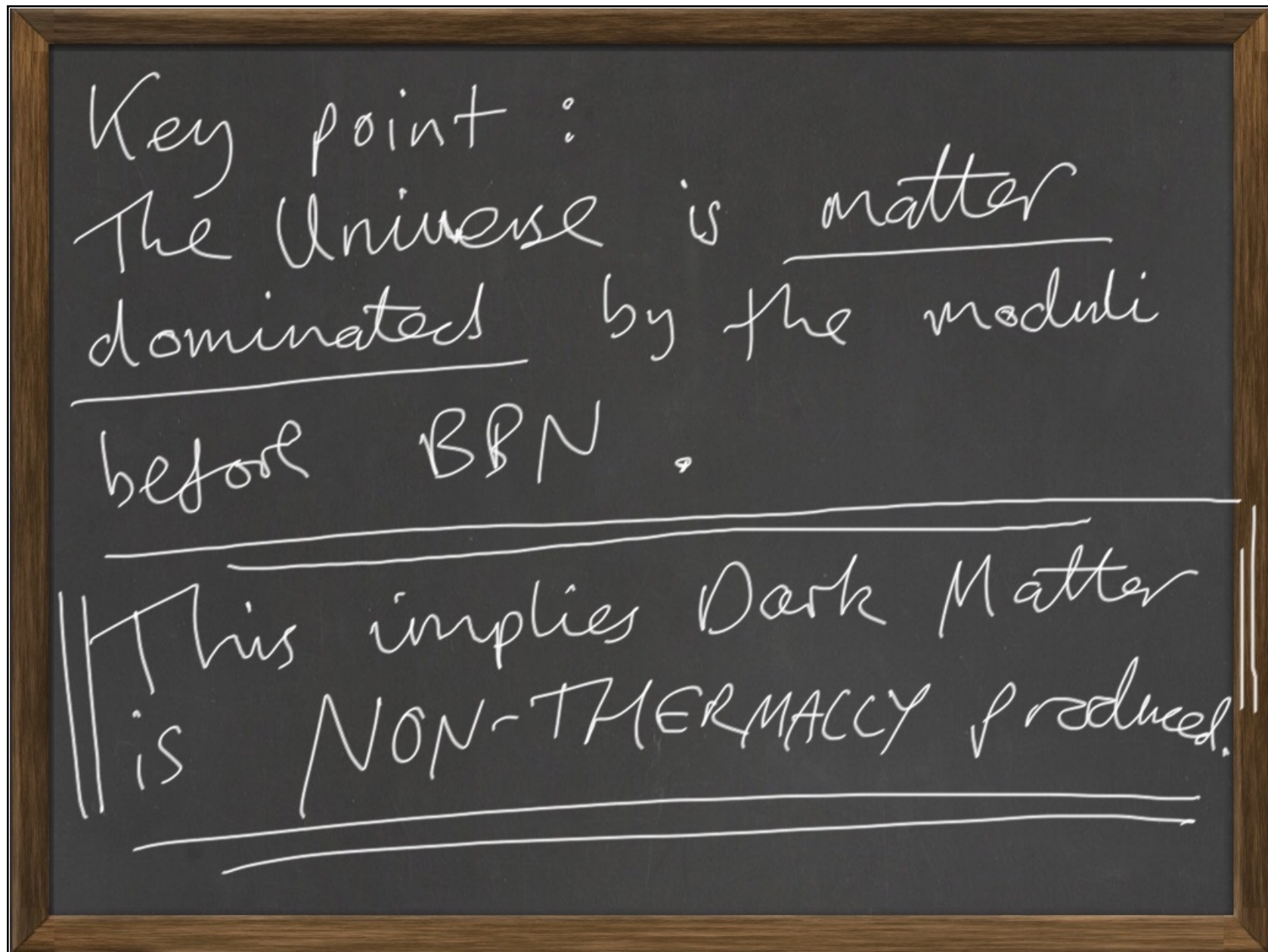
Lifetime $\tau_{moduli} \approx \frac{M_{Pl}^2}{M_{moduli}^3} \leftarrow$



So for $M_{3,2} \sim \text{TeV}$, moduli decay during BBN. This is bad as they decay into quarks, leptons and gauge bosons.

This injects charged particles and hadrons into the plasma which can dis-associate nuclei and drastically change the successful predictions of BBN.

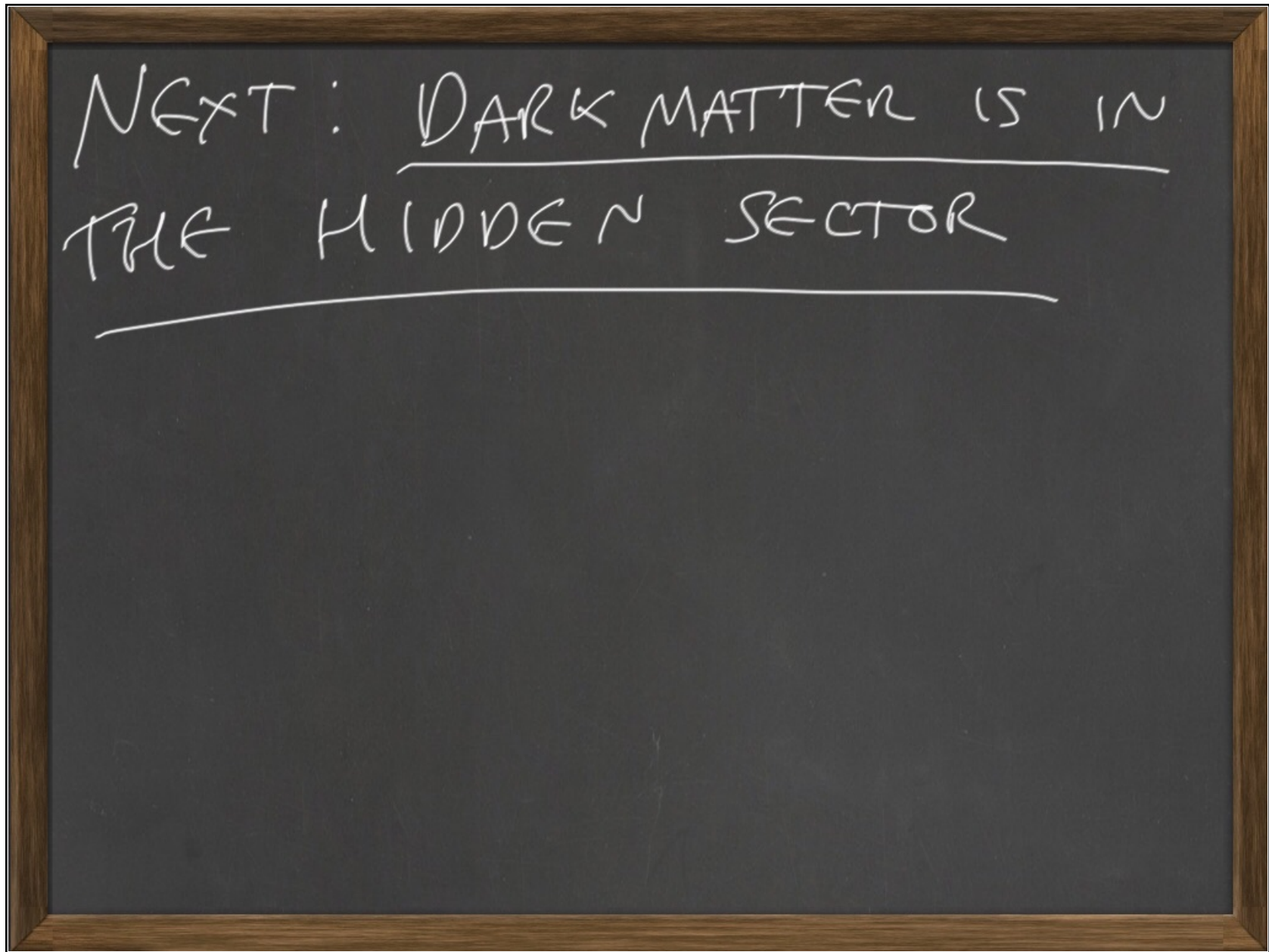




This seems quite a generic
conclusion.

Caveats

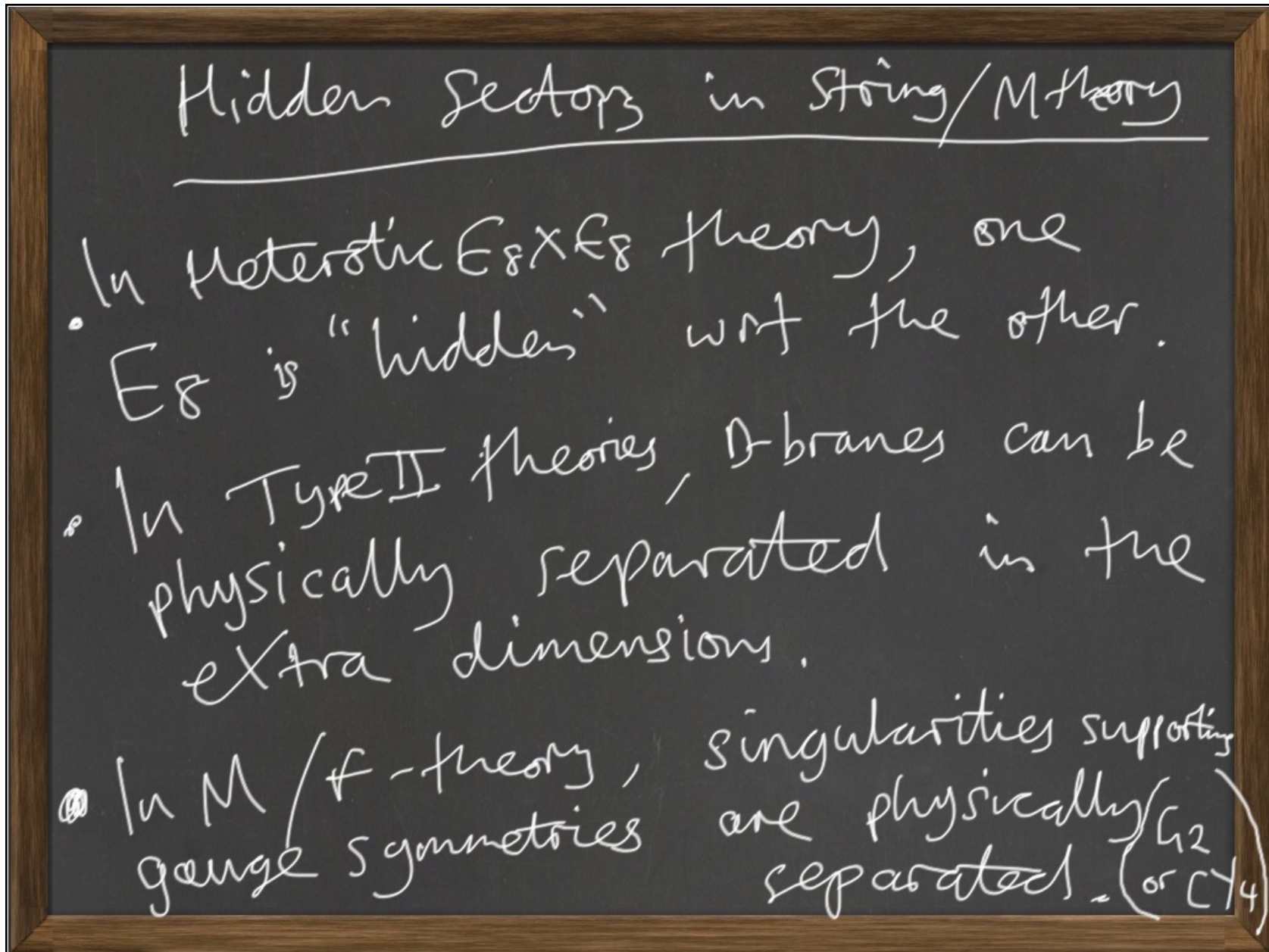
- Could assume $H_{\text{inf}} \ll M_{3/2}$
(not typical)
- Could arrange a late period
of inflation to "get rid of the
moduli". (Seems 'tuned'.)



Hidden Sectors

Defⁿ: A particle is in the
 Hidden sector if it has no
tree level gauge interactions
 with the Standard Model.
 ie it has no $SU(3) \times SU(2) \times U(1)_Y$
 charge at tree level.

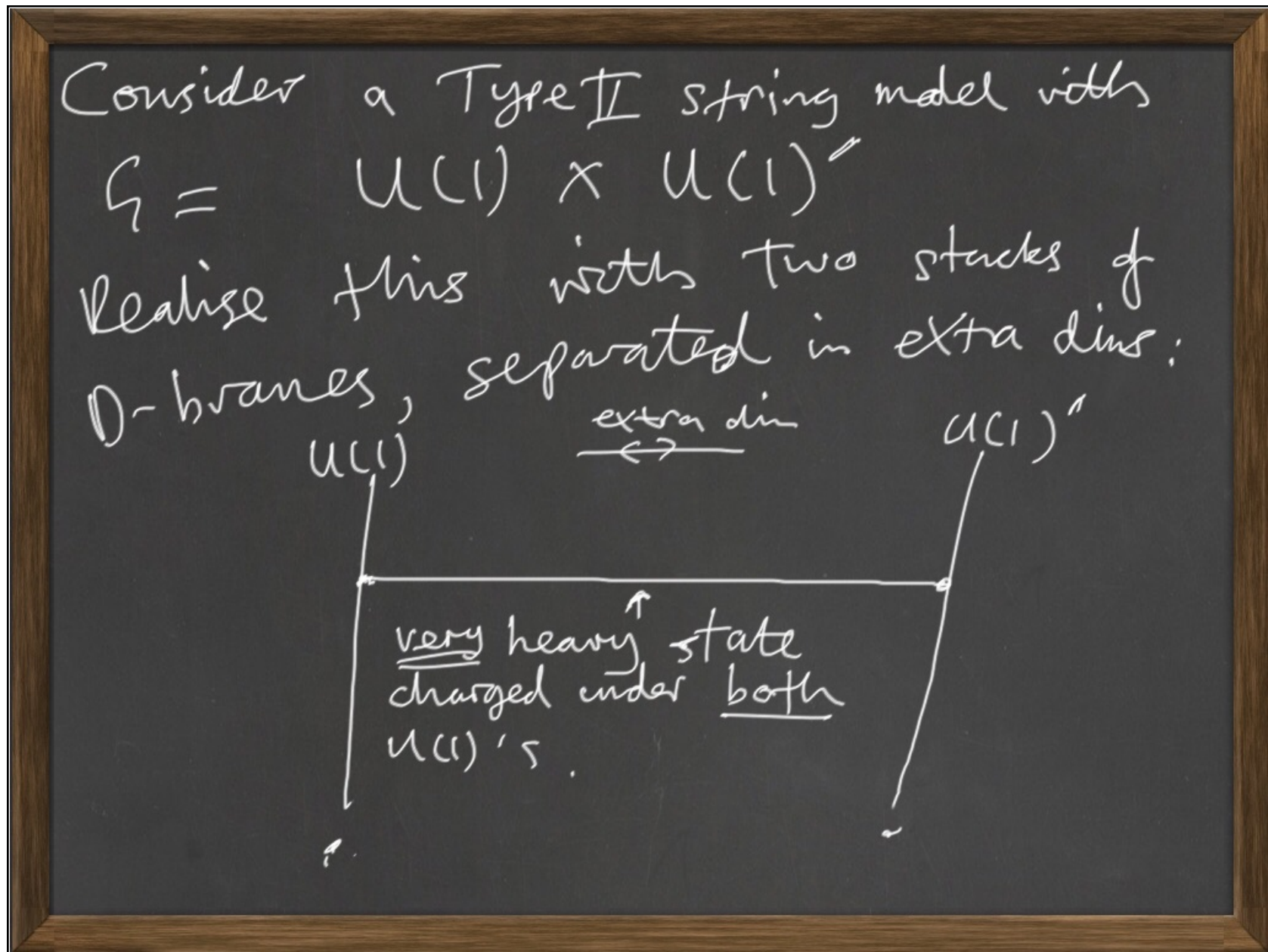
Since we have no idea why the Standard Model has $G = SU(3) \times SU(2) \times U(1)$ and 45 fermions and a Higgs doublet, there is no reason NOT to consider additional gauge sectors and matter. This is exactly the picture that emerges from string/M theory



There is no privilege given to the Standard Model.

Generically expect additional gauge groups and matter.

HIDDEN SECTOR MATTER
IS GENERIC



Mass, heavy state $\sim \frac{M_{str}^2 R_{KK}}{M_{KK}}$

H induces a renormalisation of kinetic terms:

i.e. $F_{\mu\nu}^2 + \tilde{F}_{\mu\nu}^2 \rightarrow F_{\mu\nu}^2 + F_{\mu\nu}'^2 + \epsilon F_{\mu\nu} F_{\mu\nu}'$

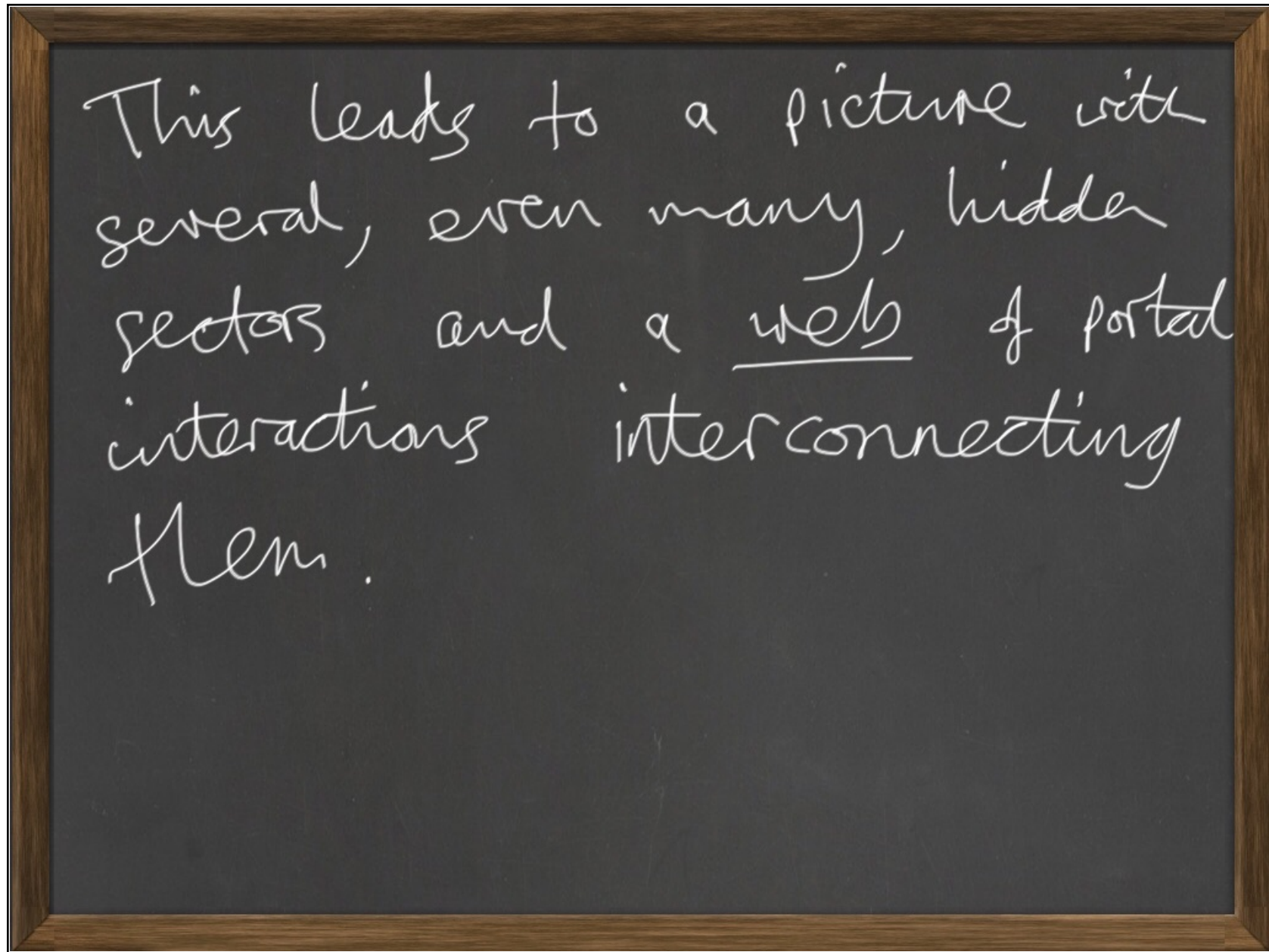
Since FF' is dim 4, ϵ is only log sensitive to UV

$$E \sim \frac{gg'}{12\pi^2} \ln \left(\frac{\Lambda}{M} \right).$$

- Such mixings are generically present between U(1)'s.

- This has been known for quite some time (Dienes, Kolda, March-Russell '97)

The $\epsilon F F'$ interactions (and those related to it by supersymmetry) provides a PORTAL between different hidden sectors, eg gauge bosons can mix between sectors, as can gauginos, via $\epsilon \lambda \phi \lambda'$.



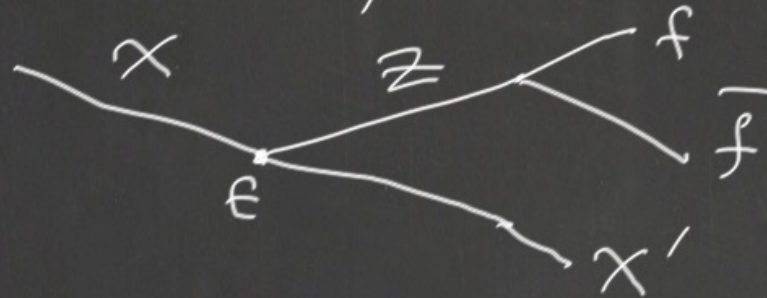
Consider now the (supersymmetric) Standard Model sector. This has a (so-called) "Lightest Supersymmetric Particle" which is often the WIMP DM candidate.

(Usually (without hidden sectors) this is stable as it is the lightest particle with non zero R-parity.

With multiple hidden sectors, there is NO GOOD REASON why the LVSP* should be the lightest R-charge charged particle in the theory. It could happen by accident, but is unlikely.

*LVSP = Lightest Visible Sector Supersymmetric Particle

Mixing between Hidden $U(1)'$
and $U(1)_Y$ leads to, e.g.



and $\tau_X \sim 10^{-17} \text{ s} \left(\frac{10^{-3}}{\epsilon}\right)^2 \times \text{mixing angles}^2$
for on shell Z

$\tau_X \sim 10^{-9} \text{ s} \left(\frac{10^{-3}}{\epsilon}\right)^2 \left(\frac{50 \text{ GeV}}{m_X - m_{X'}}\right)^4 \times \text{angles}^4$
for 3-body decay

