



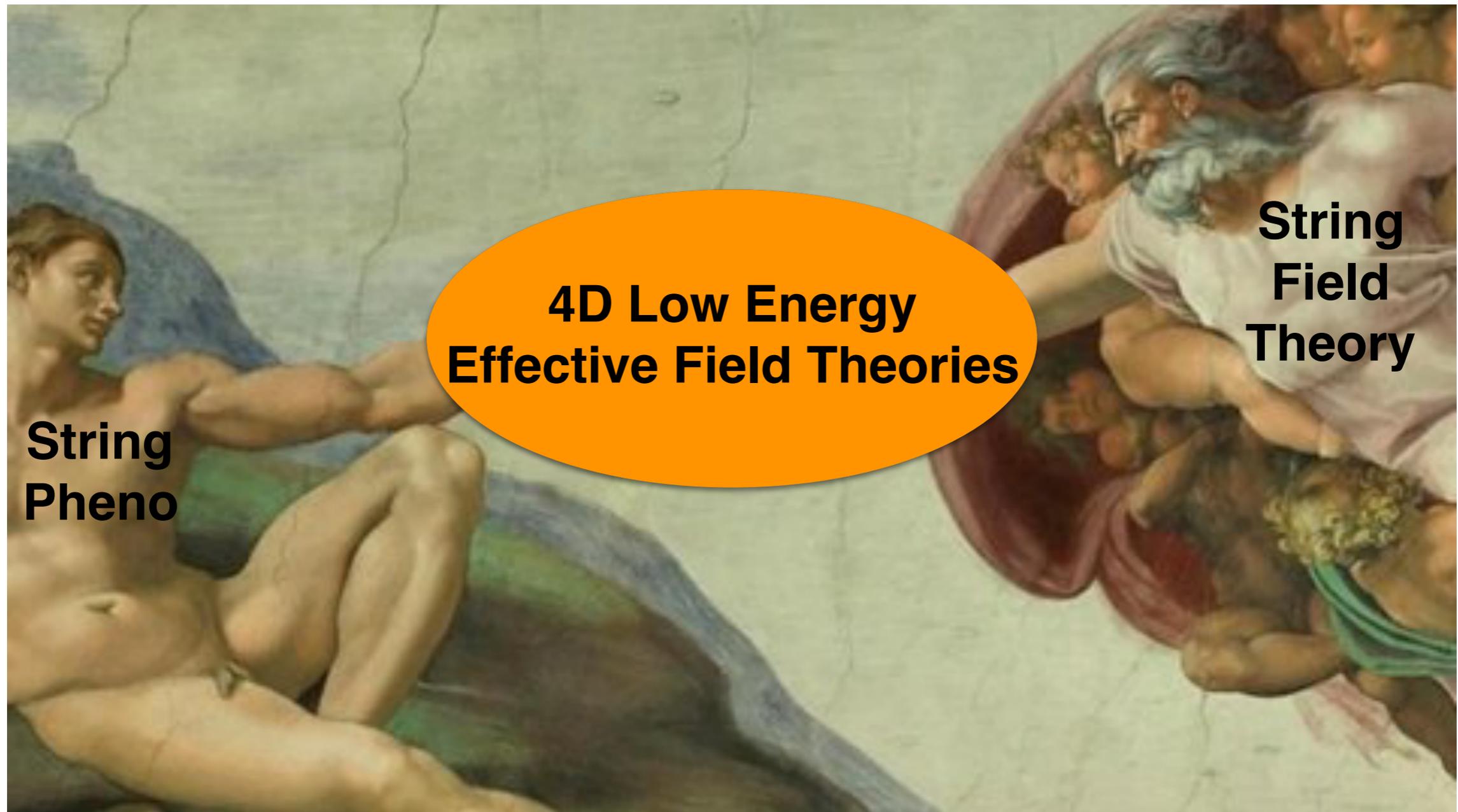
Swampland Conjectures and their Phenomenological Applications

Gary Shiu
University of Wisconsin-Madison

String Field Theory & String Phenomenology



String Field Theory & String Phenomenology



String Theory Landscape



String Theory Landscape

Anything goes?

A scenic landscape photograph of a mountain valley. In the foreground, a calm lake reflects the surrounding mountains and sky. The middle ground shows a valley with dense green forests on the lower slopes of the mountains. The background features more rugged, rocky mountain peaks under a bright blue sky with wispy white clouds. The overall scene is peaceful and majestic.

An even vaster Swampland?



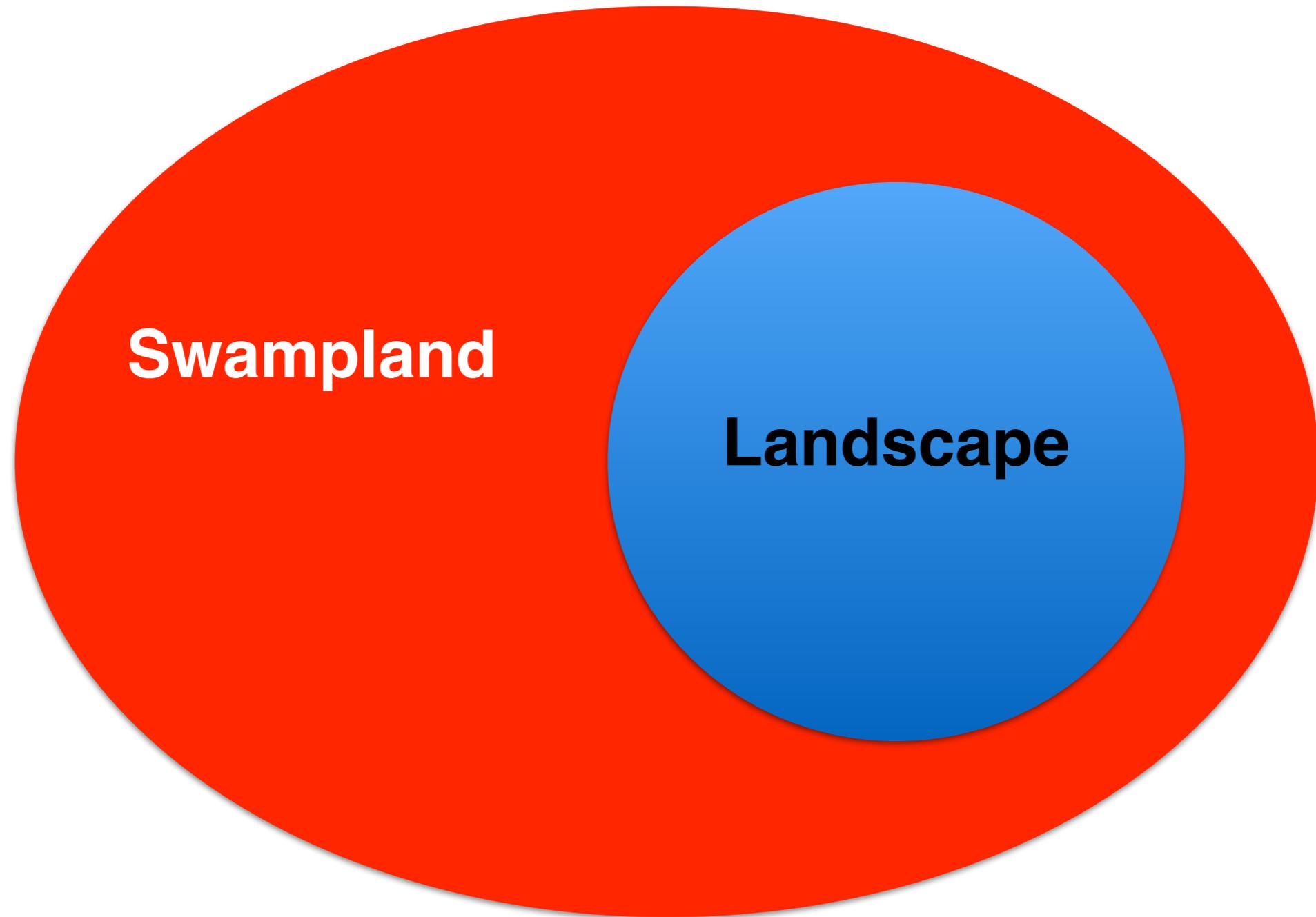
An even vaster Swampland?



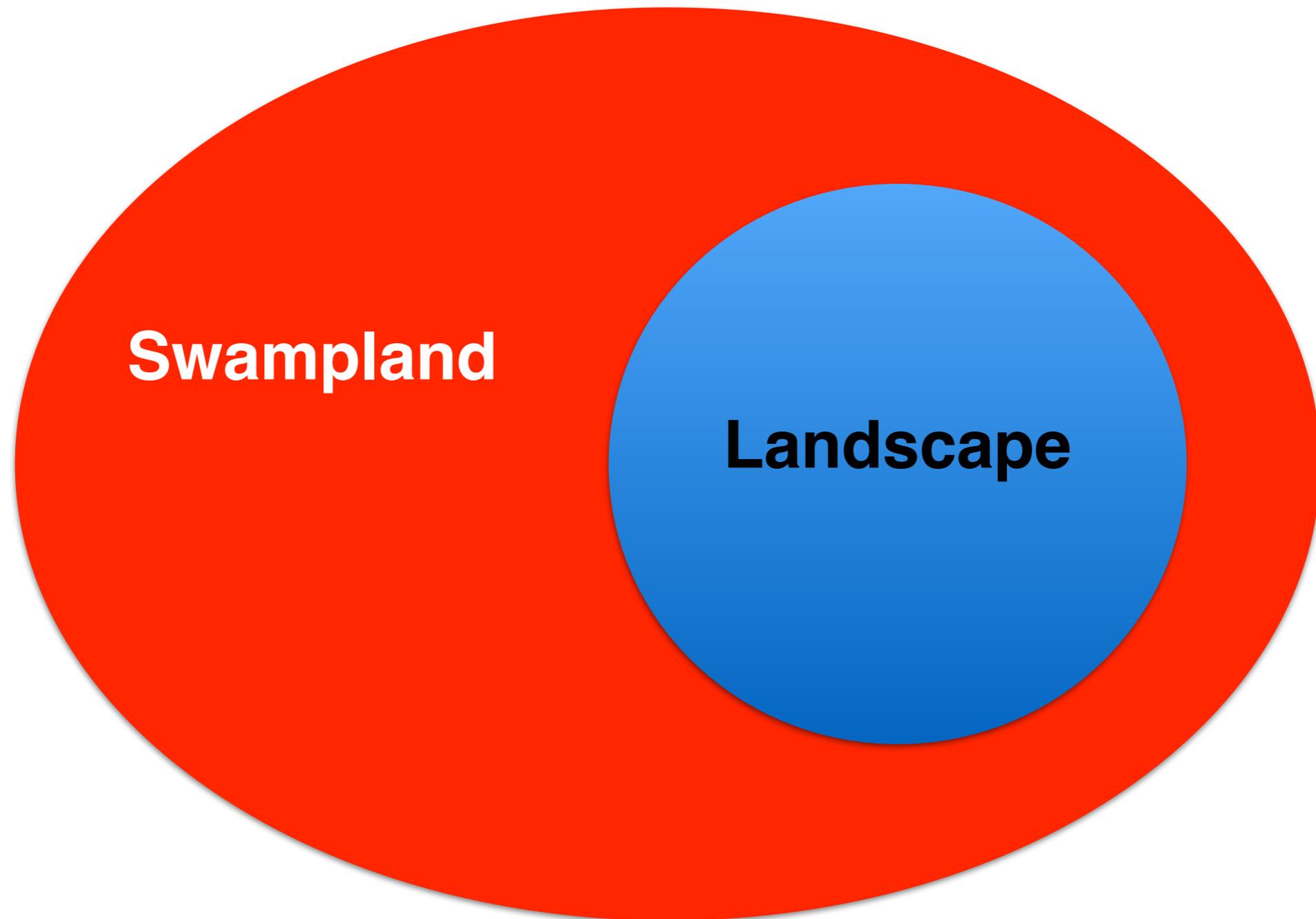
Landscape vs Swampland



Landscape vs Swampland



Landscape vs Swampland



We refer to the space of quantum field theories which are incompatible with quantum gravity as the ***swampland***. [Vafa, '05]

Based on work with:



J. Brown



W. Cottrell



P. Soler



M. Montero



Y. Hamada



S. Andriolo



D. Junghans



T. Noumi

J. Brown, W. Cottrell, GS, P. Soler, JHEP **1510**, 023 (2015), JHEP **1604**, 017 (2016), JHEP **1610** 025 (2016).

M. Montero, GS and P. Soler, JHEP **1610** 159 (2016).

W. Cottrell, GS and P. Soler, arXiv:1611.06270 [hep-th].

Y. Hamada and GS, JHEP **1711**, 043 (2017).

S. Andriolo, D. Junghans, T. Noumi and GS, arXiv: 1802.04287 [hep-th].

Outline

- What is the Weak Gravity Conjecture?
- Phenomenological applications of the WGC
 - Axions, large field inflation, and CMB B-mode
 - QCD axion
 - Relating Neutrino masses and type with the CC.
- Evidences for the WGC
- Conclusions

Quantum Gravity and Global Symmetries

QG and Global Symmetries

- **Global symmetries** are expected to be violated by gravity:



- **No hair theorem:** Hawking radiation is insensitive to Q .
 - ➔ Infinite number of states (remnants) with $m \lesssim M_p$
 - ➔ Violation of entropy bounds. At finite temperature (e.g. in Rindler space), the density of states blows up. Susskind '95
- **Swampland conjecture:** theories with exact global symmetries are not UV-completable.
- In (perturbative) string theory, all symmetries are gauged
- Many phenomenological ramifications, e.g., mini-charged DM comes with a new massless gauge boson [GS, Soler, Ye, '13].

The Weak Gravity Conjecture



The Weak Gravity Conjecture

- We have argued that global symmetries are in conflict with Quantum Gravity
- Global symmetry = gauge symmetry at $g=0$
 - It is not unreasonable to expect problems for gauge theories in the weak coupling limit: $g \rightarrow 0$
- When do things go wrong? How? ...

The Weak Gravity Conjecture

Arkani-Hamed, Motl, Nicolis, Vafa '06

- The conjecture:

“Gravity is the Weakest Force”

- For every long range gauge field there exists a particle of charge q and mass m , s.t.

$$\frac{q}{m} M_P \geq \text{“1”}$$

- Seems to hold for all known string theory models.

The Weak Gravity Conjecture

Arkani-Hamed, Motl, Nicolis, Vafa '06

- The conjecture:

“Gravity is the Weakest Force”

- For every long range gauge field there exists a particle of charge q and mass m , s.t.

$$\frac{q}{m} M_P \geq \text{“1”} \equiv \frac{Q_{Ext}}{M_{Ext}} M_P$$

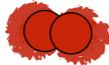
- Seems to hold for all known string theory models.

The Weak Gravity Conjecture

- Take U(1) gauge theory and a scalar with $m > q M_p$



- Stable bound states: the original argument

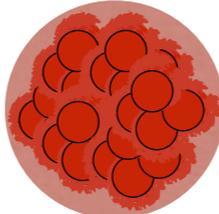


$$2m > M_2 > 2q$$



$$3m > M_3 > 3q$$

...



$$Nm > M_N > Nq$$

...



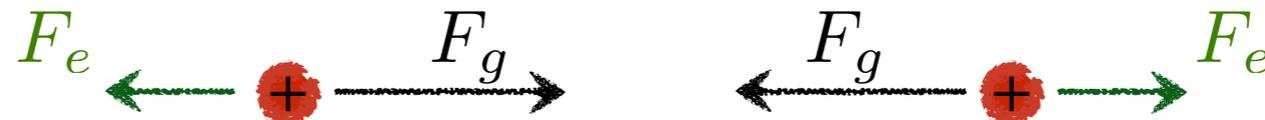
$$M_\infty \rightarrow Q_\infty$$

- All these BH states are **exactly stable**. In particular, large bound states (charged black holes) do not Hawking radiate once they reach the extremal limit $M=Q$, equiv. $T=0$.

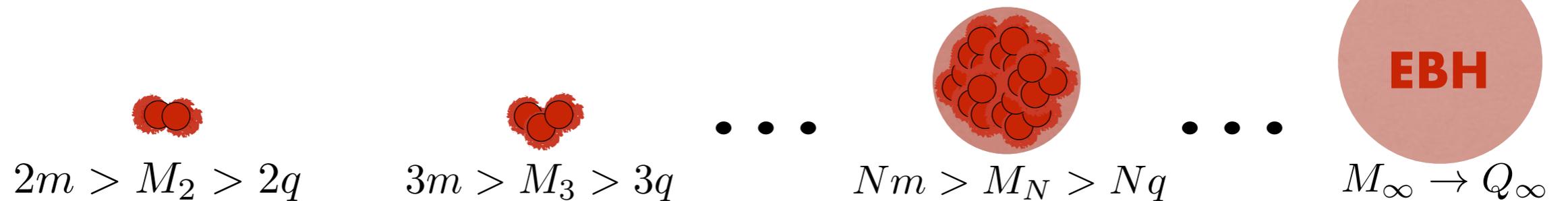
“...there should not exist a large number of exactly stable objects (extremal black holes) whose stability is not protected by any symmetries.”

The Weak Gravity Conjecture

- Take U(1) gauge theory and a scalar with $m > q M_p$



- Stable bound states: the original argument



- All these BH states are **exactly stable**. In particular, large bound states (charged black holes) do not Hawking radiate once they reach the extremal limit $M=Q$, equiv. $T=0$.

“...there should not exist a large number of exactly stable objects (extremal black holes) whose stability is not protected by any symmetries.”

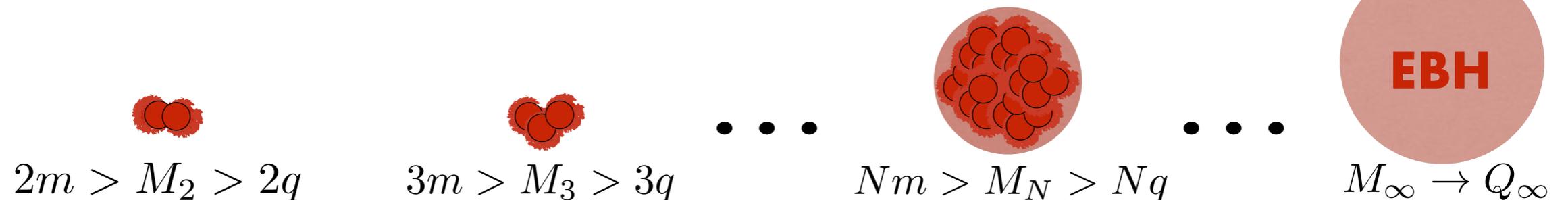


The Weak Gravity Conjecture

- Take U(1) gauge theory and a scalar with $m > q M_p$



- Stable bound states: the original argument

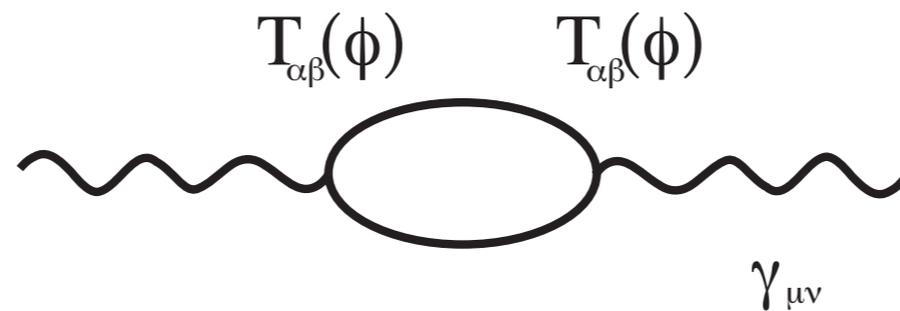


- All these BH states are **exactly stable**. In particular, large bound states (charged black holes) do not Hawking radiate once they reach the extremal limit $M=Q$, equiv. $T=0$.
- In order to avoid a large number of exactly stable states one must demand the existence of some particle with

$$\frac{q}{m} \geq \frac{Q_{ext}}{M_{ext}} = \frac{1}{M_p}$$

Why is this a conjecture?

- Heuristic argument suggests \exists a state w/ $\frac{q}{m} \geq "1" \equiv \frac{Q_{Ext}}{M_{Ext}}$
- One often invokes the remnants argument [Susskind] for the WGC but the situations are different (finite vs infinite mass range).



- Perfectly OK for some extremal BHs to be stable [e.g., Strominger, Vafa] as $q \in$ central charge of SUSY algebra.
 - No $q > m$ states possible (\because BPS bound).
 - More subtle for theories with some $q \notin$ central charge
- The WGC is a conjecture on the ***finiteness of the # of stable states that are not protected by a symmetry principle.***

WGC for Axions

Axions and ALPs

The QCD axion [Wilczek, '78]; [Weinberg, '78] was introduced in the context of the Pecci-Quinn mechanism and the strong CP problem.

An axion enjoys a **perturbative shift symmetry**.

String theory has many **higher-dimensional form-fields**:

e.g. $F = dA$

3-form flux $\xrightarrow{\quad}$ \uparrow \uparrow $\xleftarrow{\quad}$ 2-form gauge potential:

gauge symmetry: $A \rightarrow A + d\Lambda$

Integrating the 2-form over a 2-cycle gives an **axion-like particle (ALP)**:

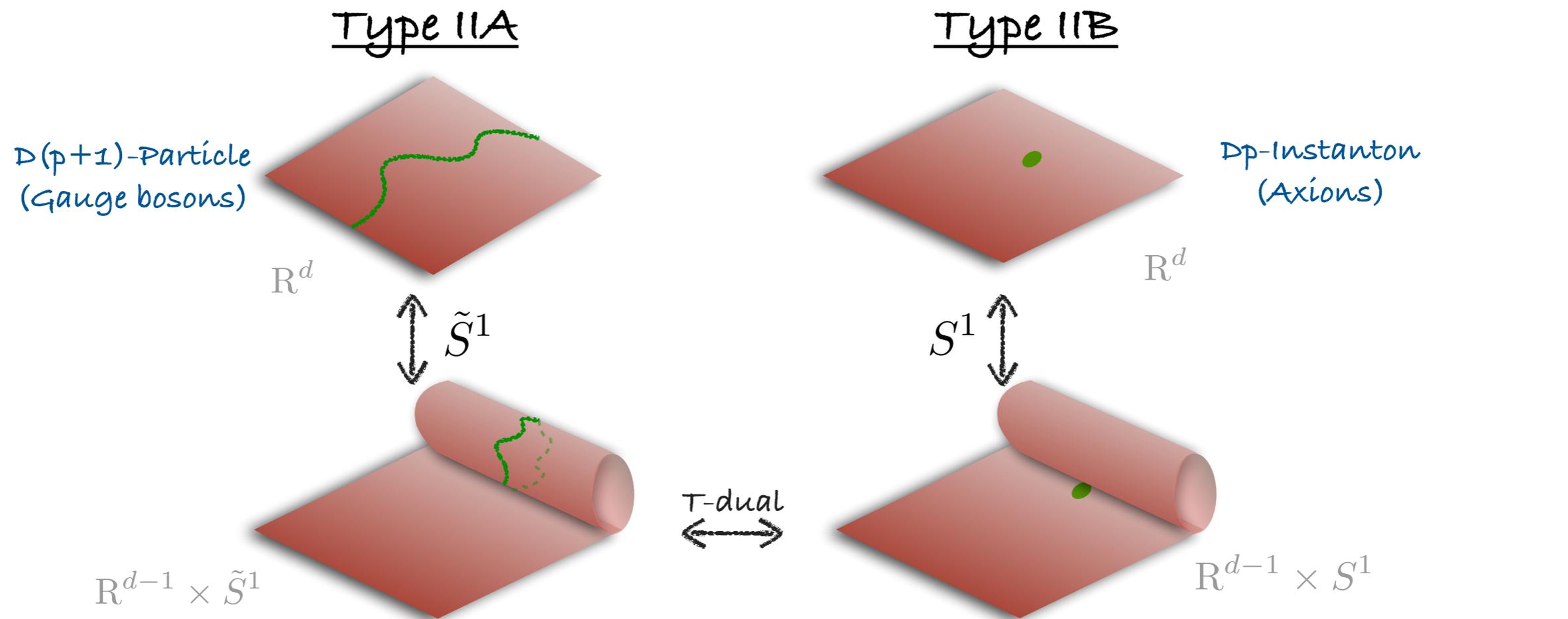
$$a(x) \equiv \int_{\Sigma_2} A$$

The gauge symmetry becomes a **shift symmetry**, that is broken by non-perturbative (instanton) effects.

WGC and Axions

Brown, Cottrell, GS, Soler

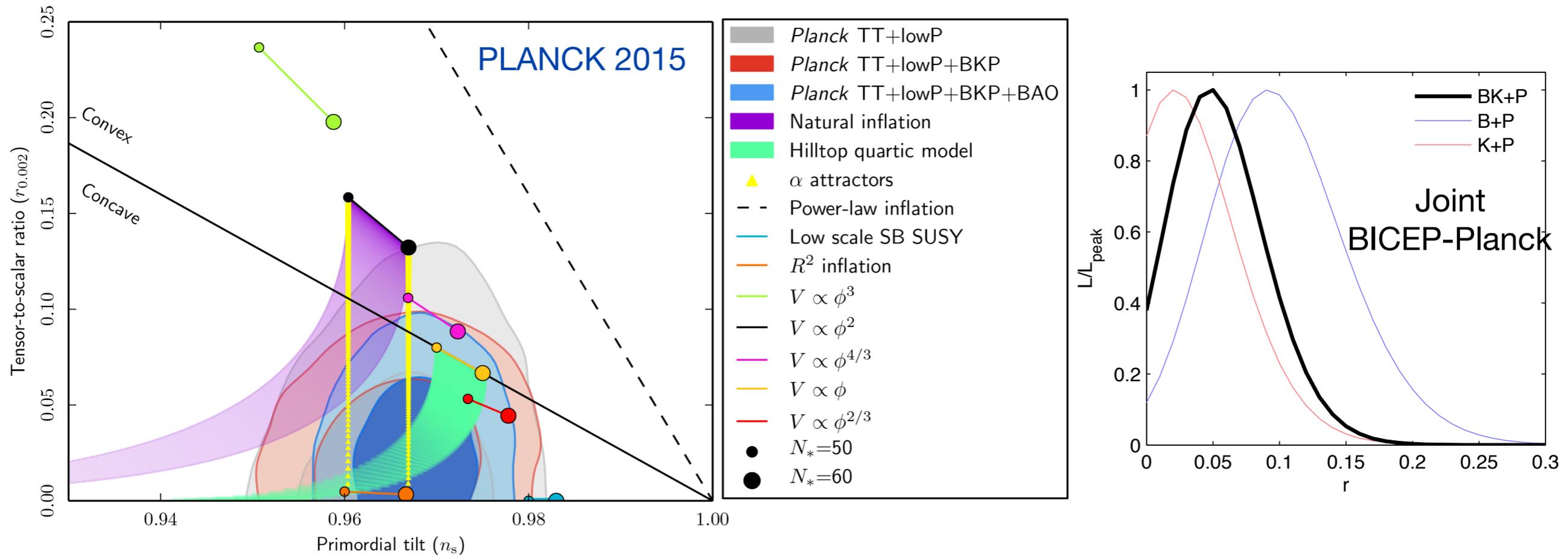
- Formulate the WGC in a duality frame where the axions and instantons turn into gauge fields and particles, e.g.



model-dependent, calculable

- The WGC takes the form $f \cdot S_{\text{instanton}} \leq \mathcal{O}(1) M_P$

Primordial Gravitational Waves



Many experiments including BICEP/KECK, PLANCK, ACT, PolarBeaR, SPT, SPIDER, QUEIT, Clover, EBEX, QUaD, ... can potentially detect primordial B-mode at the sensitivity $r \sim 10^{-2}$.

Further experiments, such as CMB-S4, PIXIE, LiteBIRD, DECIGO, Ali, .. may improve further the sensitivity to eventually reach $r \sim 10^{-3}$.

B-mode and Inflation

If primordial B-mode is detected, natural interpretations:

- ◆ Inflation took place at an energy scale around the GUT scale

$$E_{\text{inf}} \simeq 0.75 \times \left(\frac{r}{0.1}\right)^{1/4} \times 10^{-2} M_{\text{Pl}}$$

- ◆ The inflaton field excursion was super-Planckian

$$\Delta\phi \gtrsim \left(\frac{r}{0.01}\right)^{1/2} M_{\text{Pl}}$$

Lyth '96

- ◆ Great news for string theory due to strong UV sensitivity!

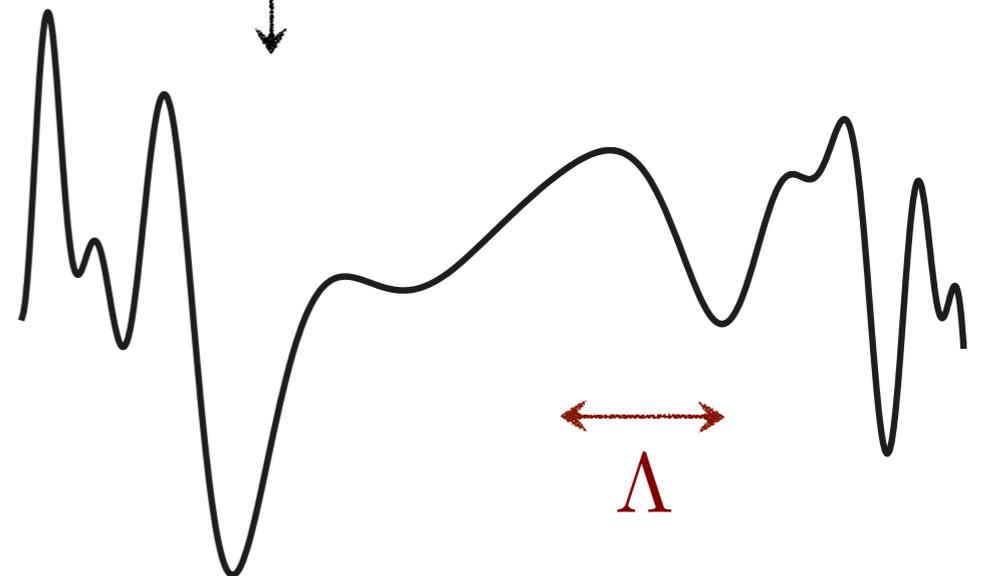
Large field inflation and UV Sensitivity

UV sensitivity of large field inflation:



$$\mathcal{L}_{\text{eff}}[\phi] = \frac{1}{2}(\partial\phi)^2 - \frac{1}{2}m^2\phi^2 \left(1 + \sum_{i=1}^{\infty} c_i \frac{\phi^{2i}}{\Lambda^{2i}} + \dots \right)$$

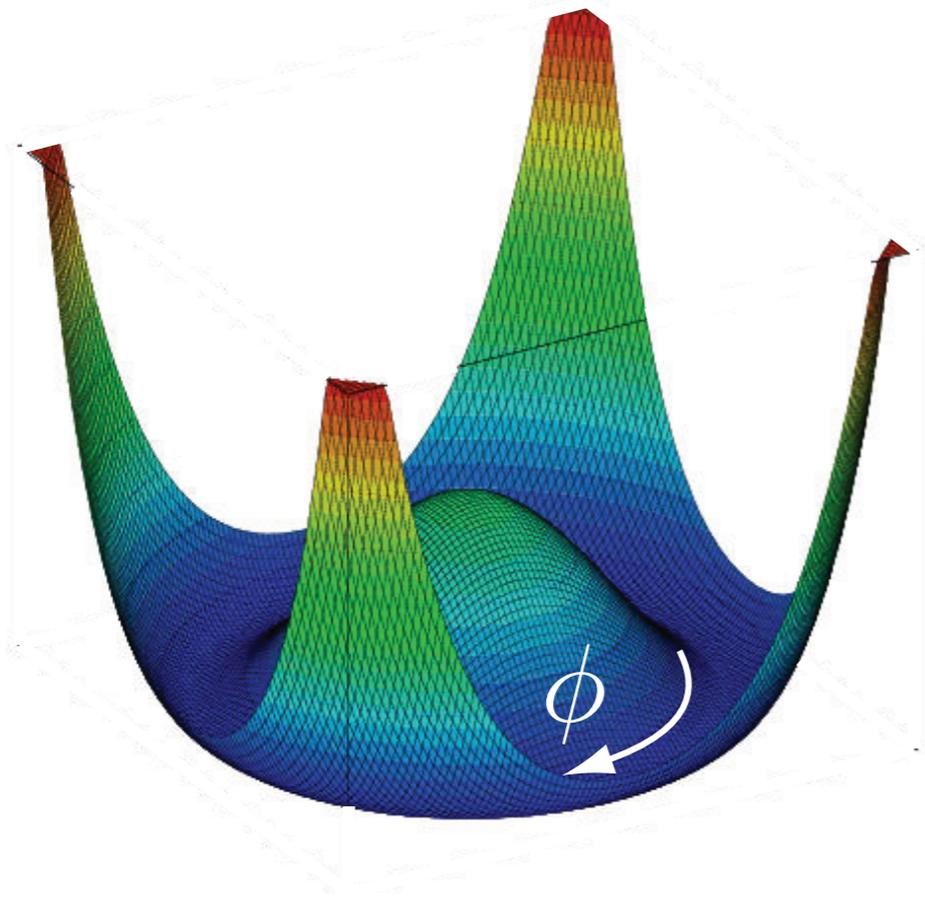
$c_i \sim \mathcal{O}(1)$



Axions & Large Field Inflation

Natural Inflation [Freese, Frieman, Olinto]

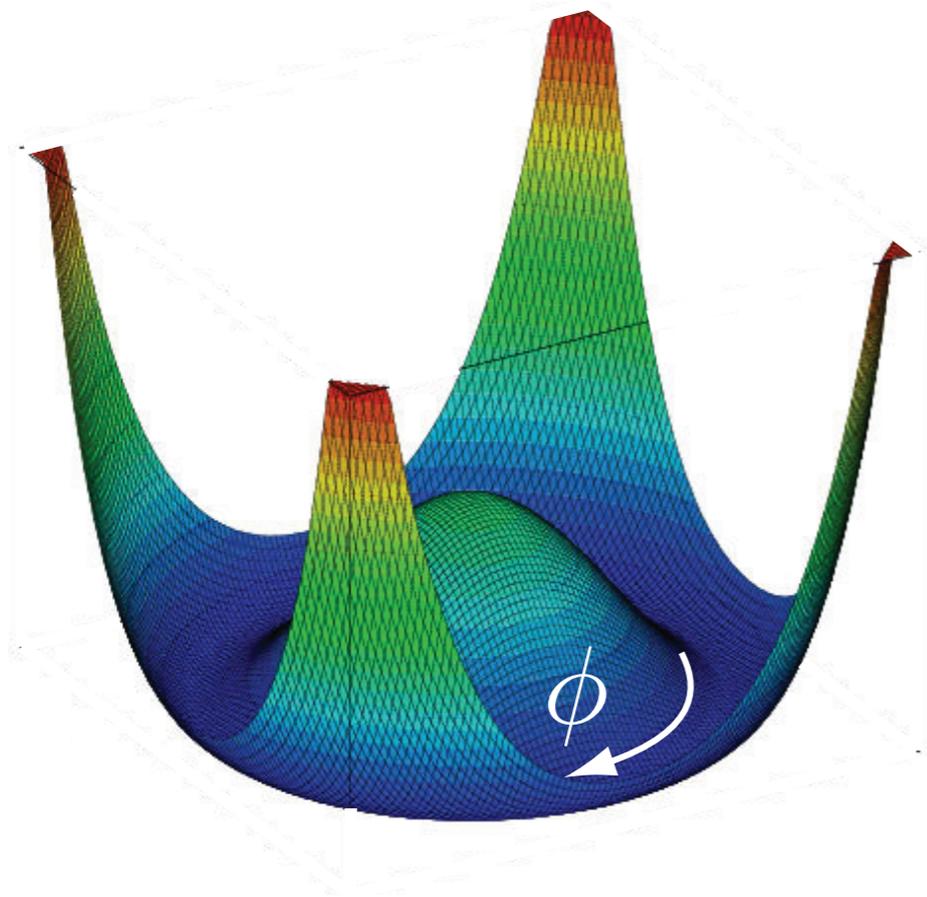
Pseudo-Nambu-Goldstone bosons are natural inflaton candidates.



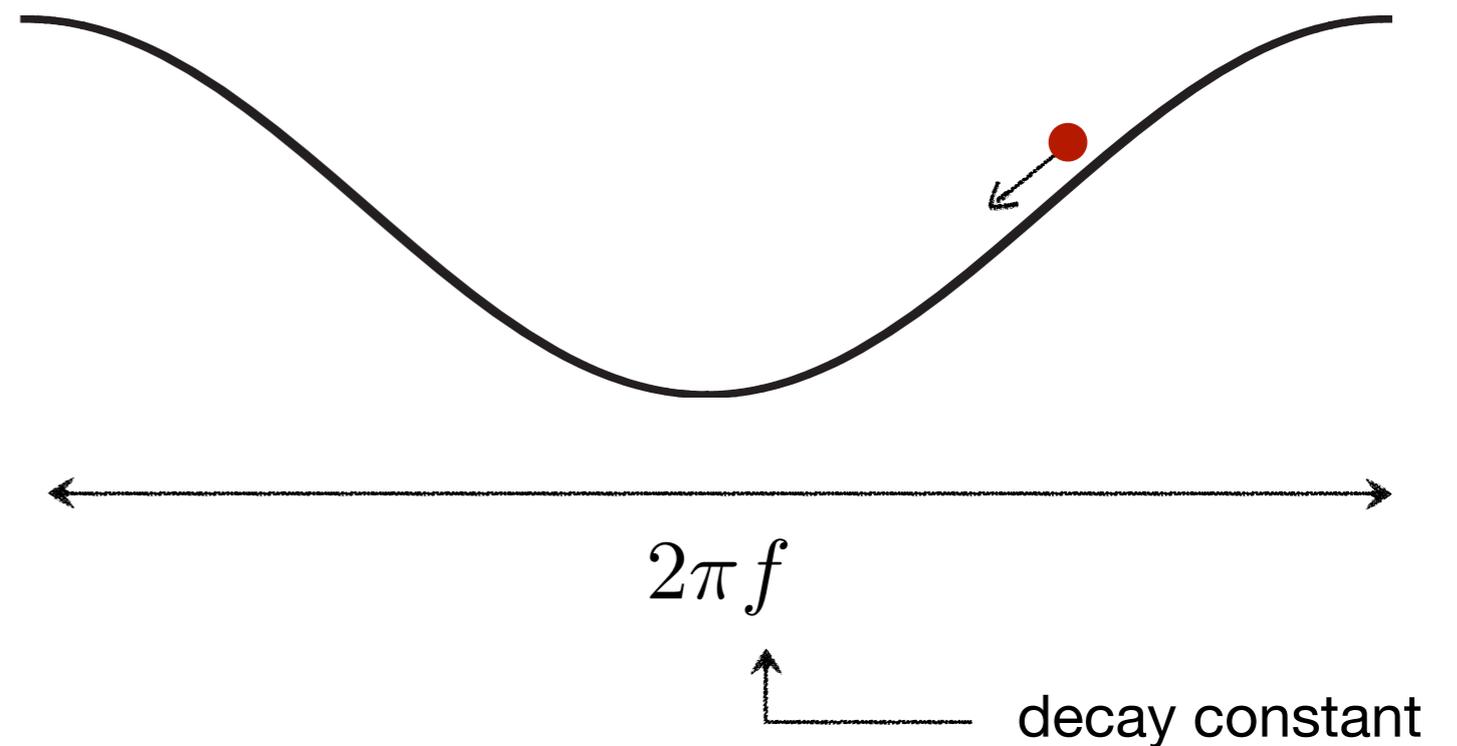
Axions & Large Field Inflation

Natural Inflation [Freese, Frieman, Olinto]

Pseudo-Nambu-Goldstone bosons are natural inflaton candidates.



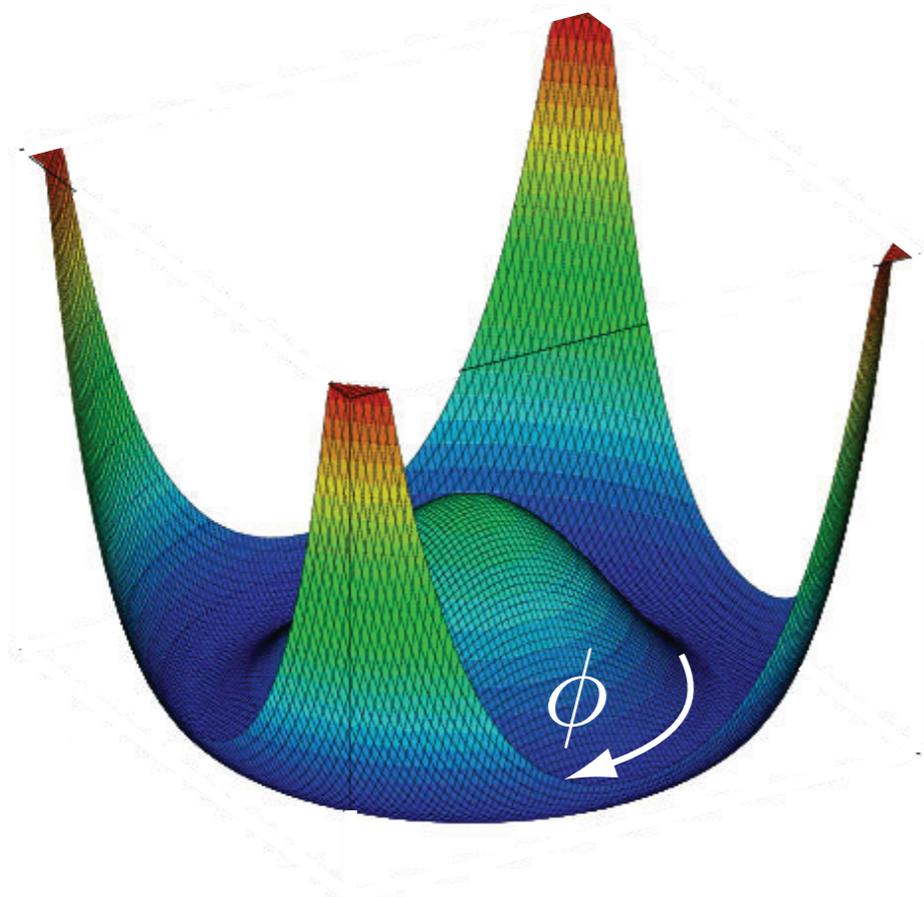
They satisfy a shift symmetry that is only broken by non-perturbative effects:



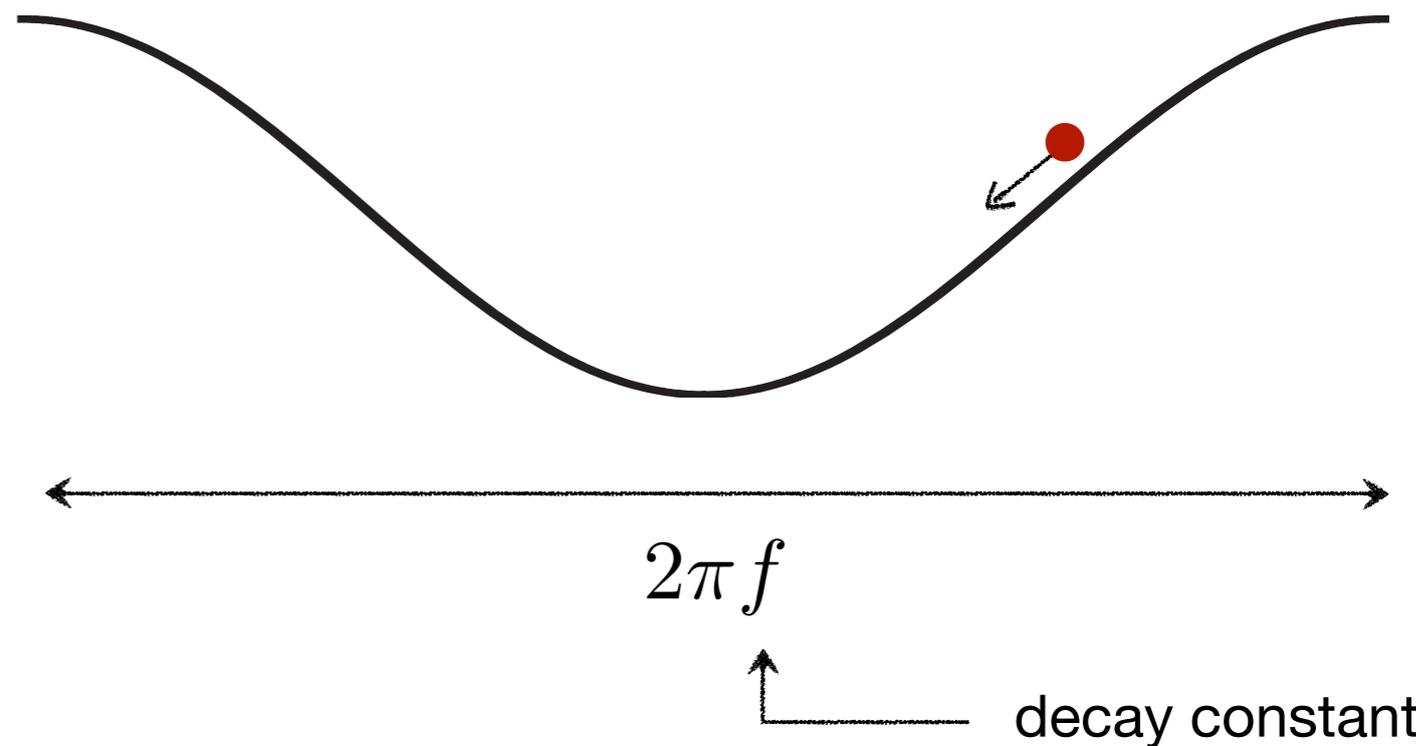
Axions & Large Field Inflation

Natural Inflation [Freese, Frieman, Olinto]

Pseudo-Nambu-Goldstone bosons are natural inflaton candidates.



They satisfy a shift symmetry that is only broken by non-perturbative effects:



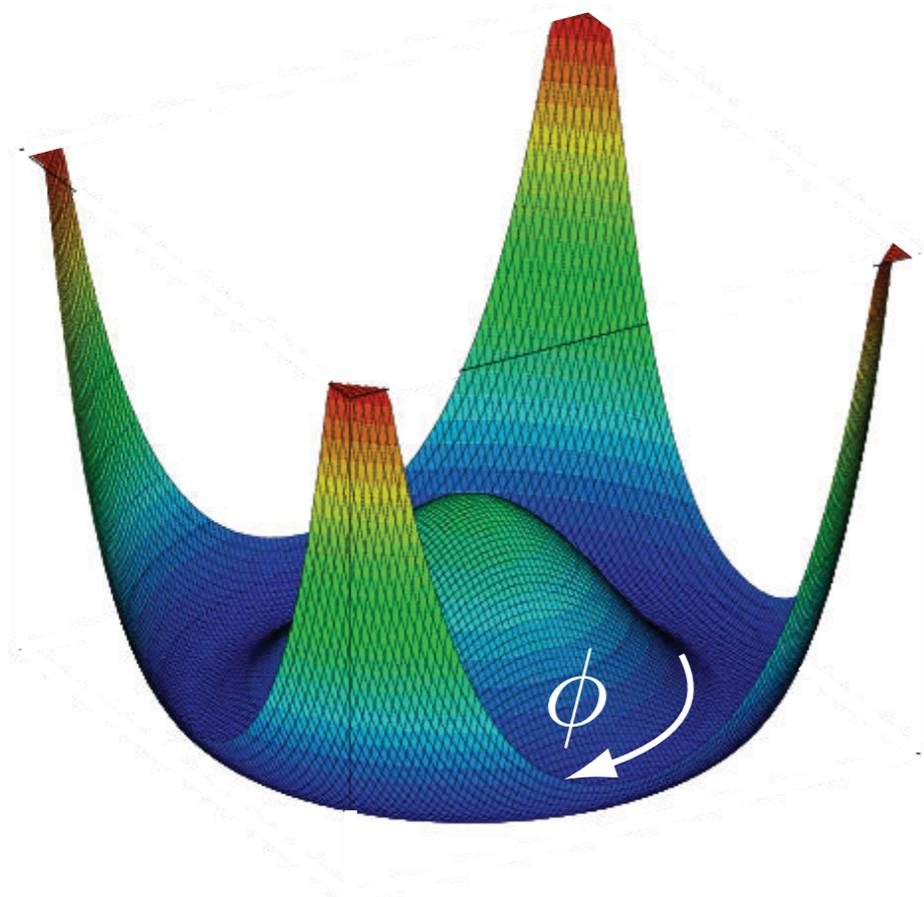
Slow roll: $f > M_P$

$$V(\phi) = 1 - \Lambda^{(1)} \cos\left(\frac{\phi}{f}\right) + \sum_{k>1} \Lambda^{(k)} \left[1 - \cos\left(\frac{k\phi}{f}\right) \right] \quad \text{if} \quad \frac{\Lambda^{(n+1)}}{\Lambda^{(n)}} \sim e^{-S_{\text{inst}}} \ll 1$$

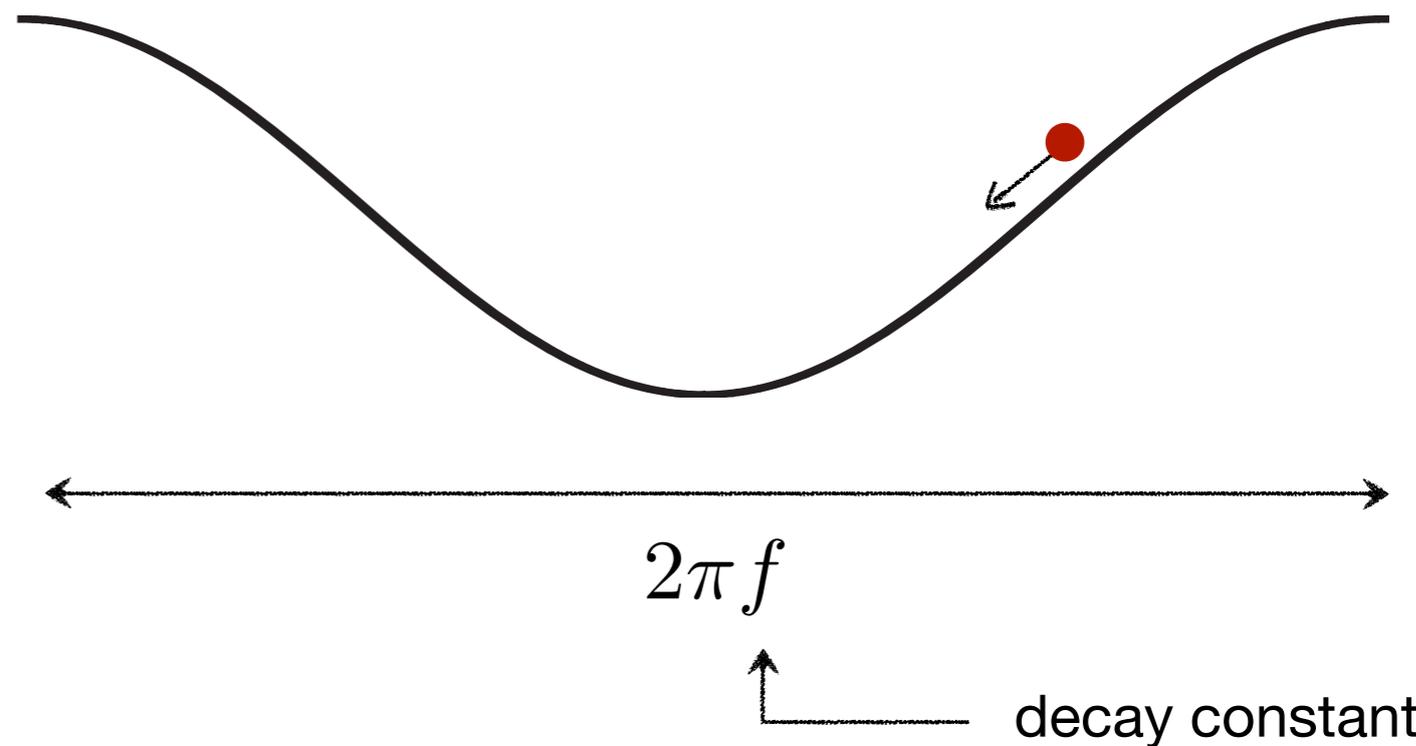
Axions & Large Field Inflation

Natural Inflation [Freese, Frieman, Olinto]

Pseudo-Nambu-Goldstone bosons are natural inflaton candidates.



They satisfy a shift symmetry that is only broken by non-perturbative effects:



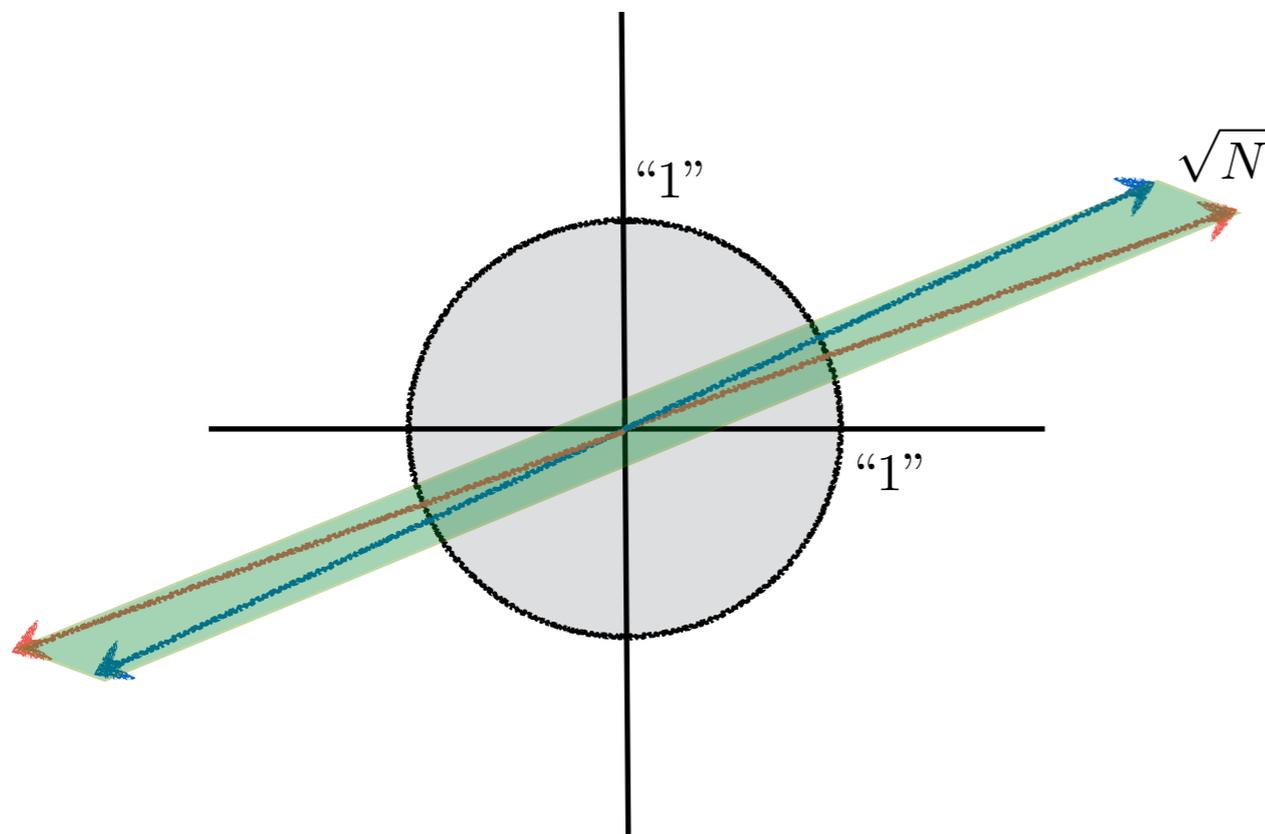
Slow roll: $f > M_P$

$$V(\phi) = 1 - \Lambda^{(1)} \cos\left(\frac{\phi}{f}\right) + \sum_{k>1} \Lambda^{(k)} \left[1 - \cos\left(\frac{k\phi}{f}\right) \right] \quad \text{if} \quad \frac{\Lambda^{(n+1)}}{\Lambda^{(n)}} \sim e^{-S_{\text{inst}}} \ll 1$$

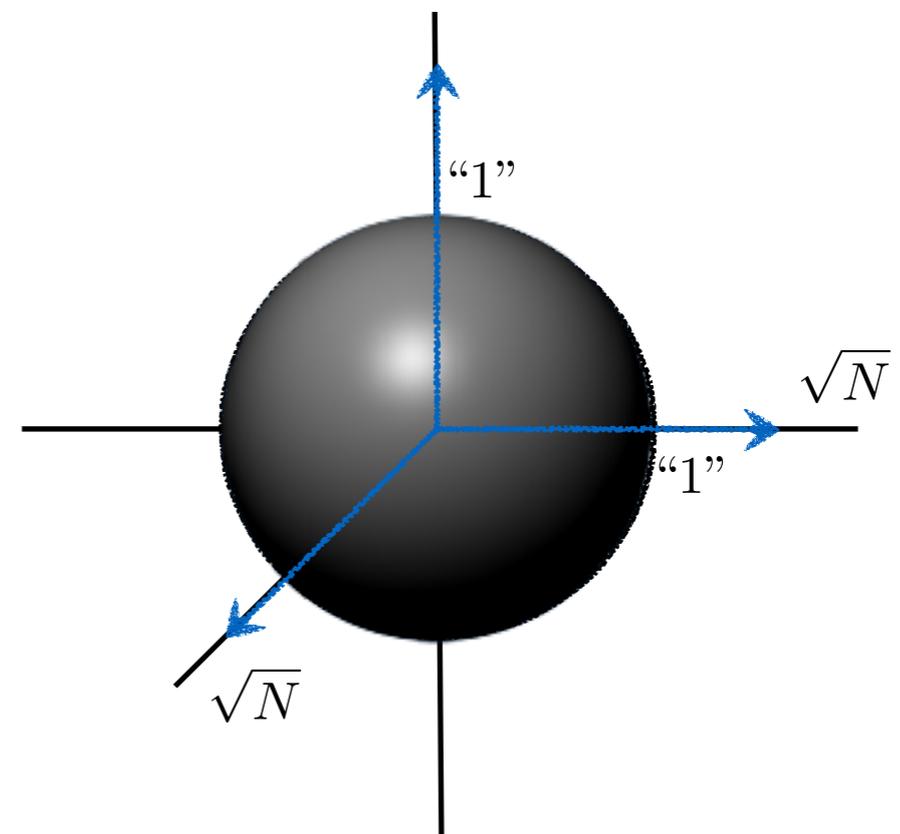
The WGC implies that these conditions cannot be *simultaneously* satisfied.

WGC and Multi-Axion Inflation

- Thorough searches for transplanckian axions in the string landscape have not been successful. Banks et al. '03 ...
- Models with multiple axions (e.g., N-flation, KNP-alignment) have been proposed but they do not satisfy the convex hull condition [Brown, Cottrell, GS, Soler];[Cheung, Remmen]



Alignment [Kim, Nilles, Peloso, '04]



N-flation [Dimopoulos et al, '05]

WGC for the QCD Axion

- **The QCD instanton action**

$$S_{\text{QCD}} = 4 \ln M_*/\Lambda_{\text{QCD}} \approx 160, \quad \text{where } M_* = \text{UV scale, e.g., } M_{\text{GUT}}$$

- **The WGC implies a bound:** $f_{\text{QCD}} \lesssim 10^{16} \text{ GeV}$

- While weaker than the commonly quoted **cosmological bound:**

$$f_{\text{QCD}} < 10^{12} \text{ GeV}$$

scenarios that allow larger f_{QCD} have been proposed, e.g. [Wilczek, '04]

- QCD axion with decay constants above the GUT scale can be tested:
 - **laboratory searches** e.g., ABRACADABRA
 - **gravitational wave observatory** e.g., LIGO (via black hole super-radiance, [Arvanitaki, Dimopoulos, Dubovsky, Kaloper, March-Russell, '09])

WGC and Particle Physics

The Standard Model in the Deep IR

- The deep IR of the SM, below the electron mass scale, is simple:
 - **Bosonic dof:** photon (2) and graviton (2)
 - **Fermionic dof:** ν 's (6 or 12 for **Majorana/Dirac** ν 's)

- The **mass scale of neutrinos:**

$$m_\nu \simeq 10^{-1} - 10^{-2} eV$$

- The only other known IR scale is the **cosmological constant:**

$$\Lambda \simeq 3.25 \times 10^{-11} eV^4 = (0.24 \times 10^{-2} eV)^4$$

- This coincidence (?) has been a source of inspiration/speculations:

$$\Lambda \simeq m_\nu^4$$

WGC for Branes

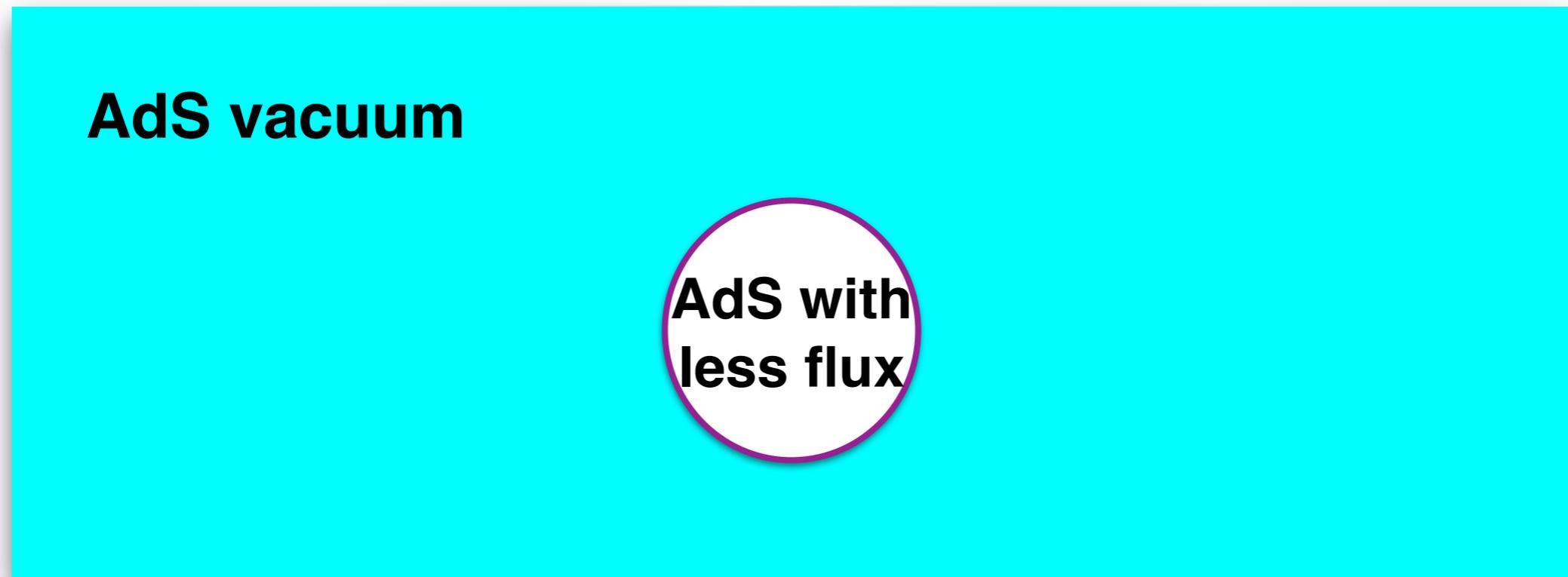
- We have seen the applications of the WGC to particles (and instantons). Analogously, the WGC for branes is:

$$“T_p \leq Q_p”$$

- A stronger form [Ooguri, Vafa, '16]: **this bound is saturated only for a BPS state in a SUSY theory.**
- A **corollary** of this strong form: **non-SUSY AdS vacua supported by fluxes are unstable.**
- In AdS space, a brane with $T < Q$ leads to an instability (AdS fragmentation) [Maldacena, Michelson, Strominger, '99].
- This brane gets nucleated and expands. It reaches the boundary of AdS within a finite time and dilute the flux.

AdS Instability

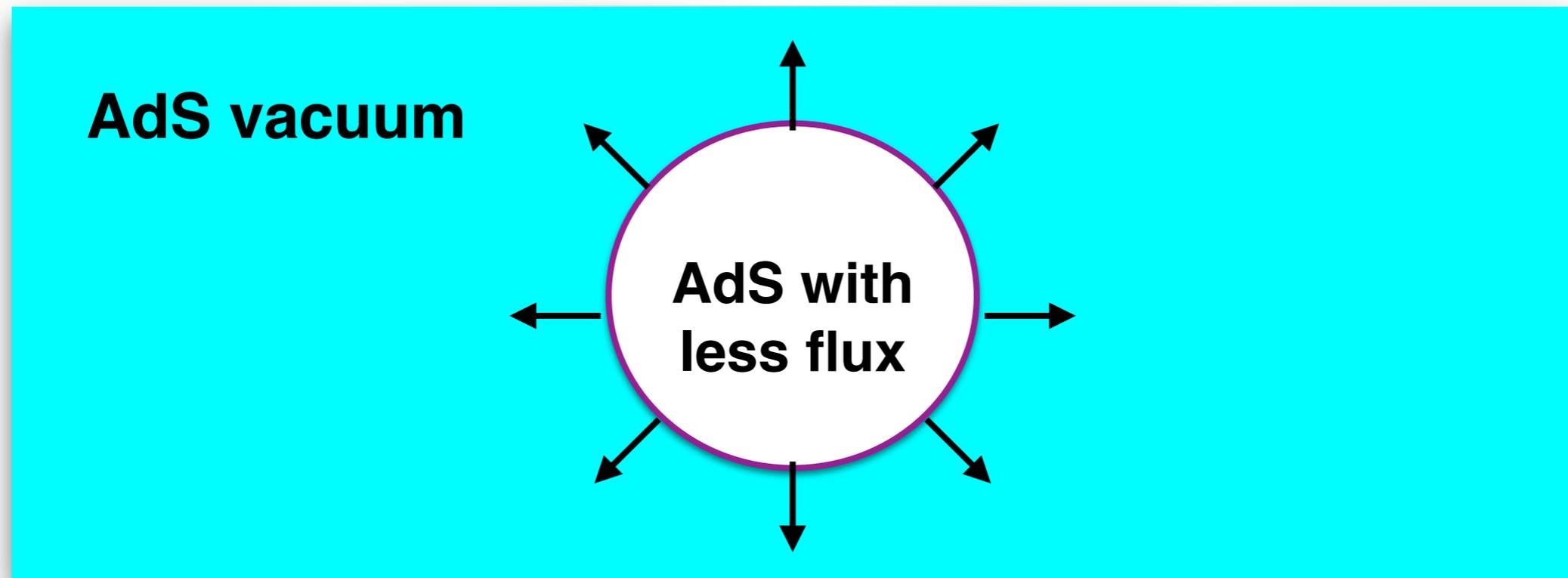
- Instability if there exists a $T < Q$ brane (bubble wall) in AdS:



- A stronger form of the Ooguri-Vafa conjecture:
 - “**all non-SUSY AdS** (in theories whose low energy description is Einstein gravity coupled to a finite # of fields) **are unstable**”
- **How do we test this conjecture?**

AdS Instability

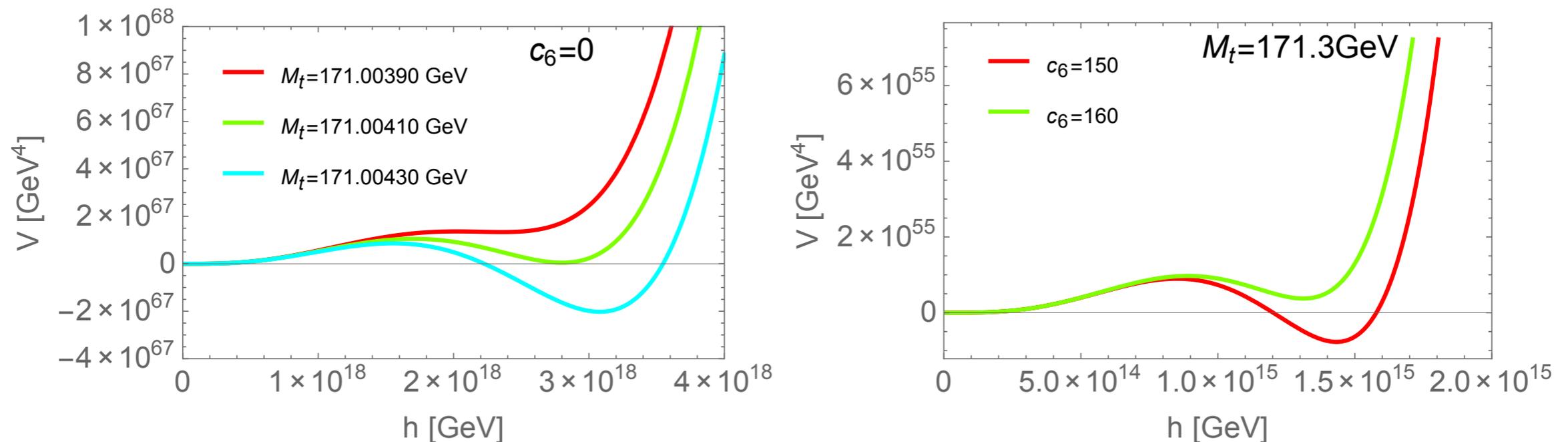
- Instability if there exists a $T < Q$ brane (bubble wall) in AdS:



- A stronger form of the Ooguri-Vafa conjecture:
 - “**all non-SUSY AdS** (in theories whose low energy description is Einstein gravity coupled to a finite # of fields) **are unstable**”
- **How do we test this conjecture?**

The Higgs Potential

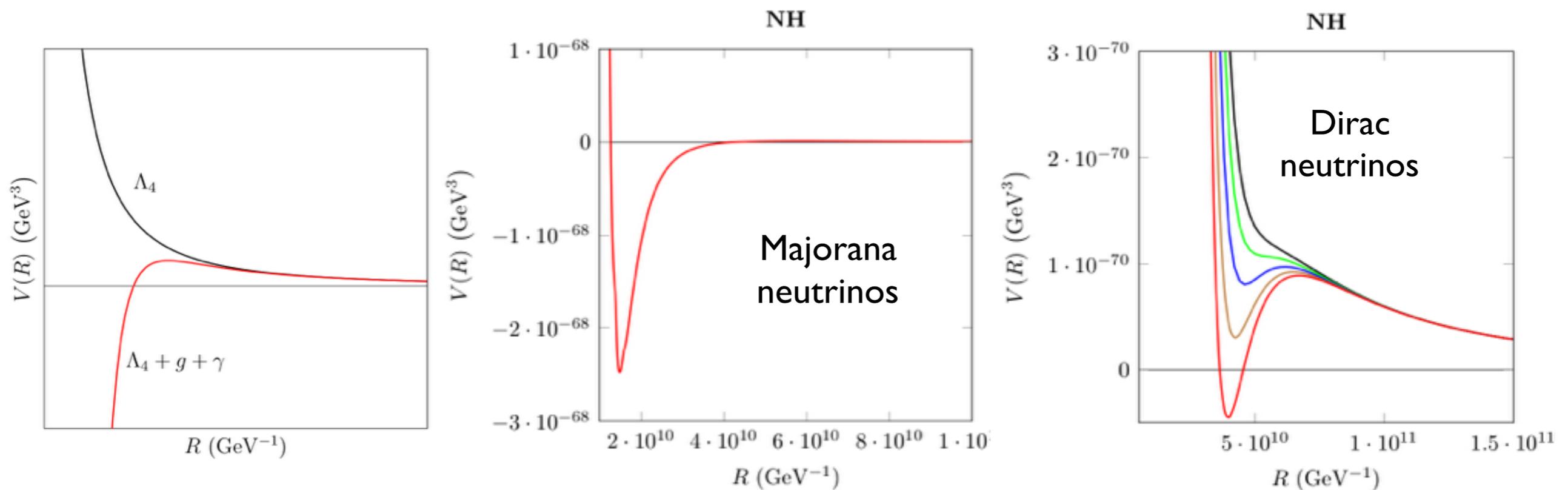
- After the Higgs discovery, we know that there is an additional Higgs vacuum at high scale, other than the EW vacuum:



- This high scale vacuum can be AdS₄, M₄, or dS₄ depending on the **top quark mass** and the **higher-dimensional operators**.
- Applying this conjecture to the SM landscape, we can constrain the **top mass**, **Higgs potential**, and **BSM physics**. [Hamada, GS].

Standard Model Landscape

- Upon compactification, the SM gives rise to a rich landscape of 3d vacua [Arkani-Hamed, Dubovsky, Nicolis, Villadoro].
- A competition between Λ_4 and **Casimir energies** (depends on mass, spin, b.c., and #dof; negligible unless $mL \ll 1$):



- The more massive the neutrinos, the deeper the AdS minimum. Barring the potential instability of the AdS vacuum [Hamada, GS], the WGC puts a bound on the **neutrino mass and type**.

Summary of Results

[Hamada, GS]

- Compactify the SM on S^1 and T^2 , starting from both the electroweak vacuum and the high scale vacuum, with general b.c. and WL.

	model	AdS	flat	dS
S^1	$U(1)$, neutral	$\Lambda_4 \lesssim 10^{-2.8} M_e^4$	$\Lambda_4 \simeq 10^{-2.8} M_e^4$	$10^{-2.8} M_e^4 \lesssim \Lambda_4 \lesssim 10^{-2.6} M_e^4$
	$U(1)$, charged	–	–	–
	SM, ν_M	always	–	–
	SM, ν_D , NH	$8.4 \text{ meV} \lesssim m_{\nu, \text{lightest}}$	$m_{\nu, \text{lightest}} \simeq 8.4 \text{ meV}$	$7.3 \text{ meV} \lesssim m_{\nu, \text{lightest}} \lesssim 8.4 \text{ meV}$
	SM, ν_D , IH	$3.1 \text{ meV} \lesssim m_{\nu, \text{lightest}}$	$m_{\nu, \text{lightest}} \simeq 3.1 \text{ meV}$	$2.5 \text{ meV} \lesssim m_{\nu, \text{lightest}} \lesssim 3.1 \text{ meV}$
	SM, ν_M , high scale	–	–	–
	SM, ν_D , high scale	$\Lambda_4 \ll (\text{neutrino mass})^4$	–	–
	axion	$\Lambda_4 < 0$	–	–
T^2	$U(1)$, neutral	$\Lambda_4 \lesssim 10^{-2.1} M_e^4$	$\Lambda_4 \simeq 10^{-2.1} M_e^4$	$10^{-2.5} M_e^4 \lesssim \Lambda_4 \lesssim 10^{-2.1} M_e^4$
	$U(1)$, charged	–	–	–
	SM, ν_M	always	–	–
	SM, ν_D , NH	$4.5 \text{ meV} \lesssim m_{\nu, \text{lightest}}$	$m_{\nu, \text{lightest}} \simeq 4.5 \text{ meV}$	$4.5 \text{ meV} \lesssim m_{\nu, \text{lightest}} \lesssim 6.5 \text{ meV}$
	SM, ν_D , IH	$1.1 \text{ meV} \lesssim m_{\nu, \text{lightest}}$	$m_{\nu, \text{lightest}} \simeq 1.1 \text{ meV}$	$1.1 \text{ meV} \lesssim m_{\nu, \text{lightest}} \lesssim 1.55 \text{ meV}$
	axion	$\Lambda_4 < 0$	–	–

- Can avoid AdS vacua if neutrinos are Dirac w/ the lightest neutrino mass $\lesssim \mathcal{O}(1-10)$ meV. (also [Ibanez, Martin-Lozano, Valenzuela]).

Evidences for the WGC

Evidences for the Weak Gravity Conjecture

Several lines of argument have been taken (so far):

- Holography [Nakayama, Nomura, '15];[Harlow, '15];[Benjamin, Dyer, Fitzpatrick, Kachru, '16];[Montero, GS, Soler, '16]
- Cosmic Censorship [Horowitz, Santos, Way, '16];[Cottrell, GS, Soler, '16];[Crisford, Horowitz, Santos, '17]
- Entropy considerations [Cottrell, GS, Soler, '16] (note however unjustified claims in [Fisher, Mogni, '17]; [Cheung, Liu, Remmen, '18]).
- IR Consistencies (unitarity & causality) [Cheung, Remmen, '14] [Andriolo, Junghans, Noumi, GS, '18].

Evidences for stronger versions of the WGC:

- Consistencies with T-duality [Brown, Cottrell, GS, Soler, '15] and dimensional reduction [Heidenreich, Reece, Rudelius '15].
- Modular invariance + charge quantization suggest a **sub-lattice WGC** [Montero, GS, Soler, '16] (see also [Heidenreich, Reece, Rudelius '16])

WGC and Blackhole Entropy

Entropy Corrections

- We computed loop corrections to the entropy of extremal blackholes using Sen's entropy functional formalism **[Cottrell, GS, Soler, '16]**.
- While corrections from neutral particles have been well studied (loops of massless particles give $\log(A)$ corrections to BH entropy), we found new features when charged particles are integrated out.
- Fermion spectral density in $AdS_2 \times S_2$ is divergent for:

$$\text{Energy} \sim \frac{\lambda}{a} = \sqrt{2}qM_P \quad \text{Magnetic WGC!}$$

- The entropy corrections formulae used in **[Fisher, Mogni, '17]** cannot be applied to macroscopic black holes, nor away from extremality, which is where conflicts with the WGC were argued to arise.
- **[Cheung, Liu, Remmen, '18]** made a connection between the WGC and the positivity of entropy corrections. It is not known, however, if the latter follows from some fundamental consistency conditions.

WGC and Positivity Bounds

Einstein-Maxwell + massive charged particles



integrate out matters

IR effective theory of photon & graviton

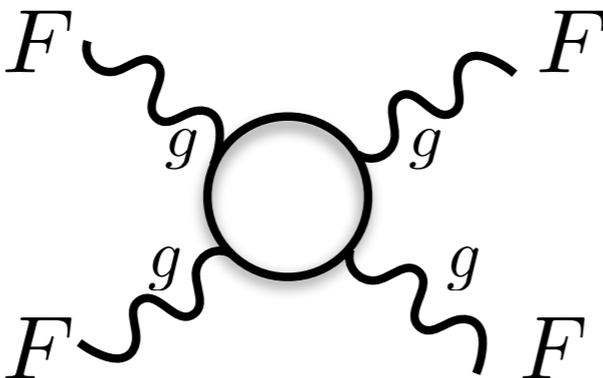
Positivity of EFT coefficients follow from unitary, causality, and analyticity of scattering amplitudes.

Q. What does the positivity of this EFT imply?

1-loop effective action for photon & graviton

$$\mathcal{L}_{\text{eff}} = \frac{M_{\text{Pl}}^2}{2} R - \frac{1}{4} F_{\mu\nu}^2 + \alpha_1 (F_{\mu\nu} F^{\mu\nu})^2 + \alpha_2 (F_{\mu\nu} \tilde{F}^{\mu\nu})^2 + \alpha_3 F_{\mu\nu} F_{\rho\sigma} W^{\mu\nu\rho\sigma} + \dots$$

- positivity implies $\alpha_1 + \alpha_2 \geq 0$
- α_i depends on mass and charge of particles integrated out

$$\alpha_i = \frac{\text{Diagram} + \mathcal{O}(g^2) + \mathcal{O}(g^0)}{\text{gravitational effects}}$$


- Cheung-Remmen found positivity implies $z^4 - z^2 + \gamma \geq 0$

$$\text{⌘ } z = \frac{qg}{m/M_{\text{Pl}}}, \quad \gamma \text{ is a UV sensitive } \mathcal{O}(z^0) \text{ coefficient}$$

(free parameter in the EFT framework)

Positivity of photon-graviton EFT implies $z^4 - z^2 + \gamma \geq 0$

→ at least one of the following two should be satisfied

1) WGC type lower bound on charge-to-mass ratio

in particular when $\gamma = 0$, WGC $z^2 \geq 1$ is reproduced!

2) not so small value of UV sensitive parameter $\gamma > 0$

In [Andriolo, Junghans, Noumi, GS], we discussed

- multiple U(1)'s
- implications for KK reduction

and found **qualitatively new features**.

Multiple U(1)'s

for example, let us consider $U(1)_1 \times U(1)_2$

a new ingredient is positivity of $\gamma_1 + \gamma_2 \rightarrow \gamma_1 + \gamma_2$

Im \rightleftarrows  $\rightleftarrows \geq 0$ implies $z_1^2 z_2^2 - z_1^2 - z_2^2 \geq 0$

- $z_i = q_i/m$ is the charge-to-mass ratio for each U(1)

- we set $\mathcal{O}(z^0) = 0$ for illustration (same as $\gamma = 0$ before)

the punchline here:

positivity bound cannot be satisfied unless $z_1^2 z_2^2 \neq 0$

\rightarrow requires existence of a bifundamental particle!

Implications for KK reduction

S^1 compactify $d+1$ dim Einstein-Maxwell with single $U(1)$
into d dim Einstein-Maxwell with $U(1) \times U(1)_{\text{KK}}$

$d+1$ dim charged particle (q, m)

→ KK tower with the charged-to-mass ratios

$$(z, z_{\text{KK}}) = \left(\frac{q}{\sqrt{m^2 + n^2 m_{\text{KK}}^2}}, \frac{n}{\sqrt{(m/m_{\text{KK}})^2 + n^2}} \right)$$

in the small radius limit $m_{\text{KK}} \rightarrow \infty$,

the lowest mode ($n = 0$): $(z, z_{\text{KK}}) = (q/m, 0)$

KK modes ($n \neq 0$): $(z, z_{\text{KK}}) \simeq (0, 1)$

✂ no bifundamentals → ~~positivity bound~~ generically

d+1 dim

charged particles

labeled by $\ell = 1, 2, \dots$

$$(q, m) = (\ell q_*, \ell m_*)$$

$$\text{s.t. } z_* = \frac{q_*}{m_*} = \mathcal{O}(1)$$

$U(1)$

ℓ



d+1 dim

charged particles

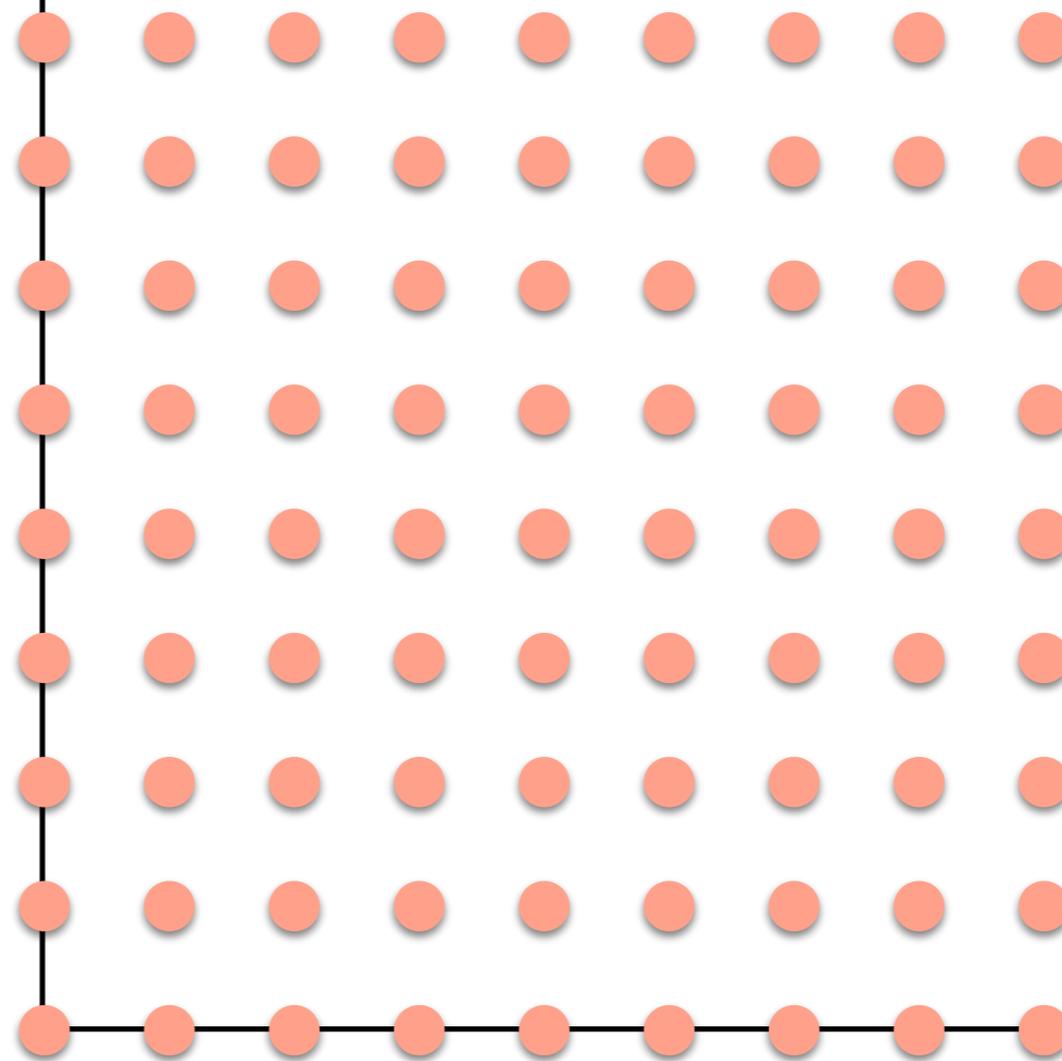
labeled by $\ell = 1, 2, \dots$

$$(q, m) = (\ell q_*, \ell m_*)$$

$$\text{s.t. } z_* = \frac{q_*}{m_*} = \mathcal{O}(1)$$

$U(1)$

ℓ



$n U(1)_{\text{KK}}$

d dim charged particles

$$(z, z_{\text{KK}}) = \left(\frac{\ell z_*}{\sqrt{\ell^2 (m_*/m_{\text{KK}})^2 + n^2}}, \frac{n}{\sqrt{\ell^2 (m_*/m_{\text{KK}})^2 + n^2}} \right)$$

d+1 dim

charged particles

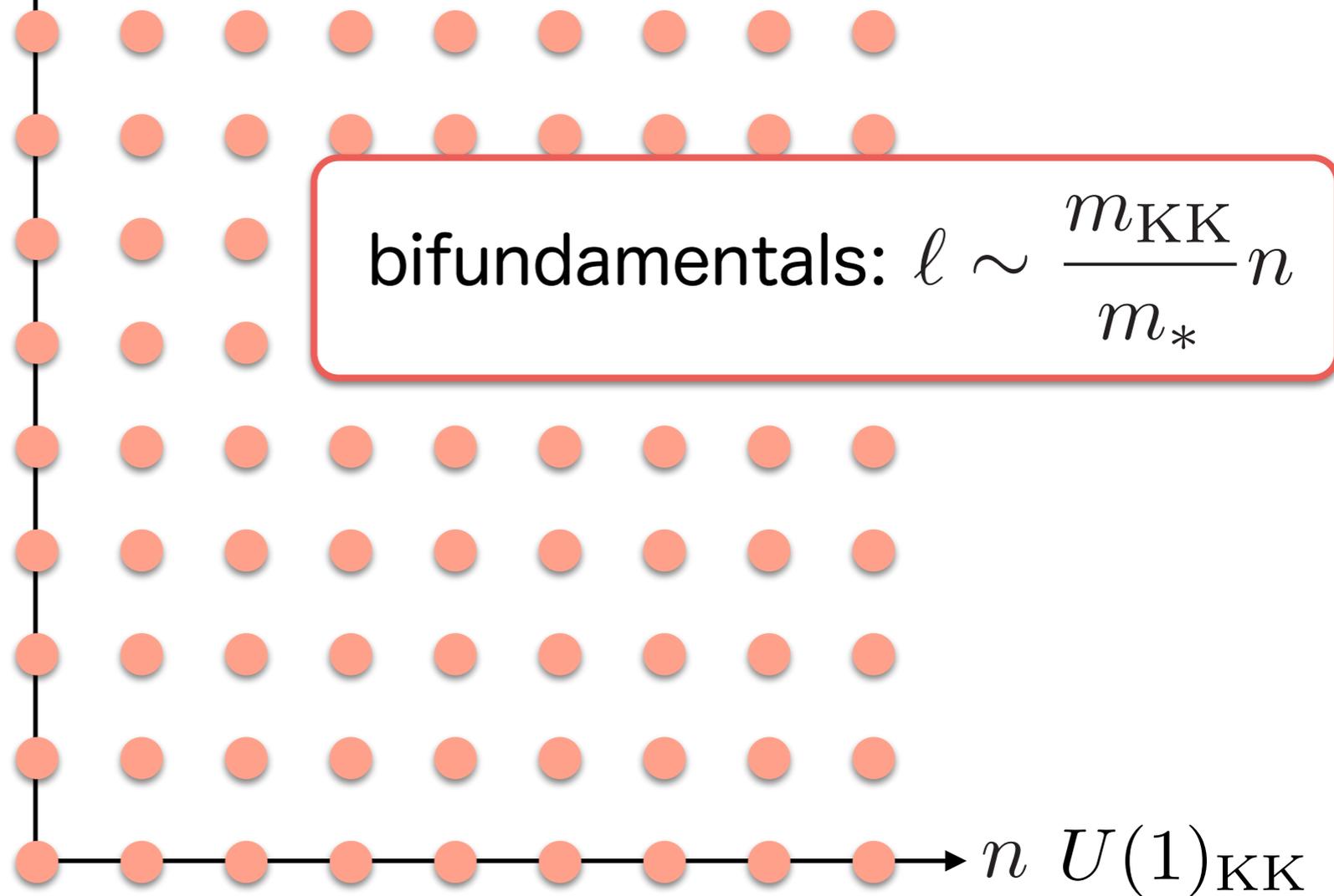
labeled by $\ell = 1, 2, \dots$

$$(q, m) = (\ell q_*, \ell m_*)$$

$$\text{s.t. } z_* = \frac{q_*}{m_*} = \mathcal{O}(1)$$

$U(1)$

ℓ



d dim charged particles

$$(z, z_{\text{KK}}) = \left(\frac{\ell z_*}{\sqrt{\ell^2 (m_*/m_{\text{KK}})^2 + n^2}}, \frac{n}{\sqrt{\ell^2 (m_*/m_{\text{KK}})^2 + n^2}} \right)$$

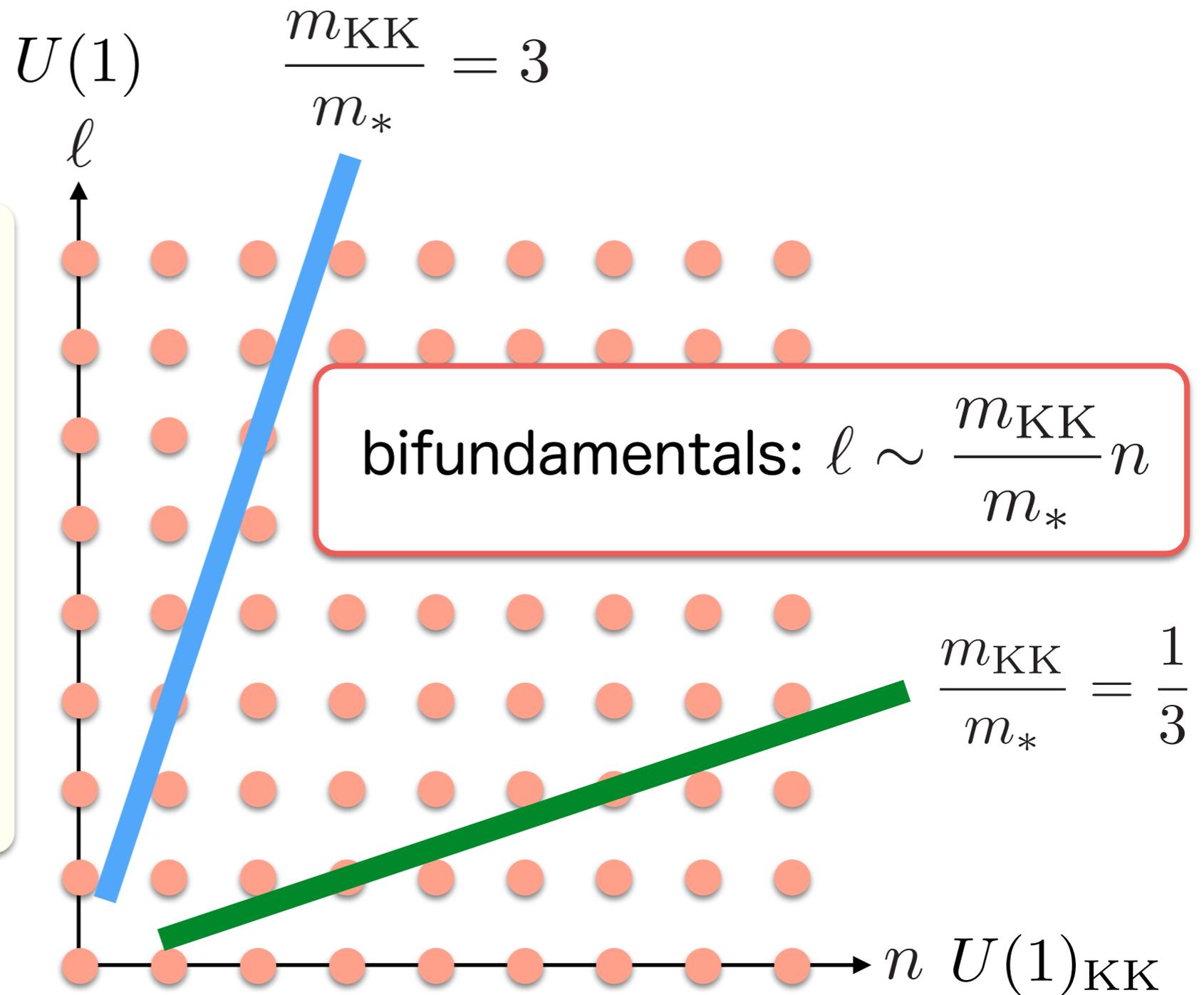
d+1 dim

charged particles

labeled by $\ell = 1, 2, \dots$

$$(q, m) = (\ell q_*, \ell m_*)$$

$$\text{s.t. } z_* = \frac{q_*}{m_*} = \mathcal{O}(1)$$



d dim charged particles

$$(z, z_{\text{KK}}) = \left(\frac{\ell z_*}{\sqrt{\ell^2 (m_*/m_{\text{KK}})^2 + n^2}}, \frac{n}{\sqrt{\ell^2 (m_*/m_{\text{KK}})^2 + n^2}} \right)$$

Tower WGC

[Andriolo, Junghans, Noumi, GS]

Consistency with KK reduction seems to imply a tower of $d+1$ dim $U(1)$ charged particles

→ Tower Weak Gravity Conjecture!

※ a similar “(sub)lattice WGC” was proposed based on modular invariance or holography

[Montero, GS, Soler, '16];[Heidenreich, Reece, Rudelius, '16]

Conclusions

Conclusions

- Swampland conjectures have a variety of interesting applications in cosmology and particle physics.
- The WGC when applied to ALPs constrains **inflationary B-modes**; when applied to the **QCD axion** implies $f_{\text{QCD}} \lesssim 10^{16}$ GeV which can be falsified by **laboratory axion searches** or **GW detectors**.
- The WGC offers interesting perspectives on how **Λ and the neutrino masses are linked**.
- Further evidences for the WGC based on **entropy considerations** and **IR consistencies**.

Conclusions

Thank
You

- Swampland conjectures have a variety of interesting applications in cosmology and particle physics.
- The WGC when applied to ALPs constrains **inflationary B-modes**; when applied to the **QCD axion** implies $f_{\text{QCD}} \lesssim 10^{16}$ GeV which can be falsified by **laboratory axion searches** or **GW detectors**.
- The WGC offers interesting perspectives on how **Λ and the neutrino masses are linked**.
- Further evidences for the WGC based on **entropy considerations** and **IR consistencies**.