

Collider Physics

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Many excellent references

Books

Modern Particle Physics: Mark Thomson

Introduction to Elementary Particles: Griffiths

Quantum Field Theory and the Standard Model : Schwartz

QCD and Collider Physics : Ellis, Stirling and Webber

Online

CMS and ATLAS physics webpages

COLLIDER PHENOMENOLOGY : Tao Han(hep-ph:0508097)

Particle data Group <https://pdg.lbl.gov/2021/reviews/rpp2020-rev-passage-particles-matter.pdf>

Particle data Group <https://pdg.lbl.gov/2023/AtomicNuclearProperties/adndt.pdf>

CMS and ATLAS physics webpages

CMS L1 TDR 2020

Towards Jetography : G Salam

Pileup Mitigation by G. Soyez 1801.09721

Tracking and Calorimetry

Tracking

A charged particle bends in the magnetic field=> momentum can be measured from the bending

Need to measure the position of the charged particle at different points => reconstruct the track

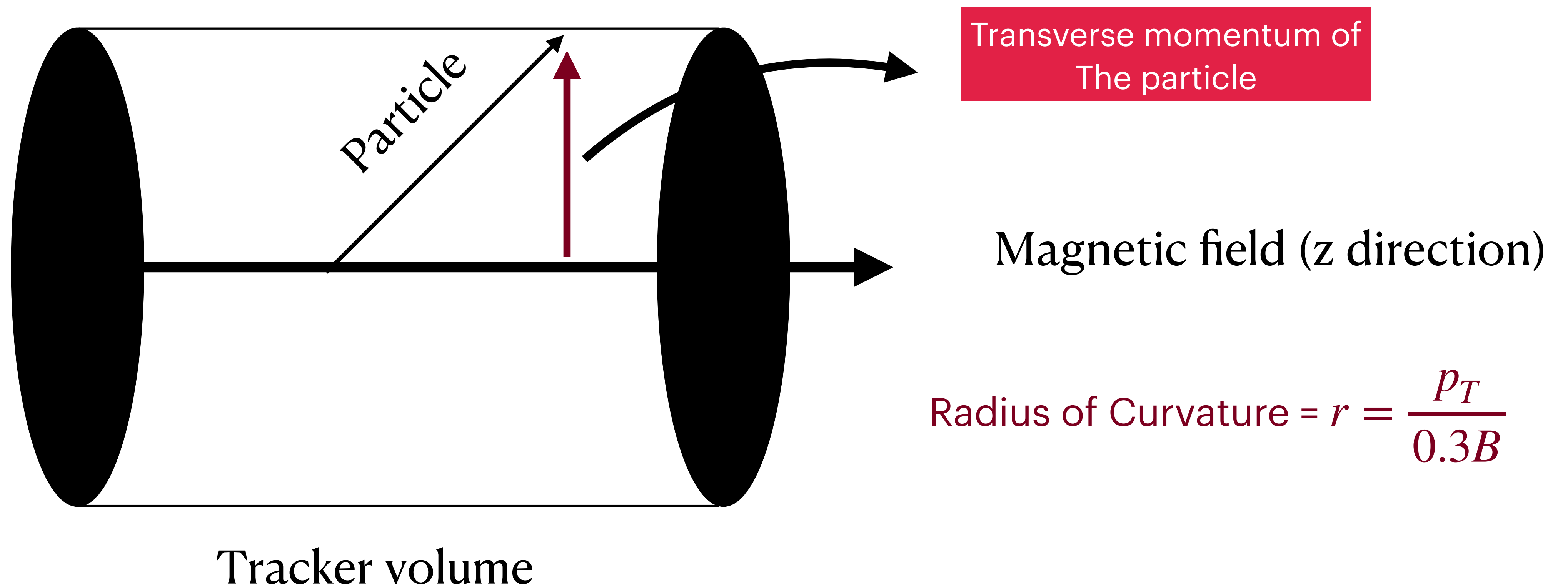
The position measurement should not reduce the energy of the charged particle

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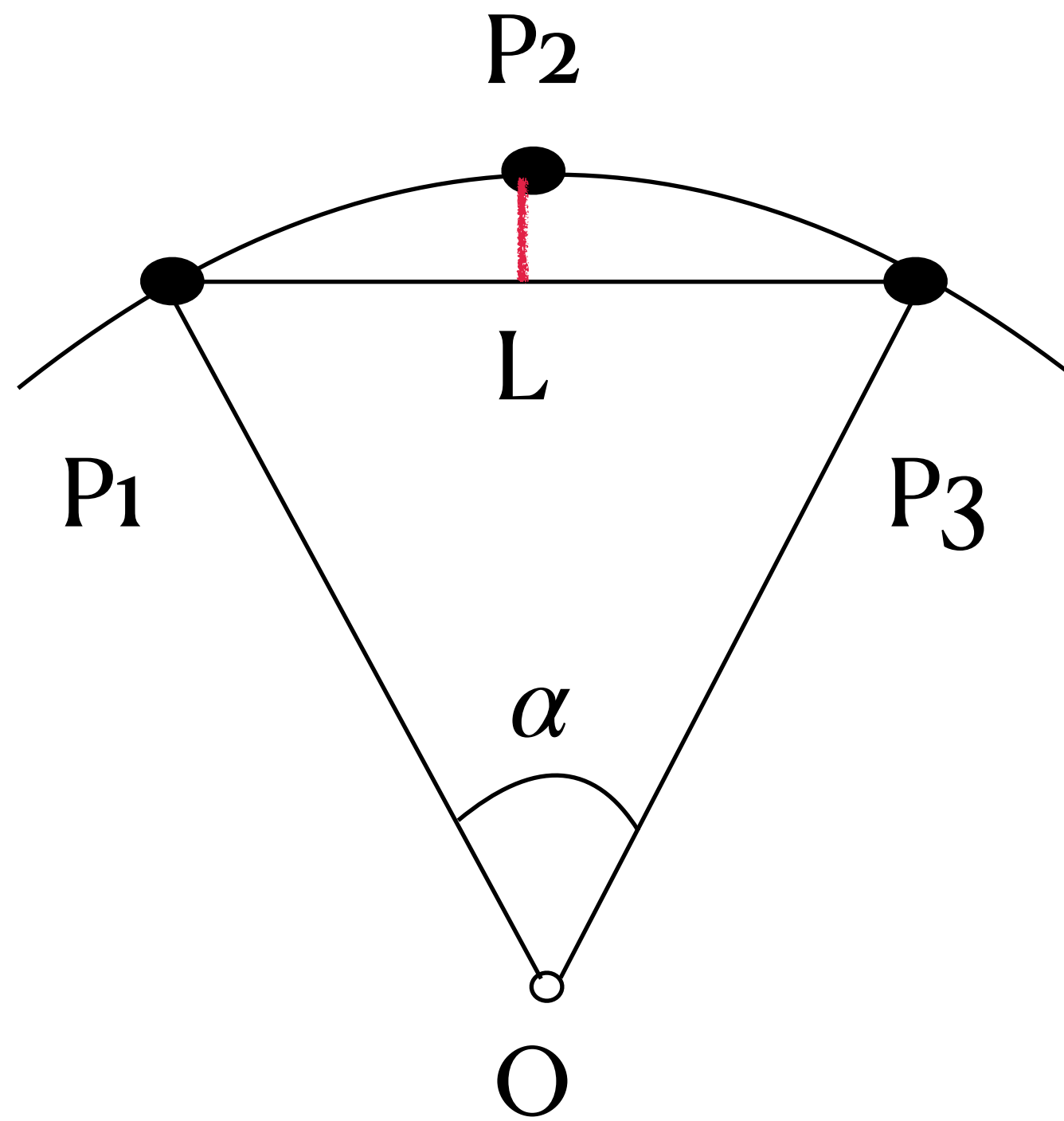
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Tracking

⊗ Magnetic field



Suppose a charged particle is detected at P₁, P₂, P₃

B = Magnetic field in Tesla

$$\alpha \simeq \frac{L}{r}$$

L = The distance between P₁ and P₃

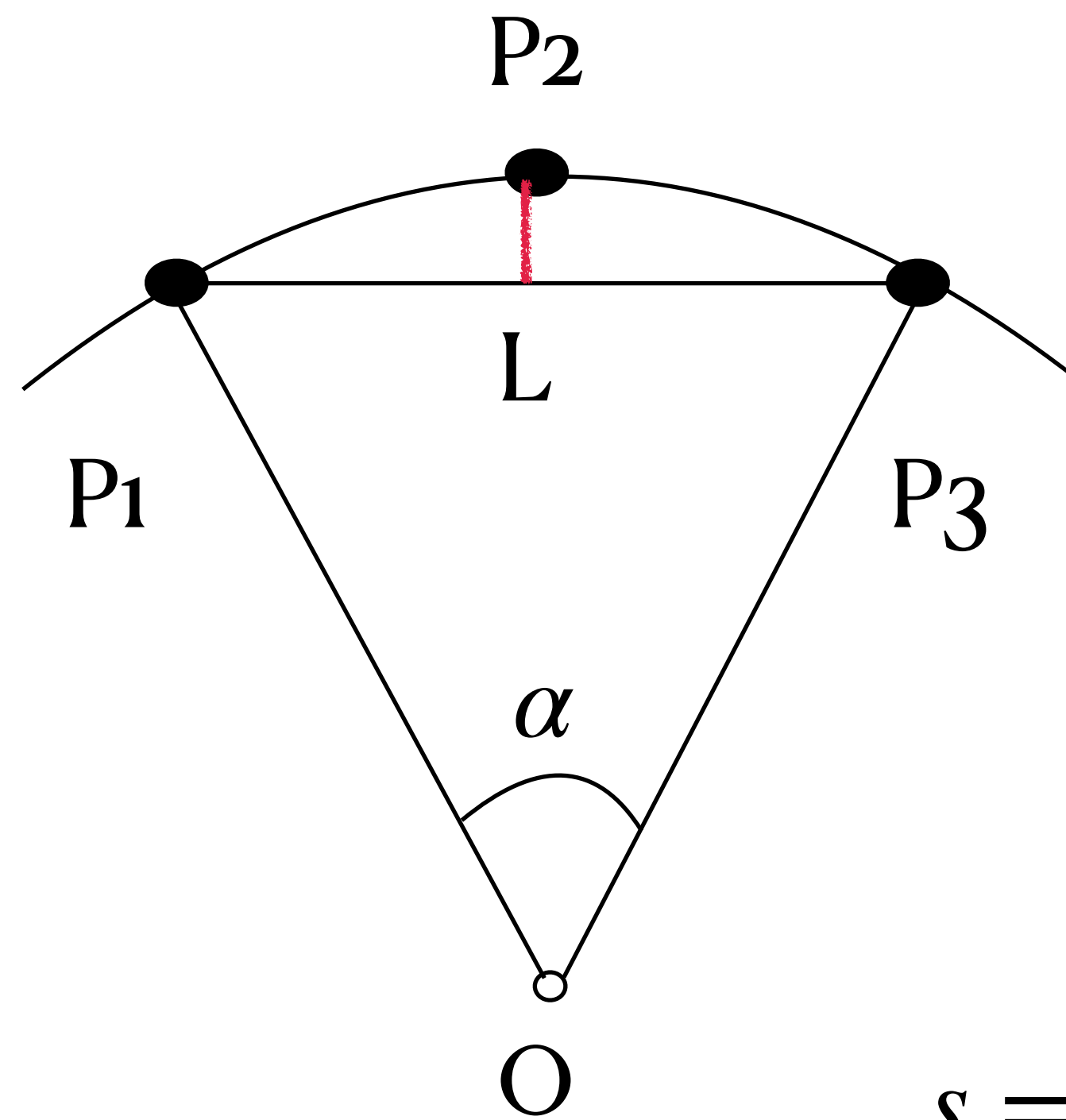
r = Radius of the circle in Meter

p_T = Momentum of the charged particle = 0.3 B r

S = Depth of the arc, called Sagitta in Meter

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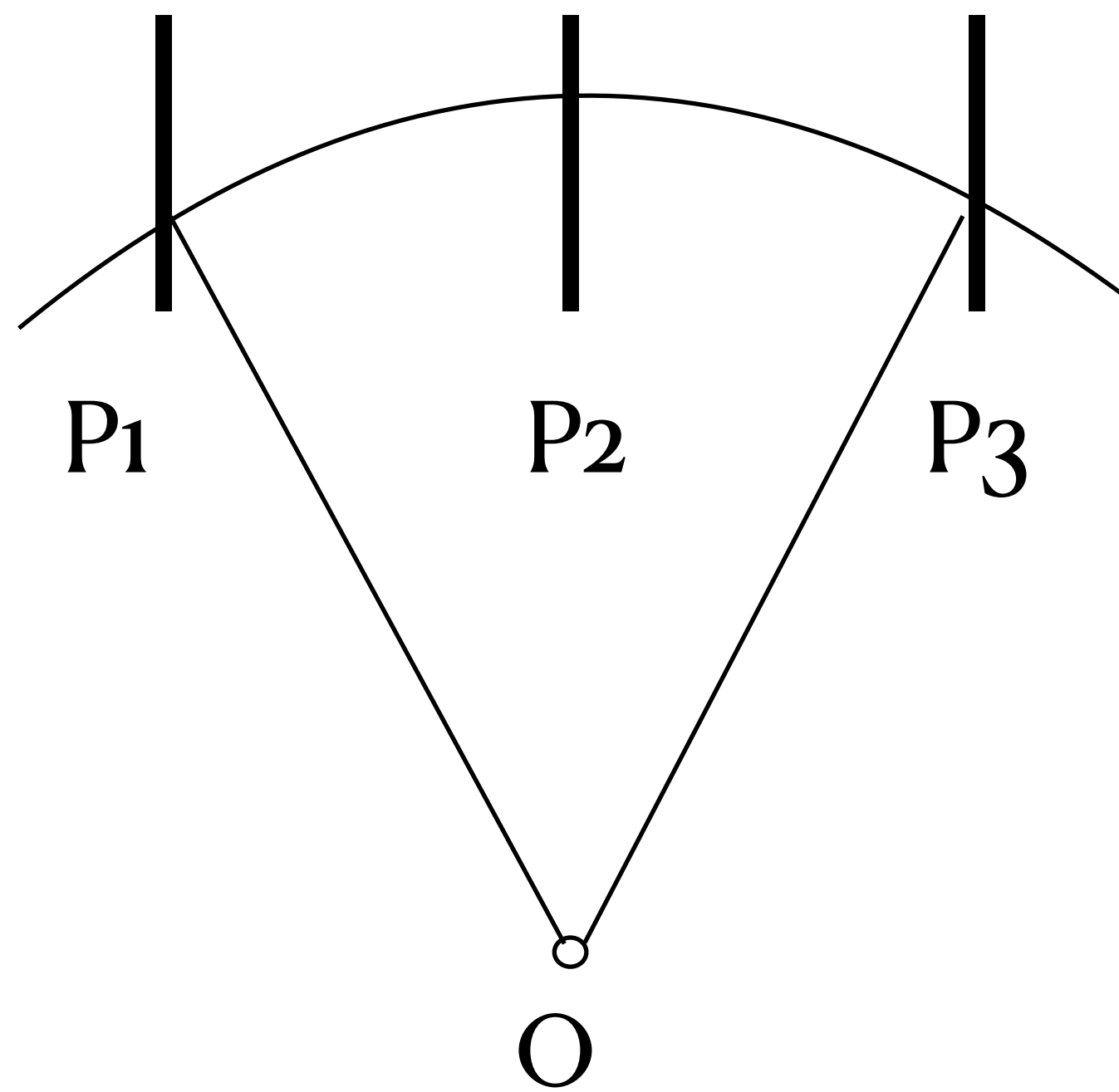
$$s = r \left(1 - \cos \frac{\alpha}{2} \right) \simeq r \left[1 - \left(1 - \frac{1}{2} \frac{\alpha^2}{4} \right) \right] = R \frac{\alpha^2}{8} = \frac{0.3 B L^2}{8 p_T}$$

Example : for p_T = 1 GeV , L = 1 m and B = 1 T Sagitta (s) is ~ 3.8 cm

Tracking



Magnetic field



Suppose three points are used to measure the track

$$s = x_2 - \frac{x_1 + x_3}{2}$$

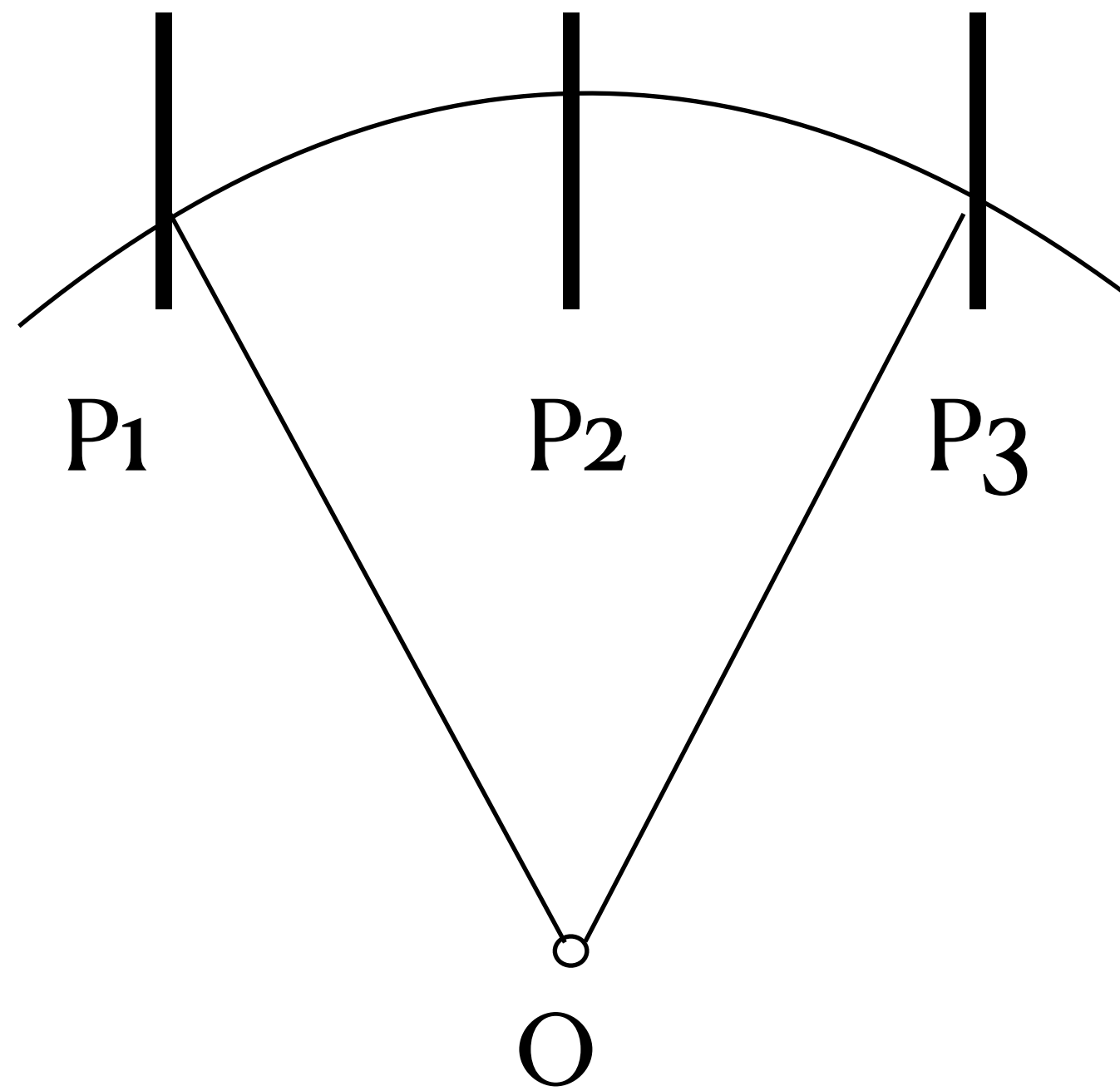
$$\text{Momentum resolution } \frac{\sigma_{p_T}}{p_T} \propto \frac{\sigma}{s} \propto \frac{\sigma 8 p_T}{0.3 B L^2}$$

σ is the uncertainty associated with the position measurement

Tracking



Magnetic field



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For better measurement we need small σ , large B and large L

CMS uses stronger magnetic field than ATLAS

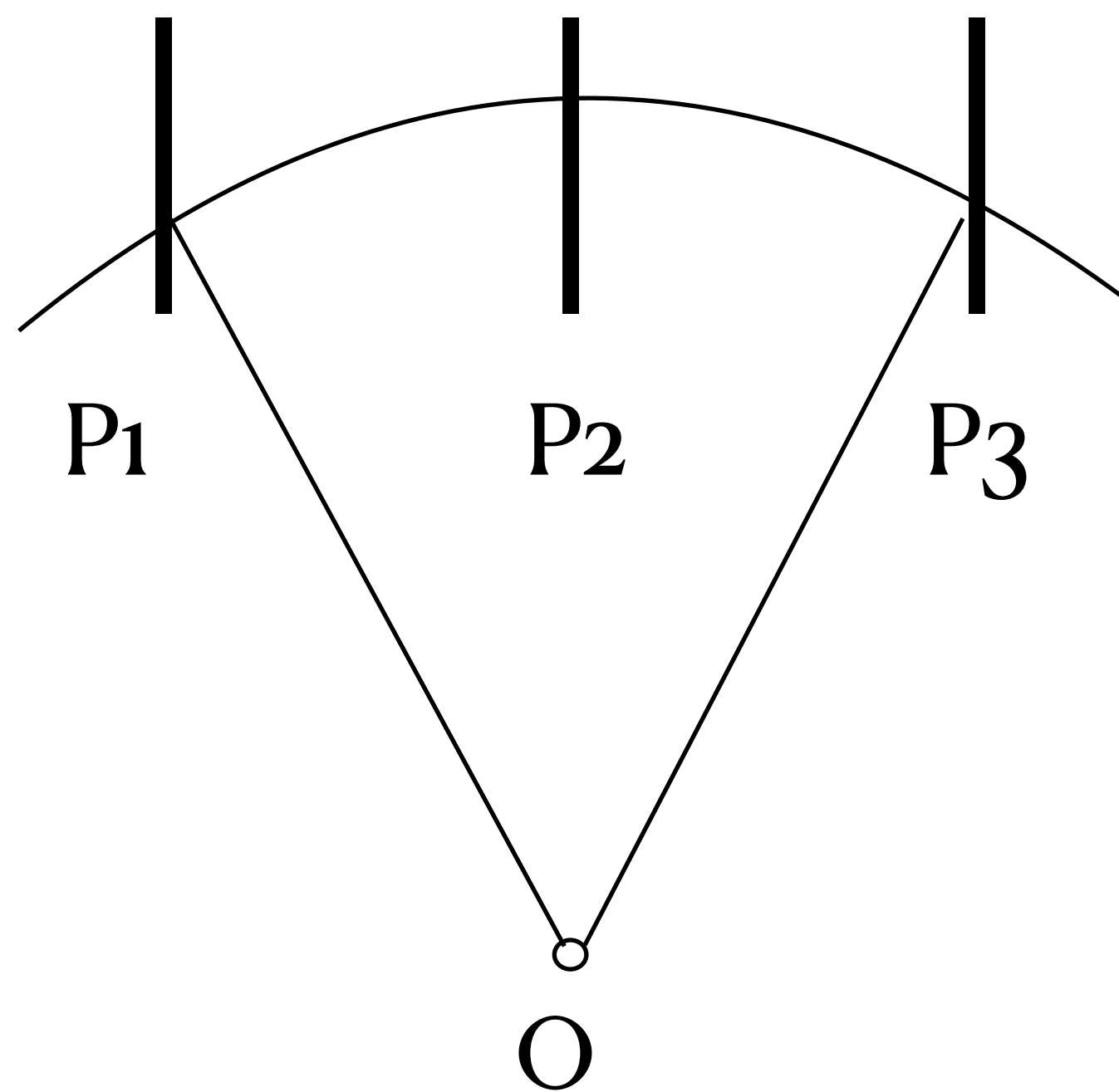
ATLAS uses bigger L than CMS

Resolution degrades with the momentum

Tracking



Magnetic field



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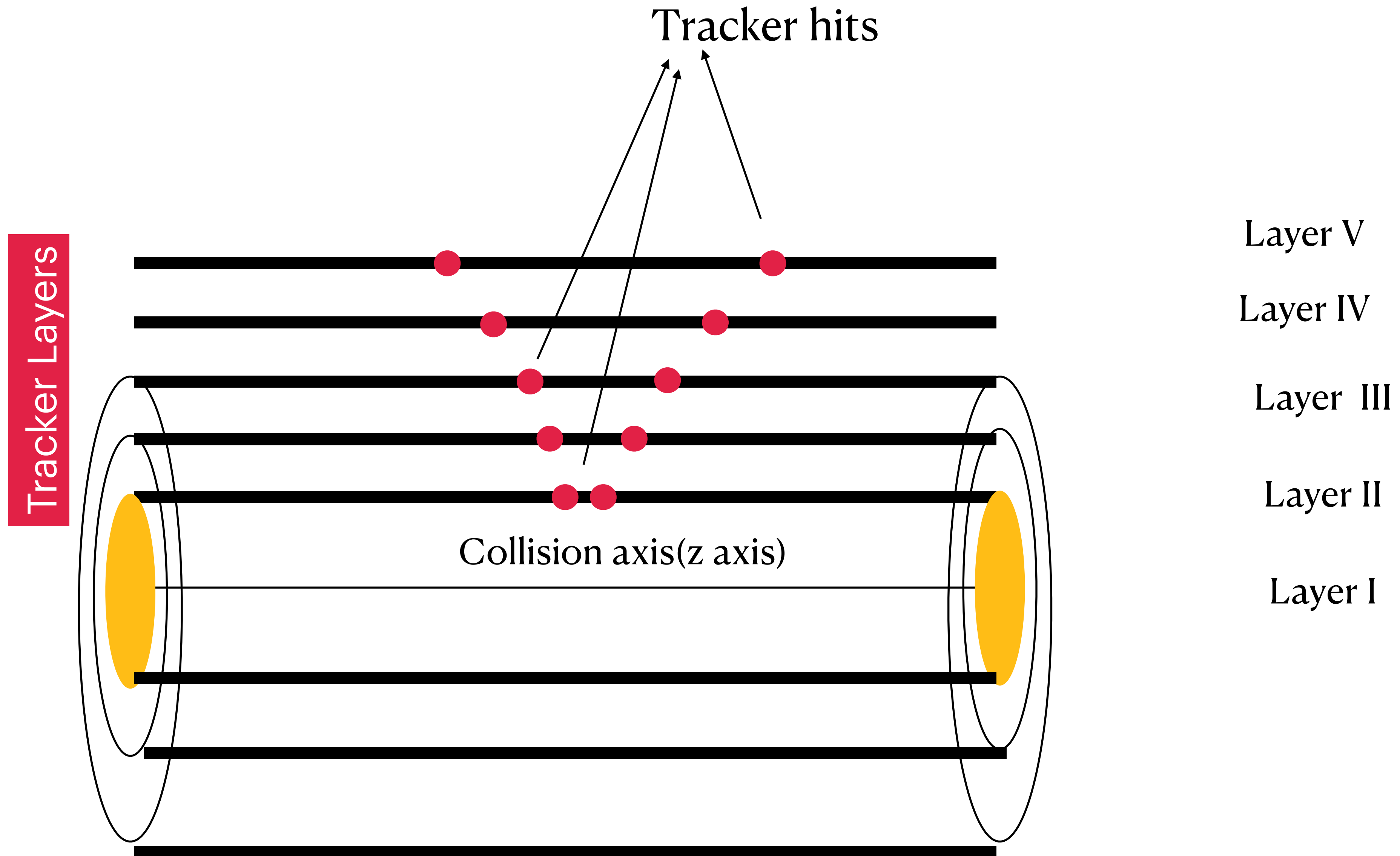
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Resolution degrades with the momentum

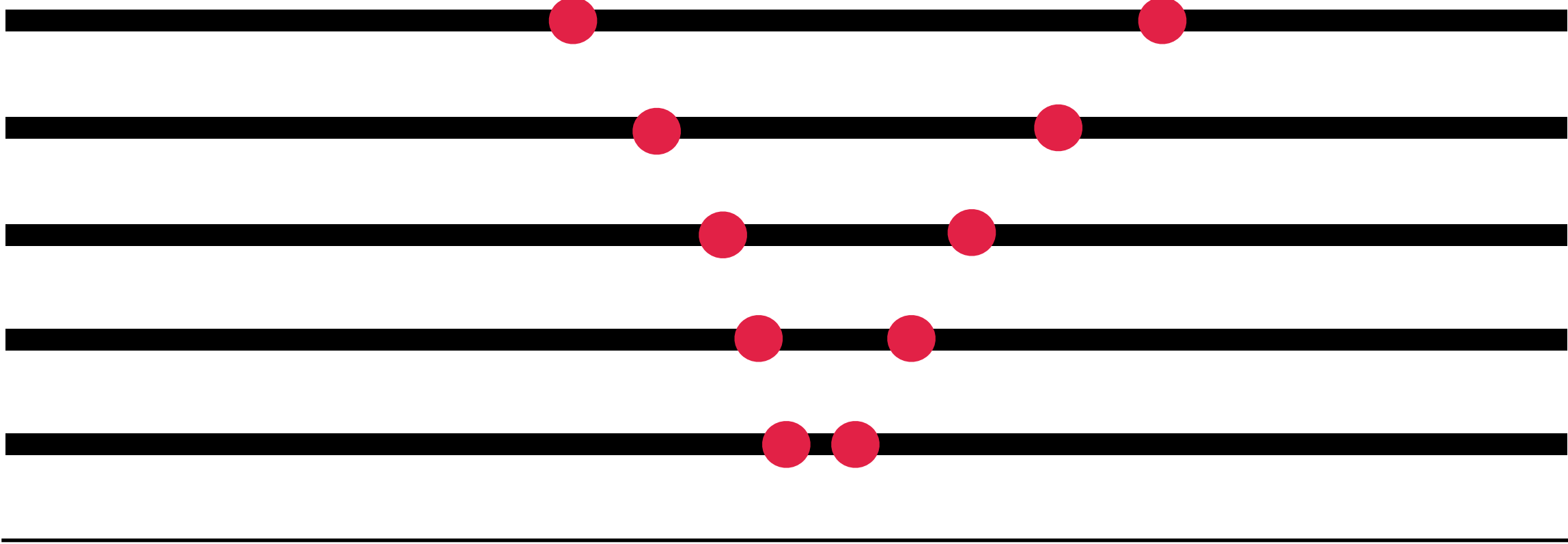
Charged particle inside the thick material undergoes multiple scatterings : This increases the error in the measurement of the Sagitta : Low Z , high radiation length and thin material reduces this effect

Basic Tracker Design



Basic Tracker Design

Tracker Layers



Layer V

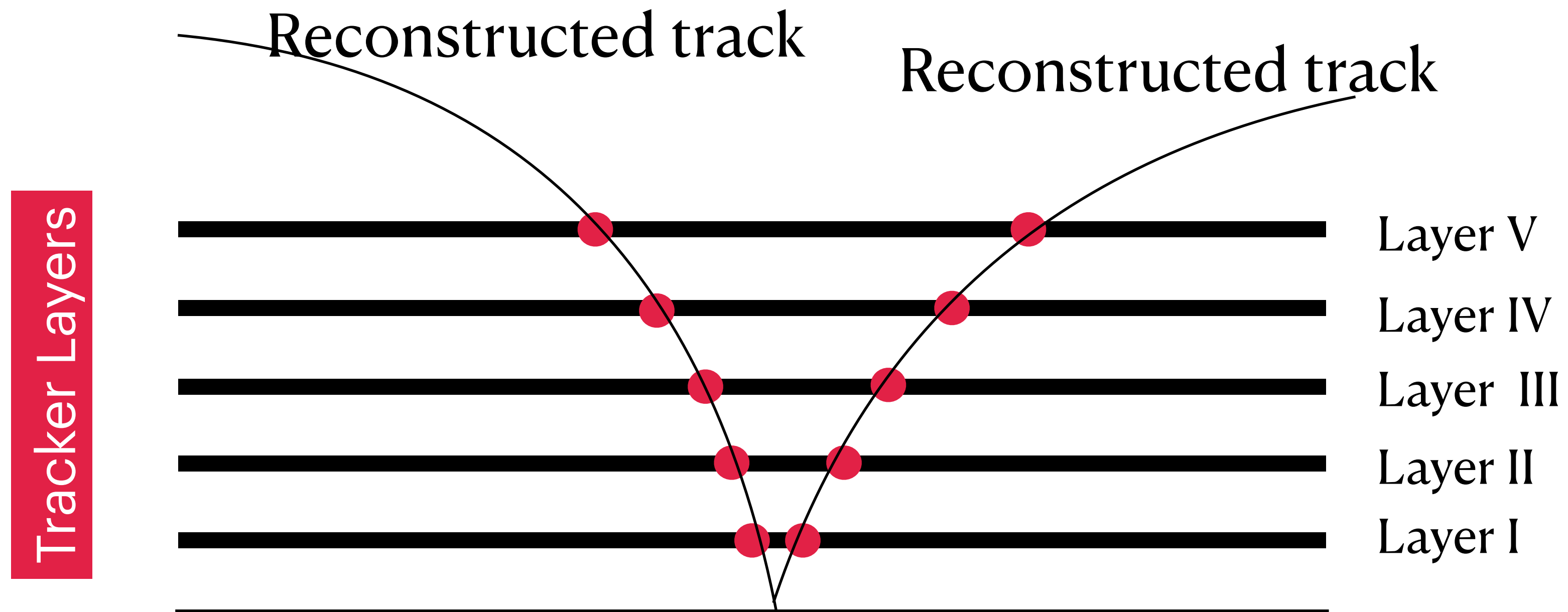
Layer IV

Layer III

Layer II

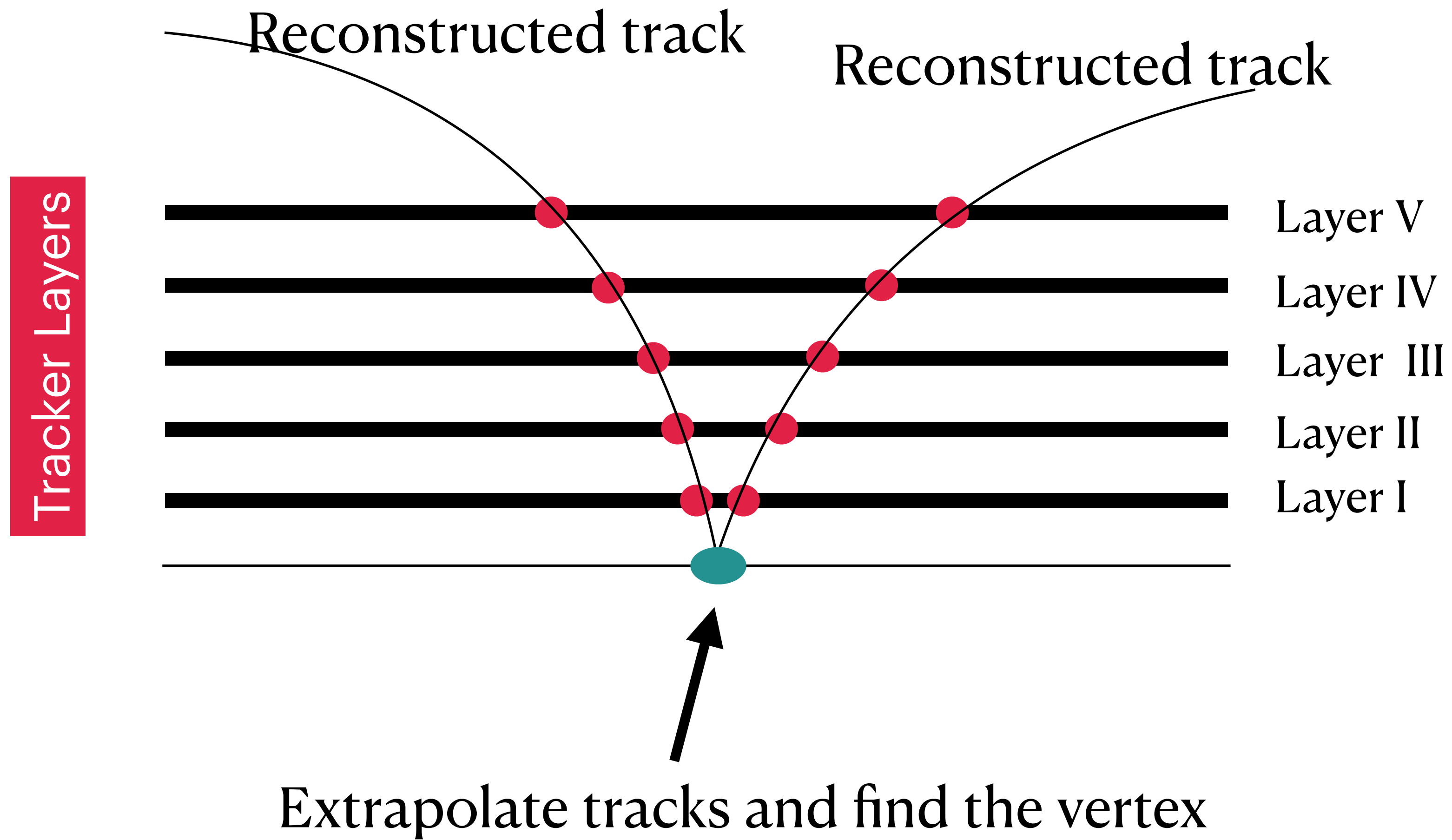
Layer I

Basic Tracker Design

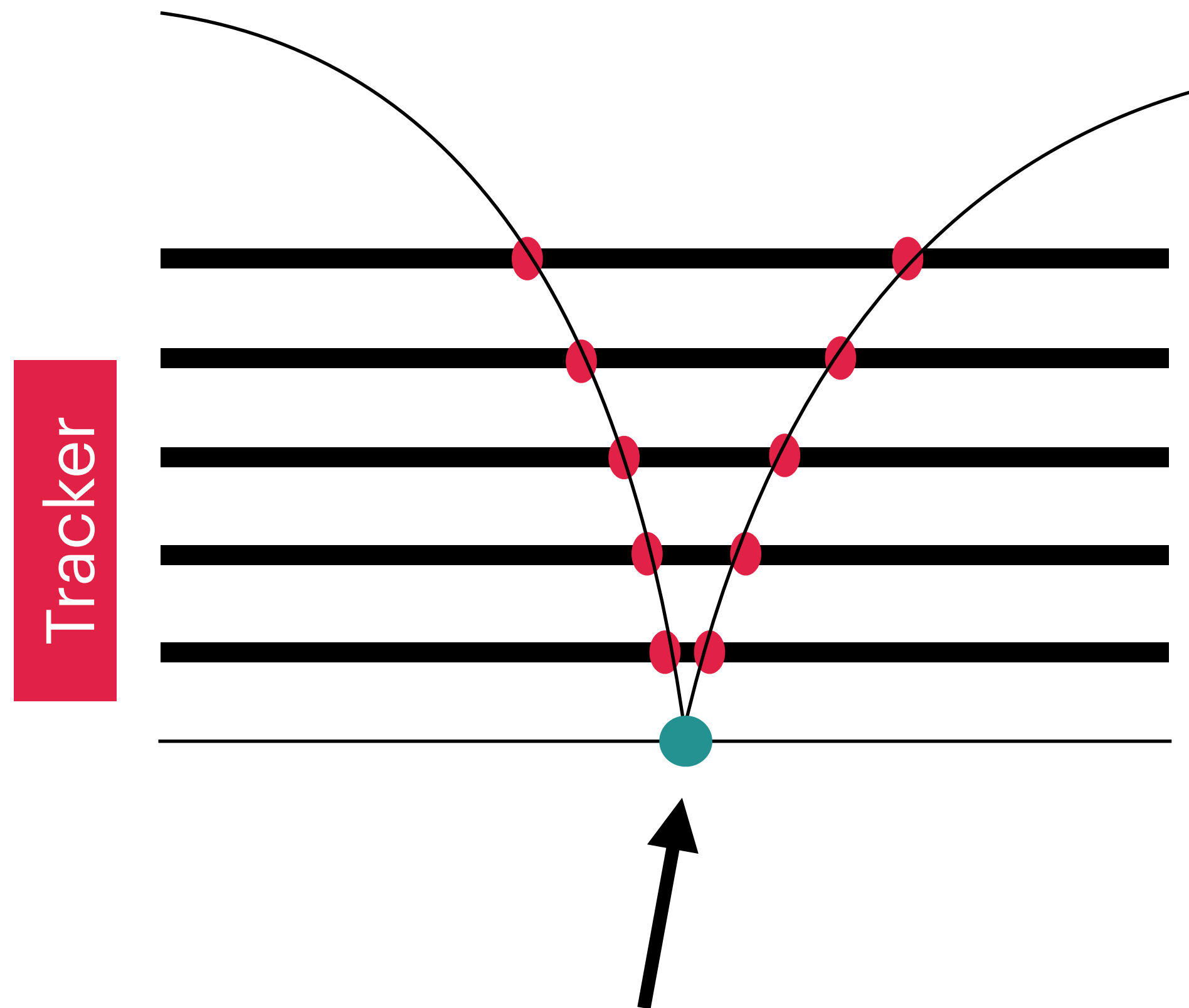


Iterative track finding algorithms (time consuming)

Basic Tracker Design



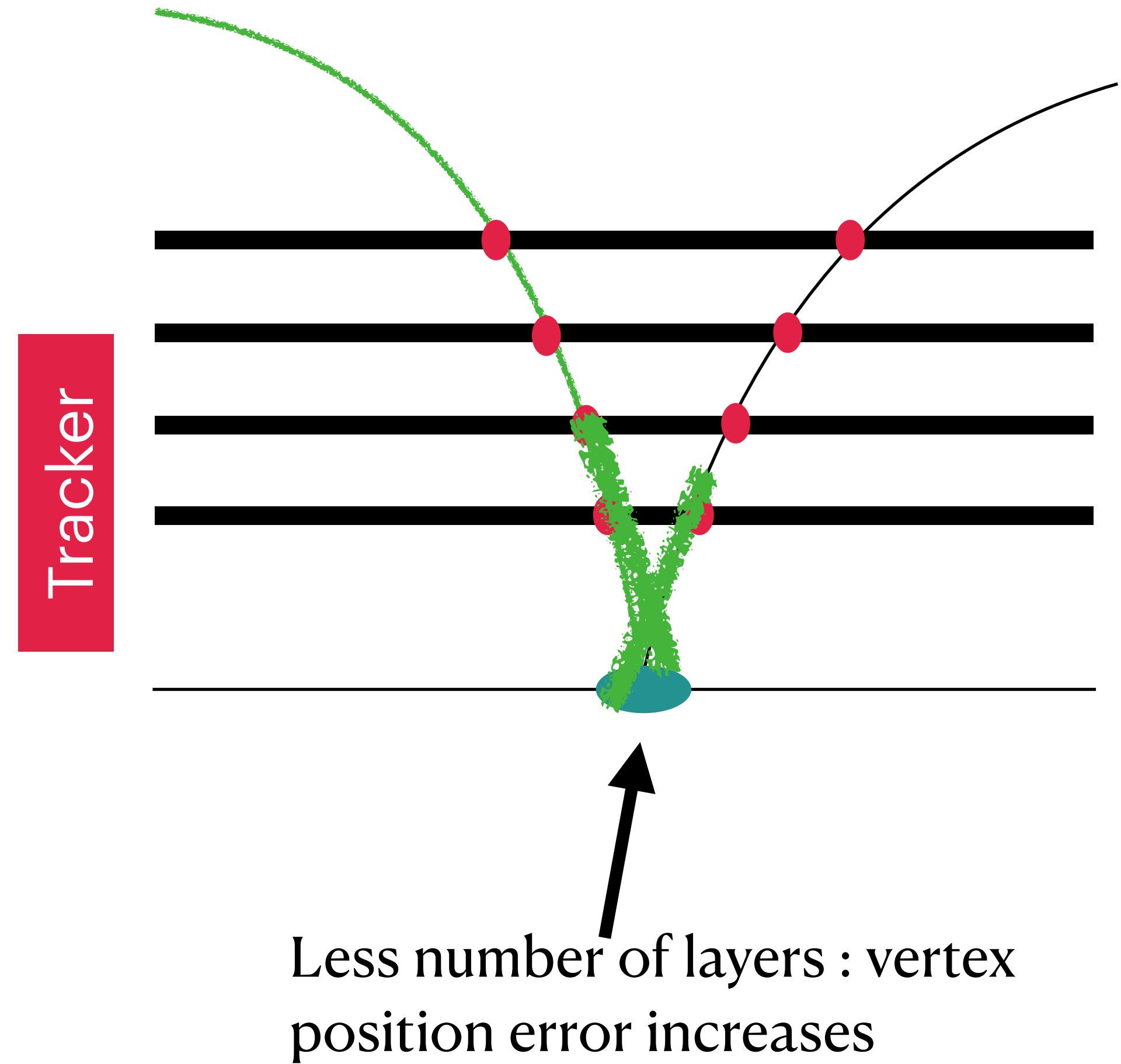
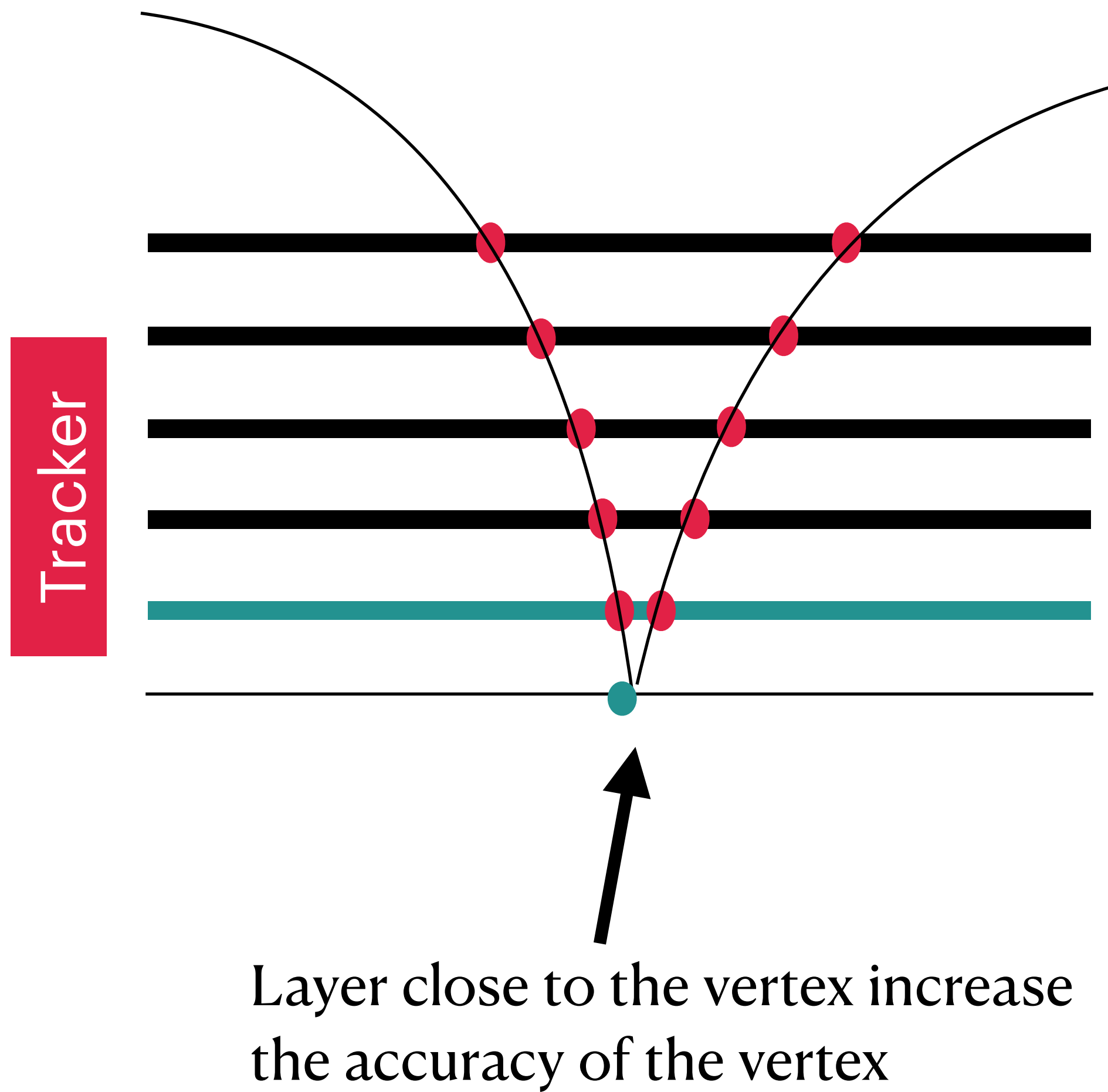
Basic Tracker Design



Extrapolate tracks and
find the vertex

Iterative track finding algorithms (time consuming)
track fitting algorithms => Momentum measurement
Efficiency increases with the number of hits

Basic Tracker Design

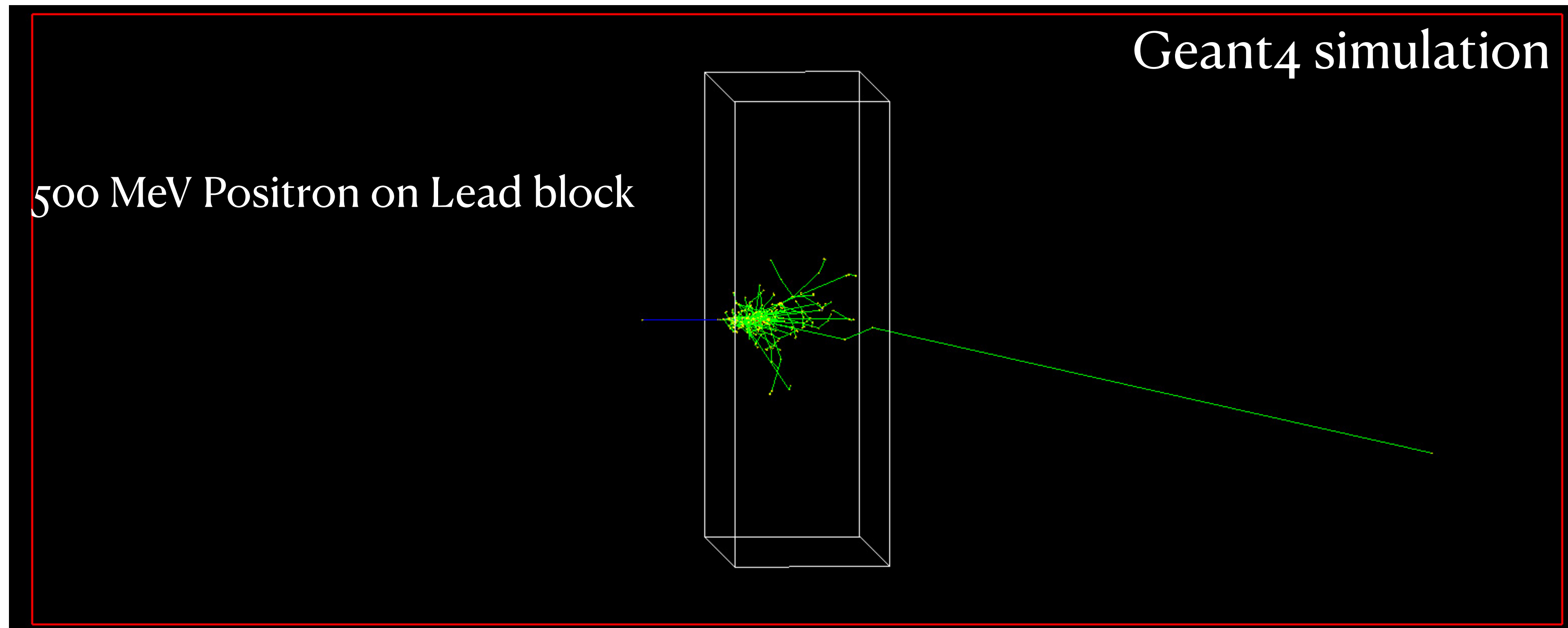


Addition of 4th layer in CMS and ATLAS tracker

Calorimetry

Calorimeter measures energy of charged and neutral hadrons(HCAL),
electron and photon (ECAL) => destructive measurement unlike tracker

Interaction of particle with the detector generates shower => identification of particle



Segmentation helps measure the position / direction of the particle

Calorimetry

Active material: which measures the shower energy

Passive material: which causes the particle to shower (high Z material)

Two Types of calorimeters :

Homogeneous: single active material

Advantage : excellent energy resolution

Disadvantage: costly **Example:** CMS ECAL



Sampling: alternative layers of active and passive materials

Advantage : optimal choice of absorber and active material possible , can be made compact

Cheap passive material

Disadvantage: Only some of the energy is deposited in the detector, energy resolution worse than homogeneous calorimeter

Example: CMS HCAL, ATLAS ECAL and HCAL



Electromagnetic Shower

Incoming particle loses energy=> production of secondary particle

Cascade of secondary electron/positron and photons produced due to the interaction of the particle with the detector material.

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Ionisation. : emission of electrons from the detector material atoms (dominant at low energy)

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$$\frac{dE}{dx} = \frac{E}{X_0} \quad , \text{X}_0 \text{ is called Radiation length}$$

Radiation length: The average distance over which the electron loses its 63% of the energy inside the detector

material $X_0 \propto \frac{1}{Z^2}$ (For air $X \sim 30000$ cm, lead = 0.5 cm)

Electromagnetic Shower

For photon

Photo-electric effect : it dominates in the low energy range

$$\sigma_{photoelectric} \propto \frac{1}{E^{3.5}}$$

Electrons are emitted

Compton Scattering: dominates in the mid energy range

Mostly isotropically

$$\sigma_{compton} \sim \frac{\ln(E)}{E}$$

Pair production: dominates in the high energy range (above 1.02 MeV) $\gamma \rightarrow e^+e^-$ (in the vicinity of the atomic nucleus)

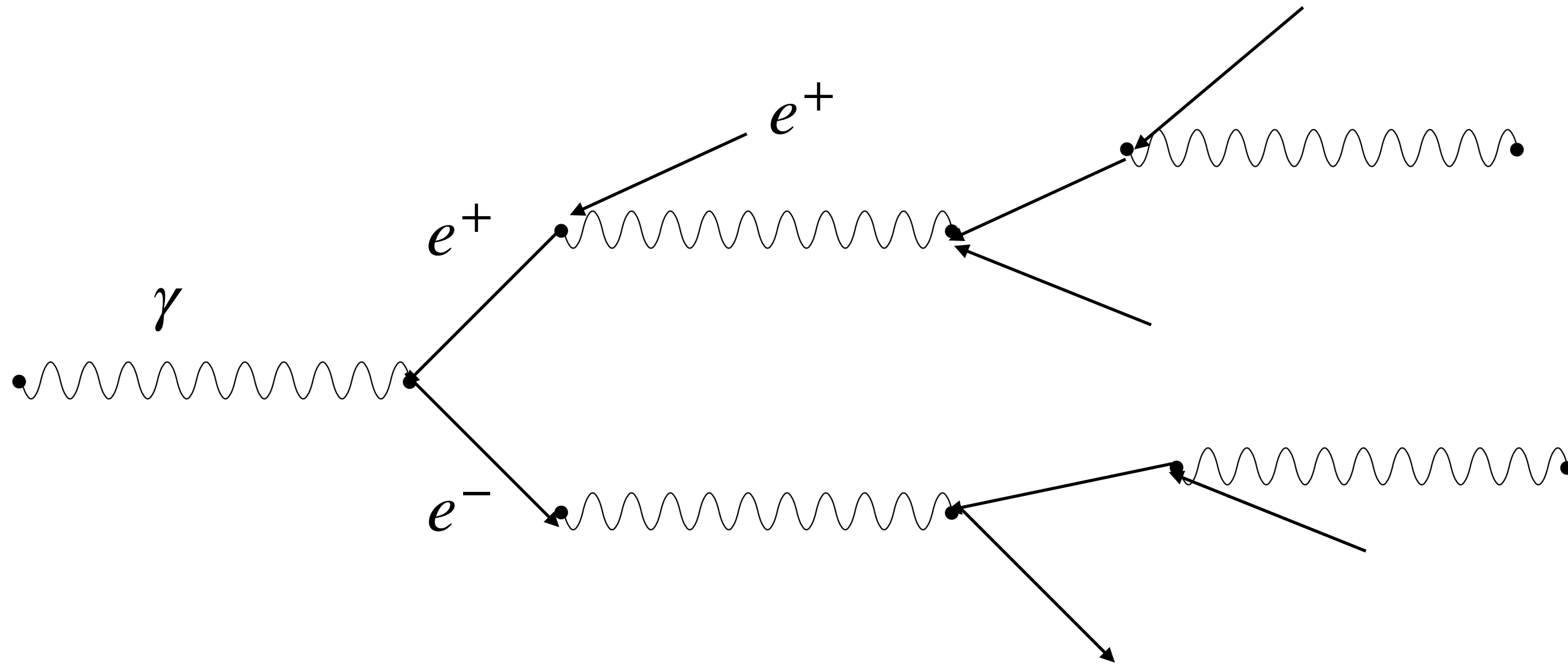
Electron and positron

$$\sigma_{pair} \propto \frac{1}{AX_0}$$

Pair mostly moves in

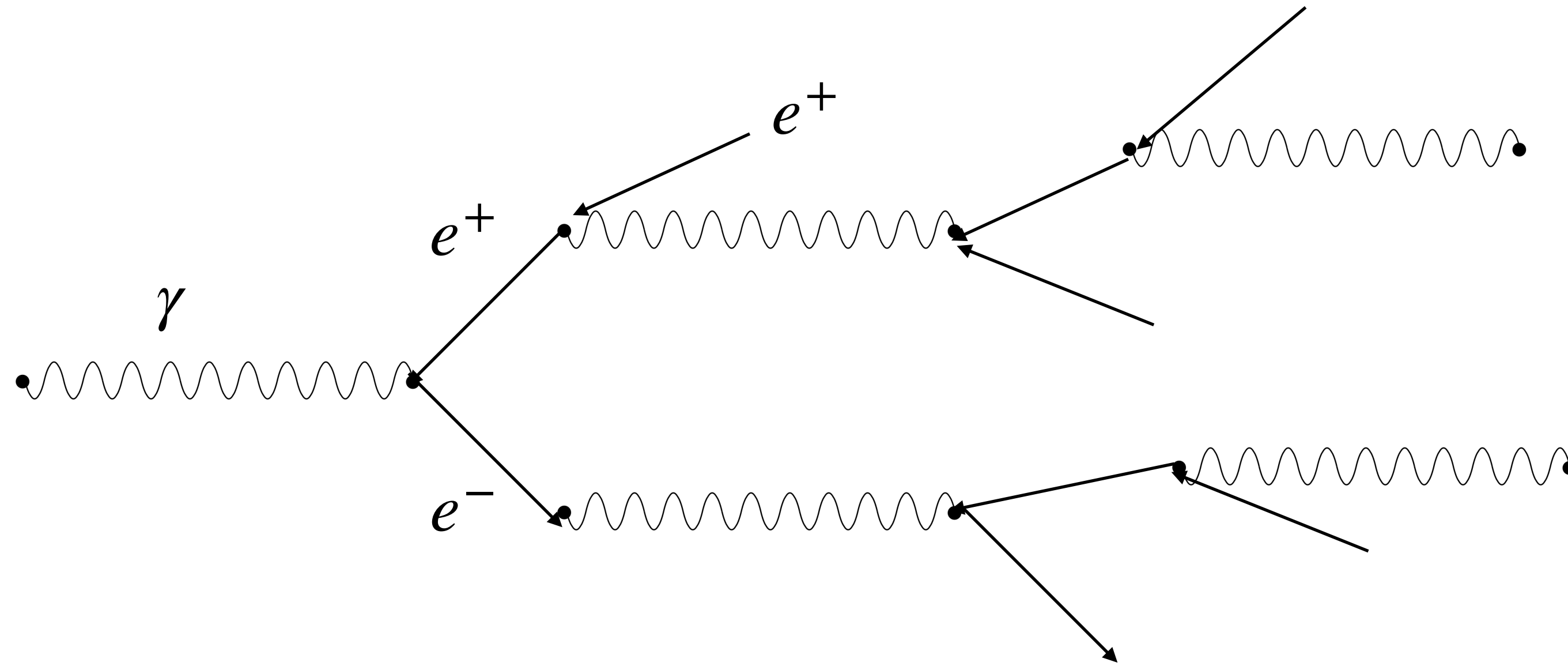
The direction of the photon

Electromagnetic Shower



Below a threshold energy
ionisation dominates ,
Number of secondary
particles reduced and
finally stopped

Electromagnetic Shower



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Shower development is determined by radiation length , it takes an absorber of about 25 radiation length to contain most of the shower

Moeller radius : The transverse development of the shower is determined by Moliere radius

$$R_M \propto X_0$$

99% of the energy is contained in cylinder of radius $5R_M$

Hadronic Shower

Very similar to the EM shower, more complex => many more processes

Elastic scattering : $hadron + nucleus \rightarrow hadron + nucleus$ (no shower produced)

Inelastic scattering : $hadron + nucleus \rightarrow \pi + \pi + \dots + nucleus^*$ etc.

Charge exchange processes: $\pi^- + n \rightarrow \pi^0 + p$

Nuclear spallation : high energy nucleus hits a nucleus, a large number of particles and debris nucleus are emitted.

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Nuclear spallation : high energy nucleus hits a nucleus, a large number of particles and debris nucleus are emitted.

Non detectable part: nuclear binding energy, neutrinos etc.

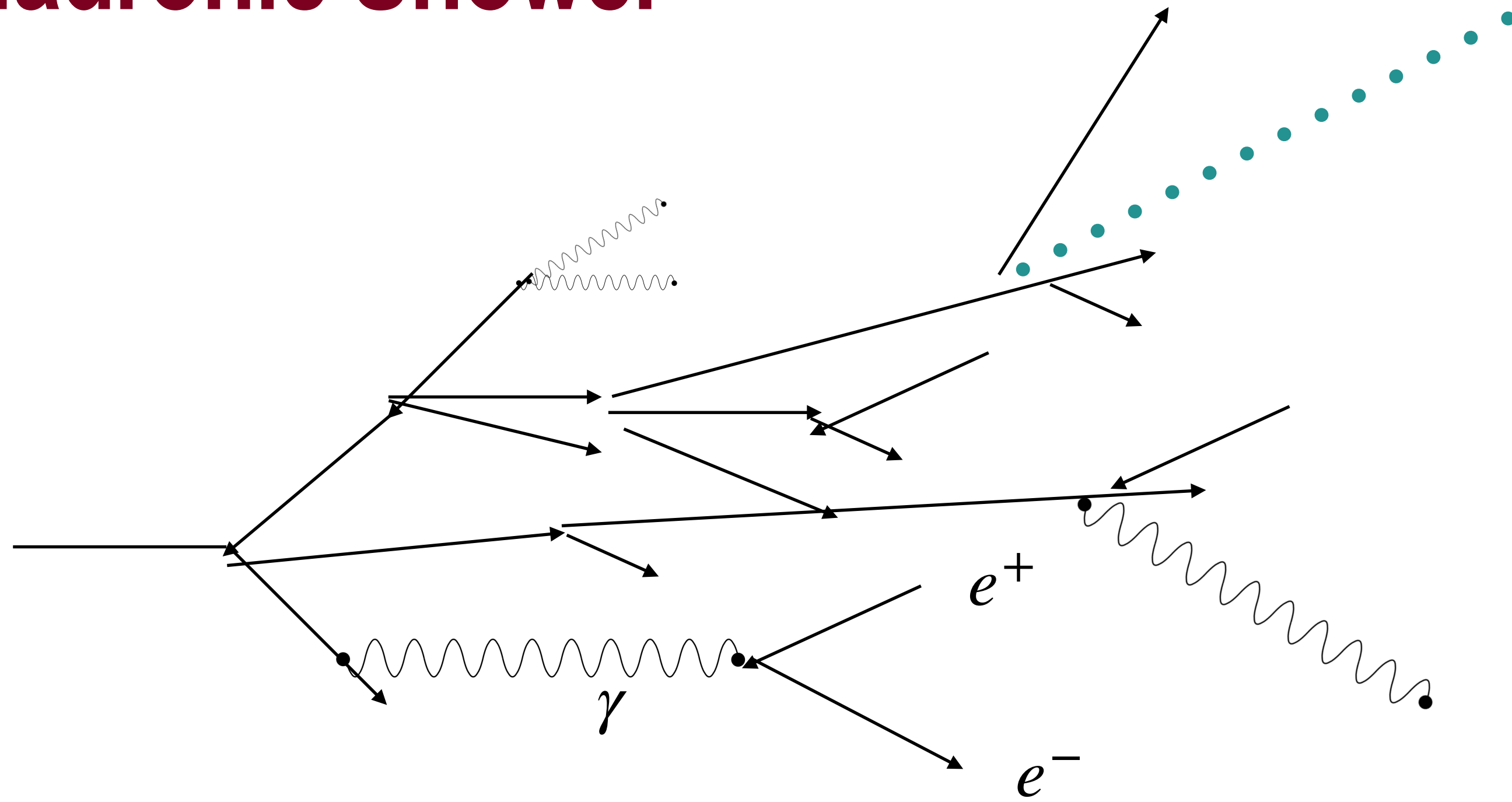
Shower has two component : hadronic and electromagnetic (photons also come from neutral

Pion decay, nuclear de-excitations) => large fluctuations of EM and hadronic components (event by event)

Shower development determined by mean free length between subsequent inelastic collisions

$$\lambda_{Interaction\ length} \sim 35 A^{1/3} \text{ in cm}$$

Hadronic Shower



Hadronic shower has more depth than EM shower

Mean fraction of EM showers
 $\propto \ln(E)$

Production of secondary hadrons from the inelastic collision, sequential inelastic collisions

Inelastic collision stops below pion production energy threshold => ionisations starts

Decays of pion to photons (hadronic shower contains a substantial electromagnetic fraction)

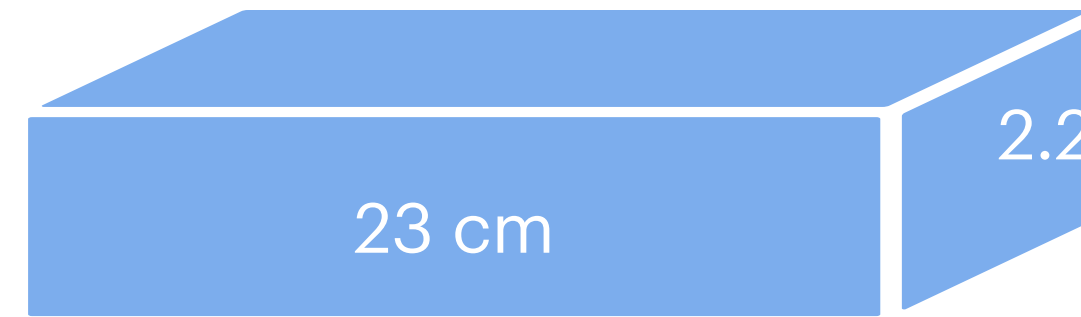
Missing part: neutrinos, nuclear binding energy, delayed photons from nuclear de-excitation, low energy neutron etc.)

some part is compensated by neutron capture (fission) -> release of energy

CMS and ATLAS Calorimeter

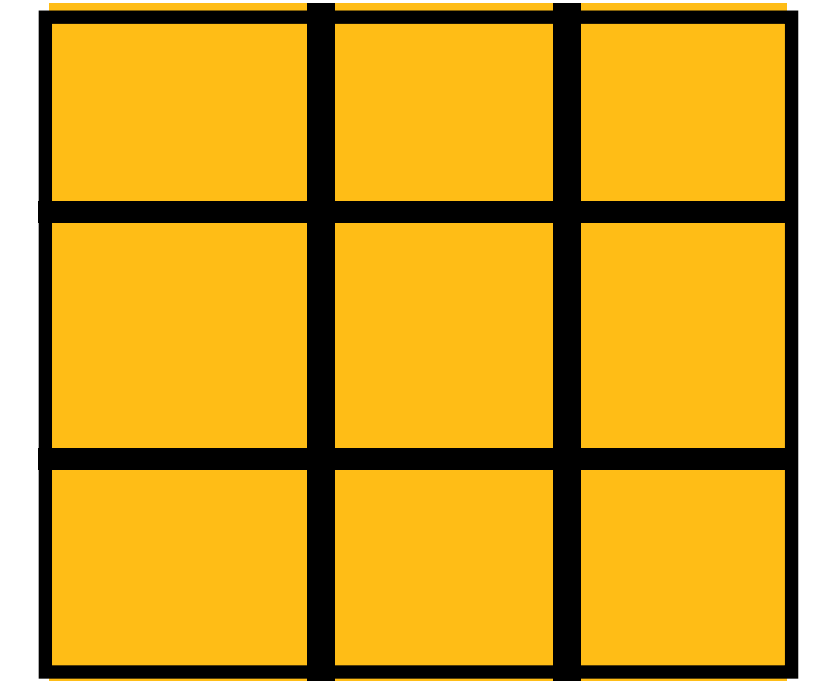
**CMS
ECAL**

Homogeneous calorimeter



PbWO_4 crystal $X_0 \sim 0.9$ cm and $R_M \sim 2.2$ cm

23 cm long crystal with a front face 2.2 cm X 2.2 cm



3 X 3 or 5X 5 crystals contain the energy of the electron/photon

Sampling calorimeter

**ATLAS
ECAL**

Active material: Liquid Argon and absorber: Pb

$24X_0$ total length

Longitudinal segmentation

CMS and ATLAS HCAL : sampling type

Energy resolution

Accuracy in the energy measurement in the Calorimeter

$$\frac{\sigma}{E} = \left(\frac{\sigma}{E}\right)_{stat} + \left(\frac{\sigma}{E}\right)_{instru} + \left(\frac{\sigma}{E}\right)_{sys}$$

$$\left(\frac{\sigma}{E}\right)_{stat} = \frac{\sqrt{N}}{N} = \frac{a}{\sqrt{E}}$$

$$\left(\frac{\sigma}{E}\right)_{Instru} = \frac{b}{E}$$

$$\left(\frac{\sigma}{E}\right)_{syst} = c$$

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Energy proportional to the number of secondary particles N

$$\left(\frac{\sigma}{E}\right)_{Instru} = \frac{b}{E}$$

Noise independent of energy

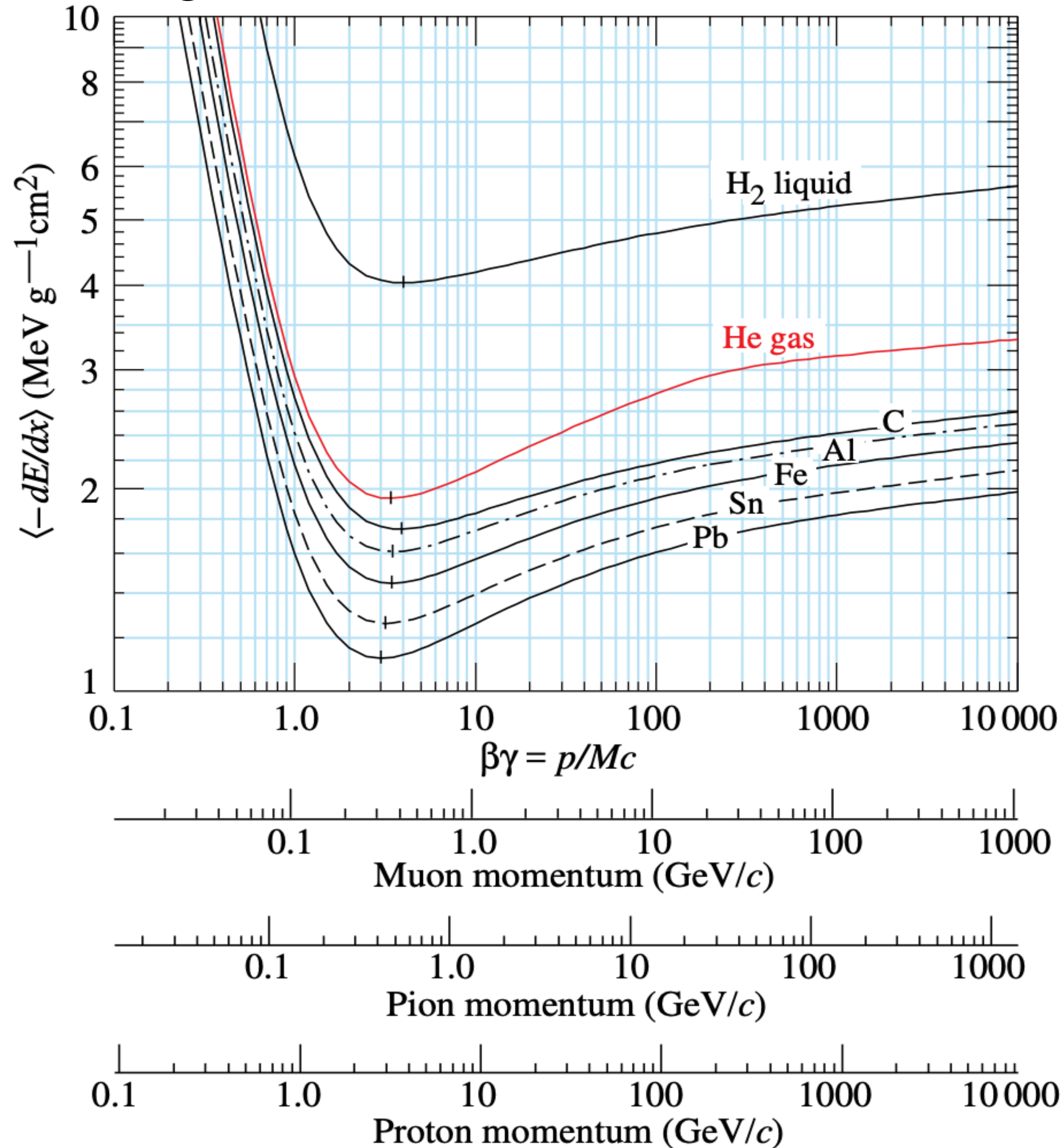
$$\left(\frac{\sigma}{E}\right)_{syst} = c$$

Some systematics increases with Energy (non uniformity of the calorimeter)

Additional error comes from the sampling

Muon Detection

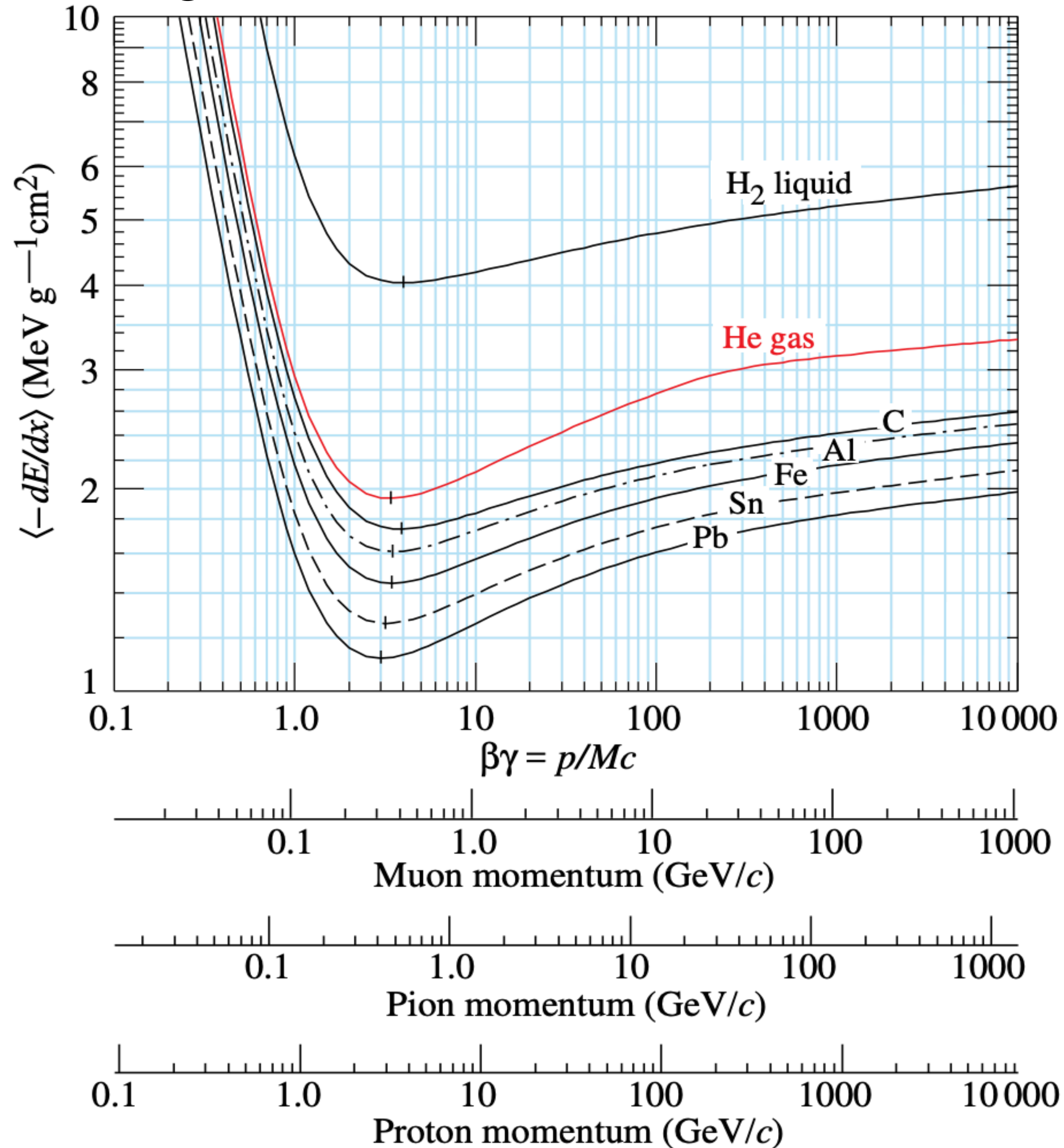
The region where Bethe Block formula is valid



Minimum Ionizing particle : whose energy loss is close to minimum

Muon Detection

The region where Bethe Block formula is valid



Minimum Ionizing particle : whose energy loss is close to minimum

Muon in 100 cm thick Iron block

$$\left\langle \frac{dE}{dX} \right\rangle \Big|_{\text{muon}} = 1.5 \text{ MeV g}^{-1} \text{ cm}^2$$

$$\rho(\text{Fe}) = 7.87 \text{ g cm}^{-3}$$

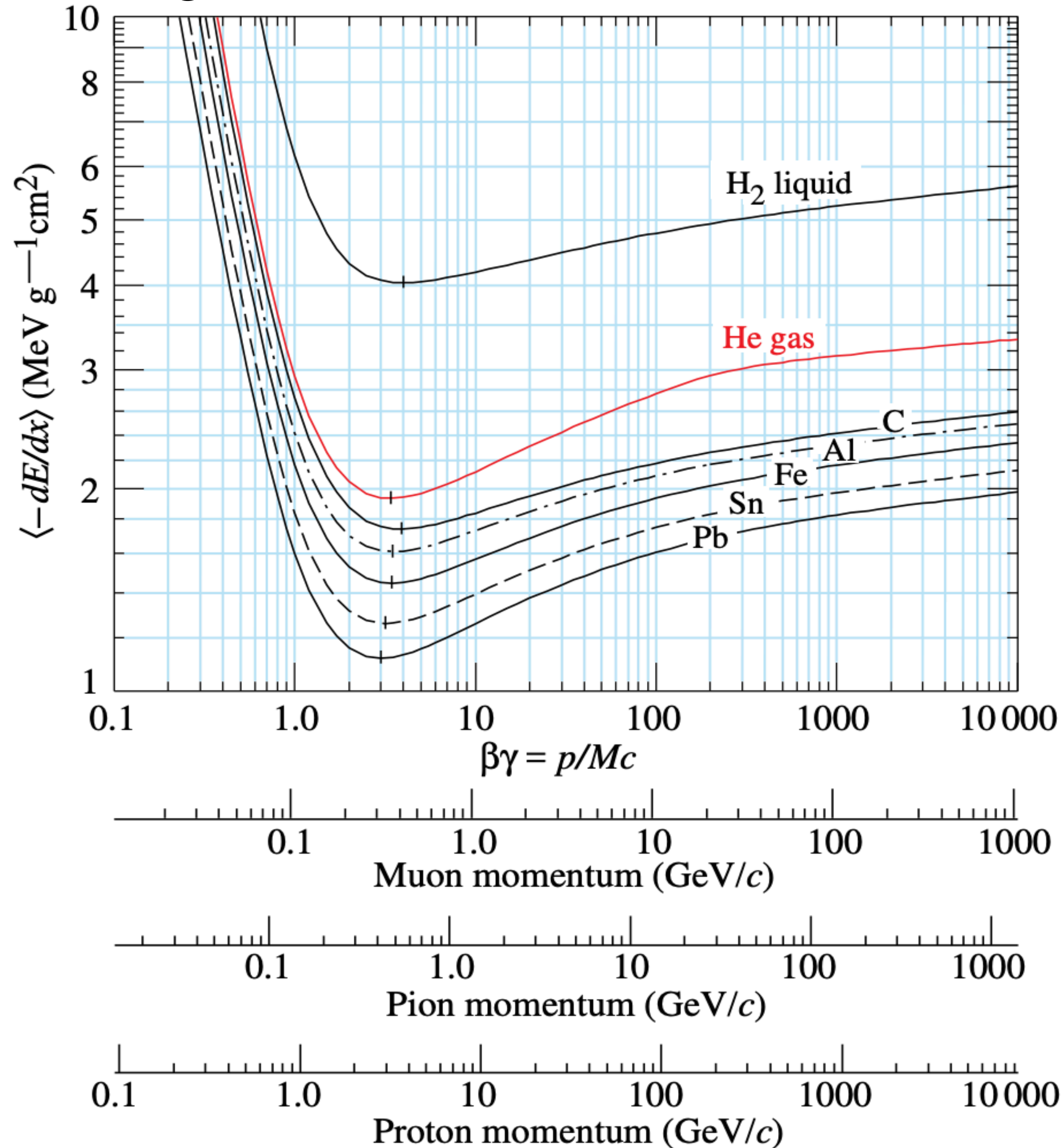
$$\text{Energy loss} = 1.5 \times 100 \times 7.8 \sim 1 \text{ GeV}$$

Muon penetrates through ECAL and HCAL

Significant bremsstrahlung from Muon starts with energy above 1 TeV

Muon Detection

The region where Bethe Block formula is valid



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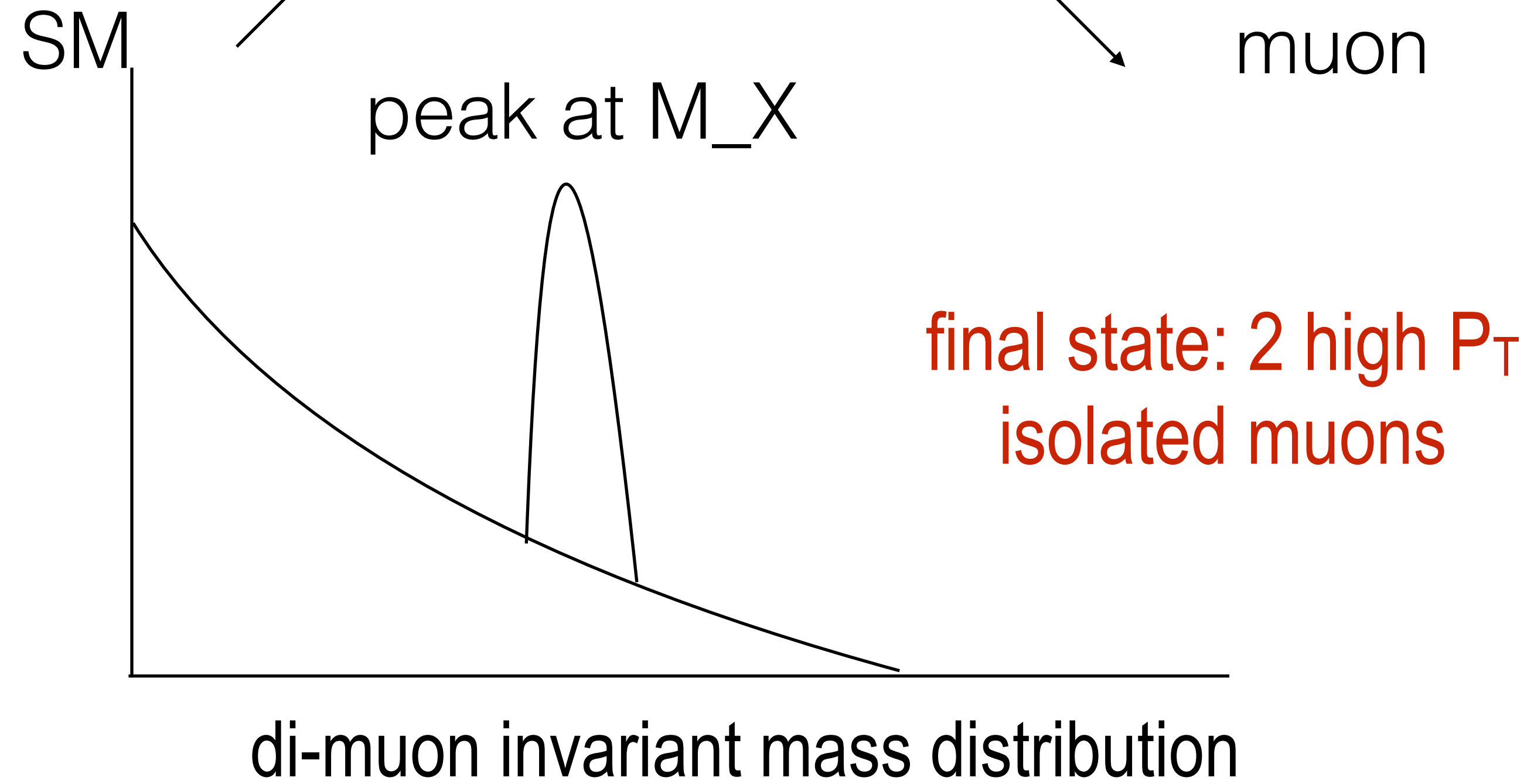
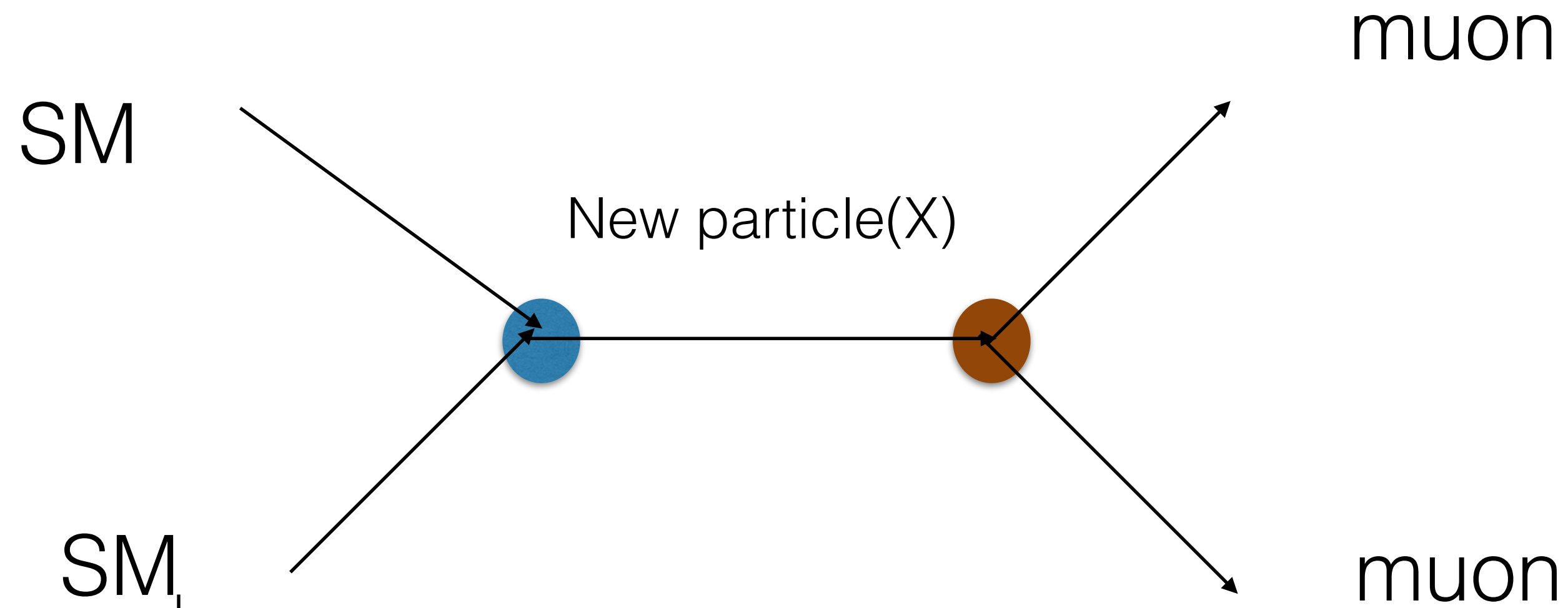
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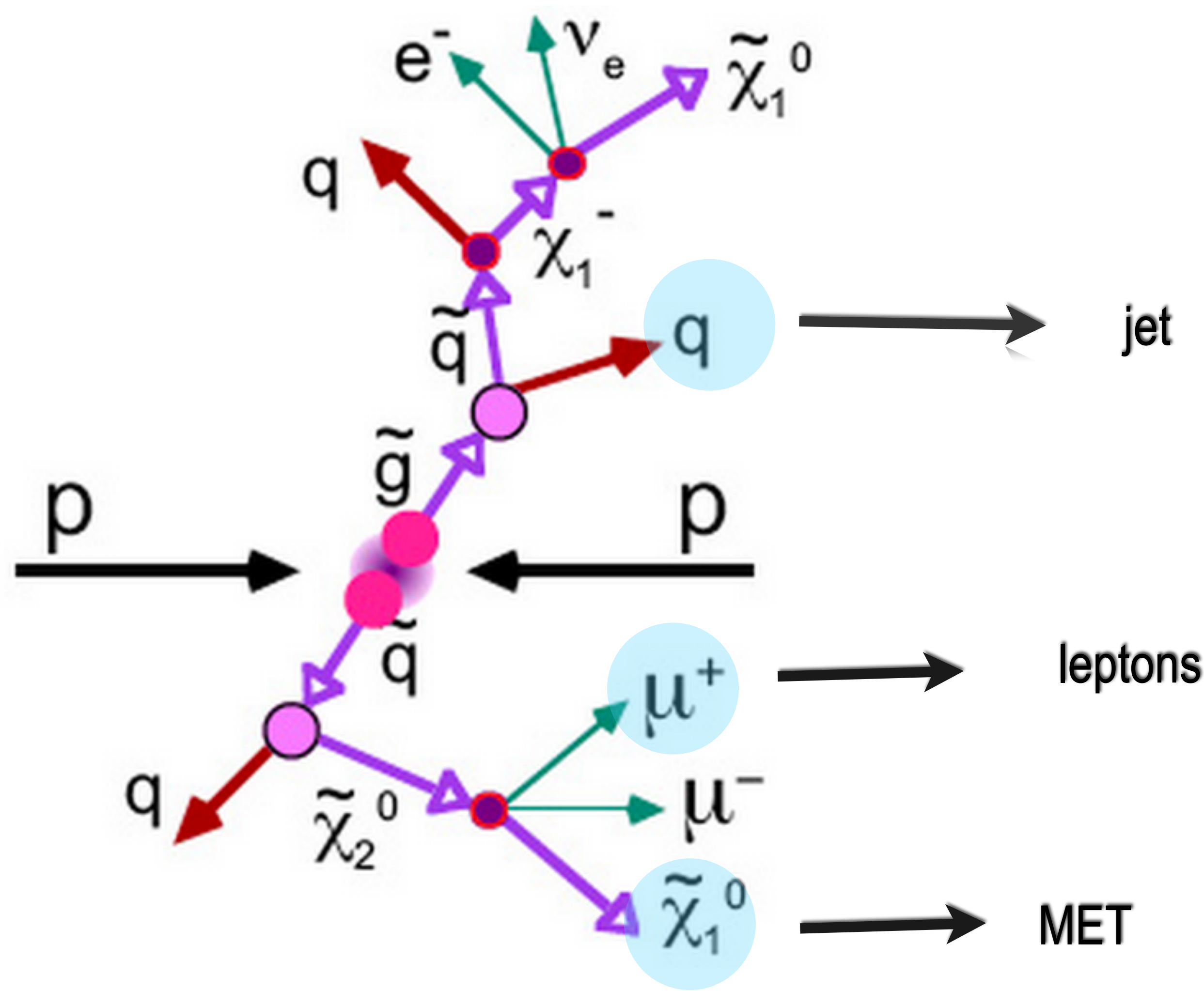
New Physics searches : Variables

New physics Search: Resonance

The decay products of the new particle are visible SM particles



New physics Search: Cascade



Final state

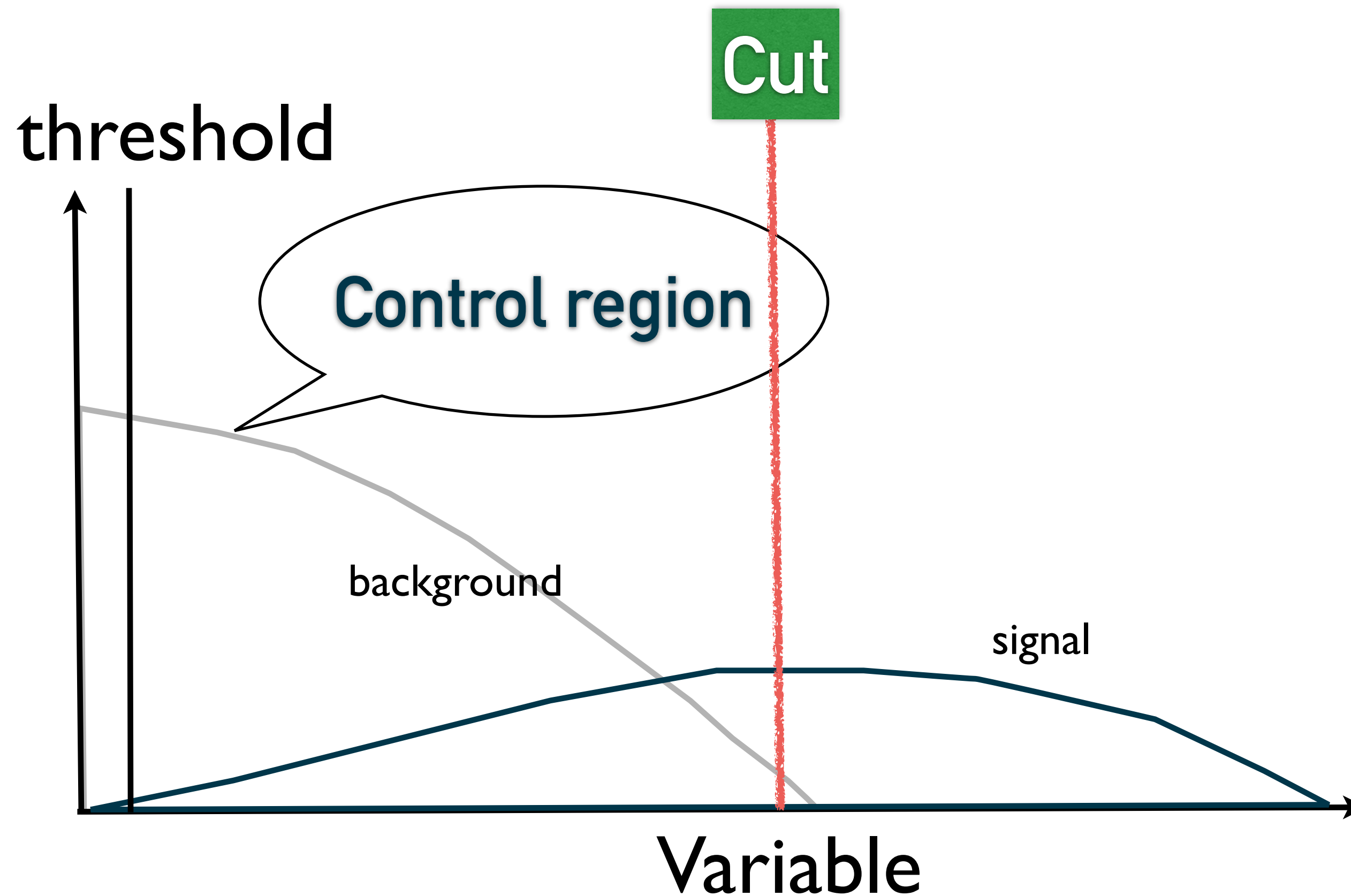
Jets
+
leptons
+
missing transverse energy

R- parity conserved

Lightest SUSY particle is stable (dark matter candidate)
Missing transverse energy

Signal vs Background : Cuts

Define variables which can discriminate signal and background



Some numbers

SM cross sections (background)
QCD($p_t > 100$ GeV) = 2000000 pb
W + jets = 20000 pb (W decays to electron)
top pair = 900 pb

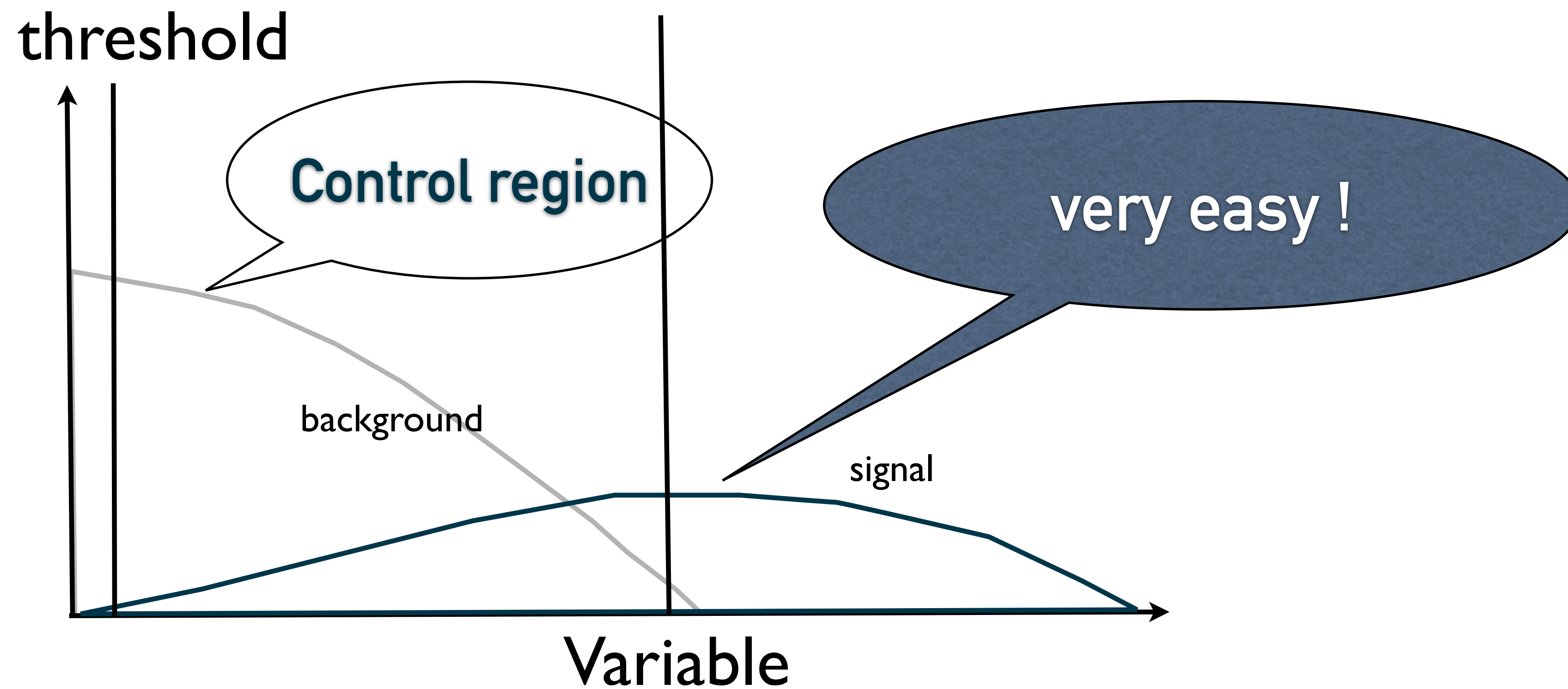
SUSY cross sections (signal)

Gluino pair (mass = 1 TeV)
~ 450 fb
stop pair (mass = 1 TeV)
~ 10 fb

Signal vs Background : Cuts

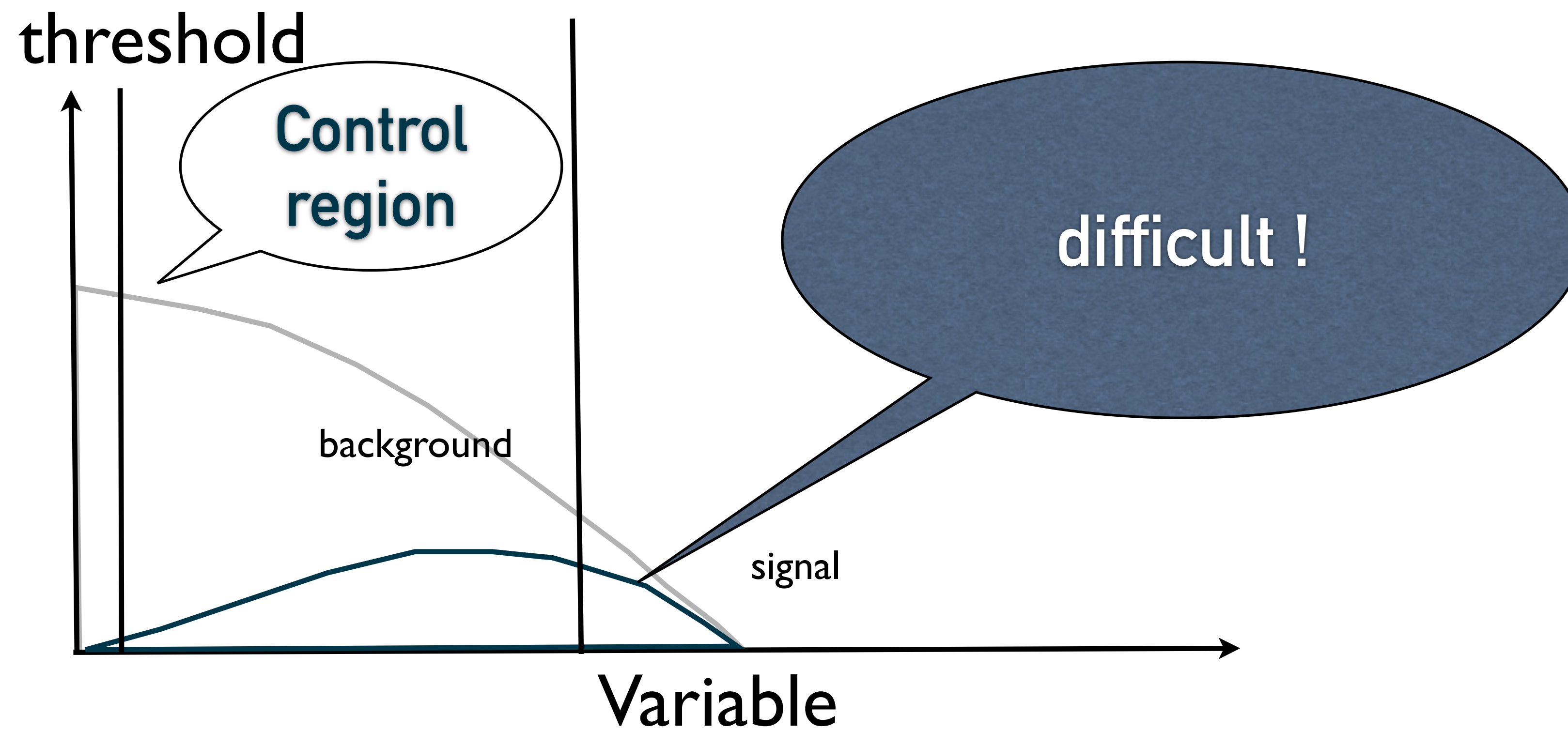
Define variables which can discriminate signal and background

Typical variable for SUSY : missing transverse energy, effective mass



Signal vs Background : Cuts

It is not always possible to construct observables which can easily discriminate signal from backgrounds



SUSY search: Multi-jet + MET

ATLAS-CONF-2017-022

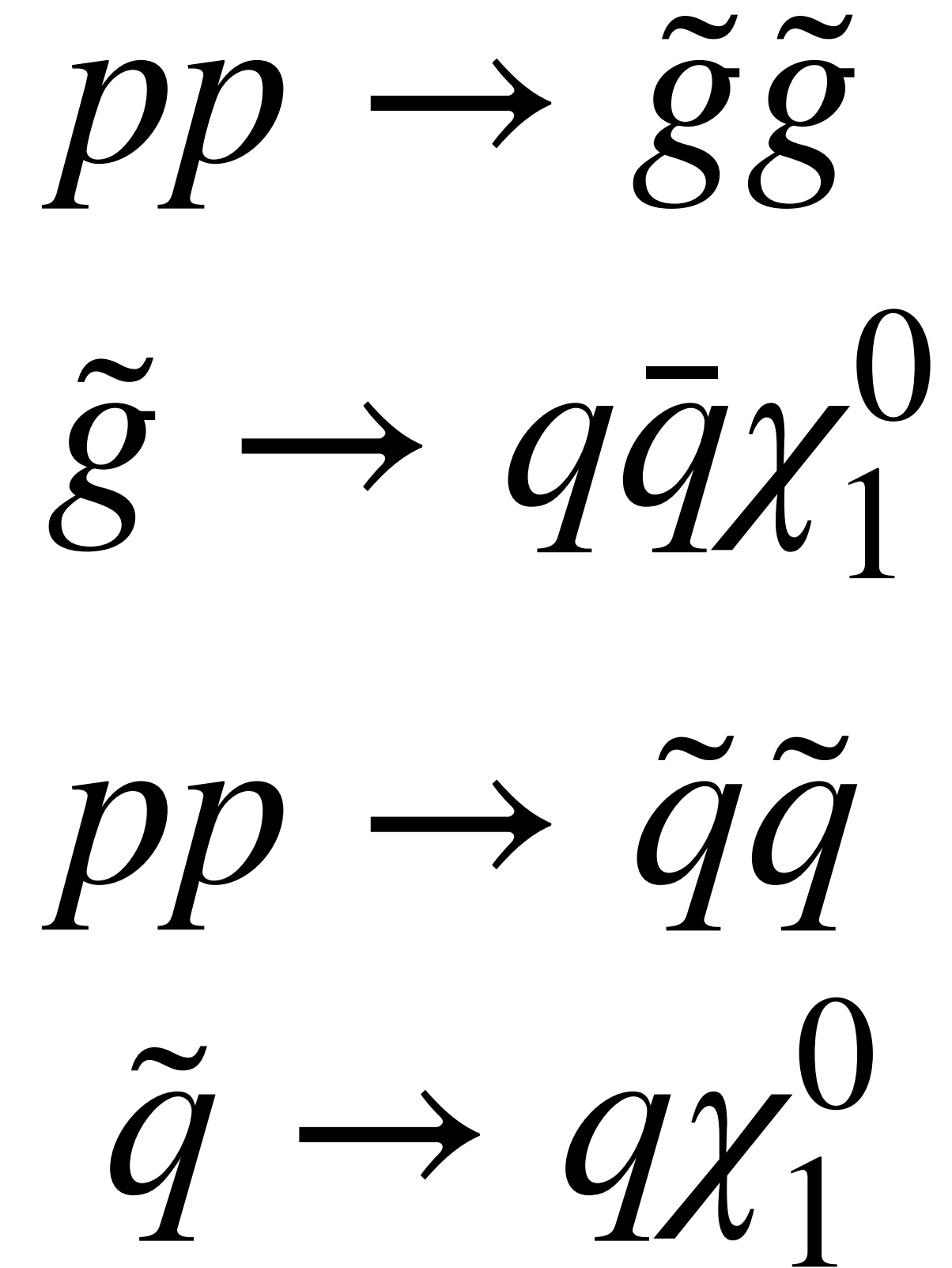
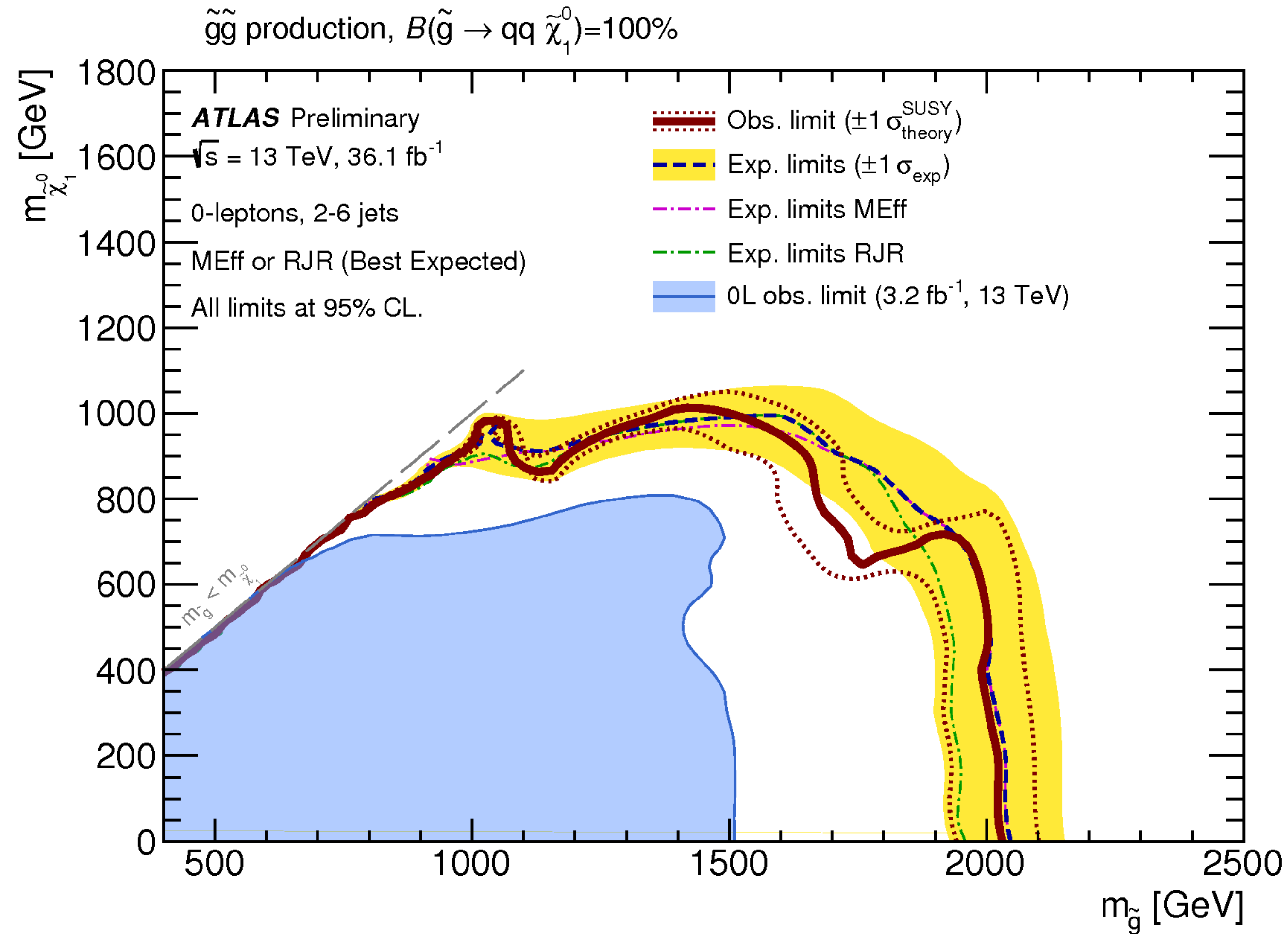
Not the most updated one

Targeted signal	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$						
Requirement	Signal Region [M _{eff} -]						
	4j-1000	4j-1400	4j-1800	4j-2200	4j-2600	4j-3000	5j-1700
E_T^{miss} [GeV] >	250						
$p_T(j_1)$ [GeV] >	200						700
$p_T(j_4)$ [GeV] >	100				150		50
$p_T(j_5)$ [GeV] >	–						50
$ \eta(j_{1,2,3,4}) <$	1.2	2.0					–
$\Delta\phi(\text{jet}_{1,2,(3)}, \vec{E}_T^{\text{miss}})_{\text{min}} >$	0.4						
$\Delta\phi(\text{jet}_{i>3}, \vec{E}_T^{\text{miss}})_{\text{min}} >$	0.4						0.2
$E_T^{\text{miss}}/m_{\text{eff}}(N_j) >$	0.3	0.25			0.2		0.3
Aplanarity >	0.04						–
$m_{\text{eff}}(\text{incl.})$ [GeV] >	1000	1400	1800	2200	2600	3000	1700

also see <http://slac.stanford.edu/pubs/slacreports/reports19/slac-r-504.pdf>

SUSY search: Multi-jet + MET

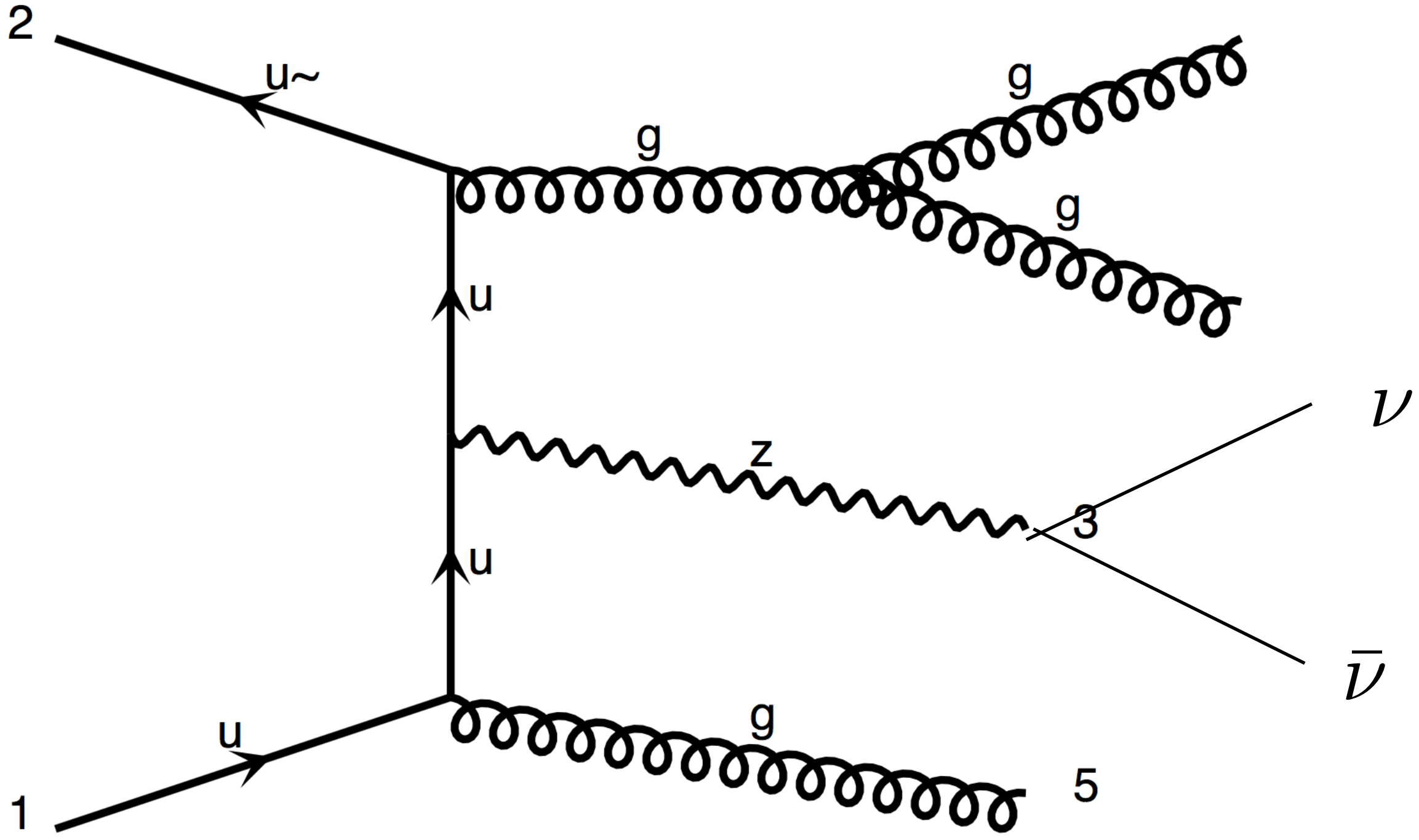
ATLAS-CONF-2017-022



Final state : *Multiple jets + MET*

SM backgrounds

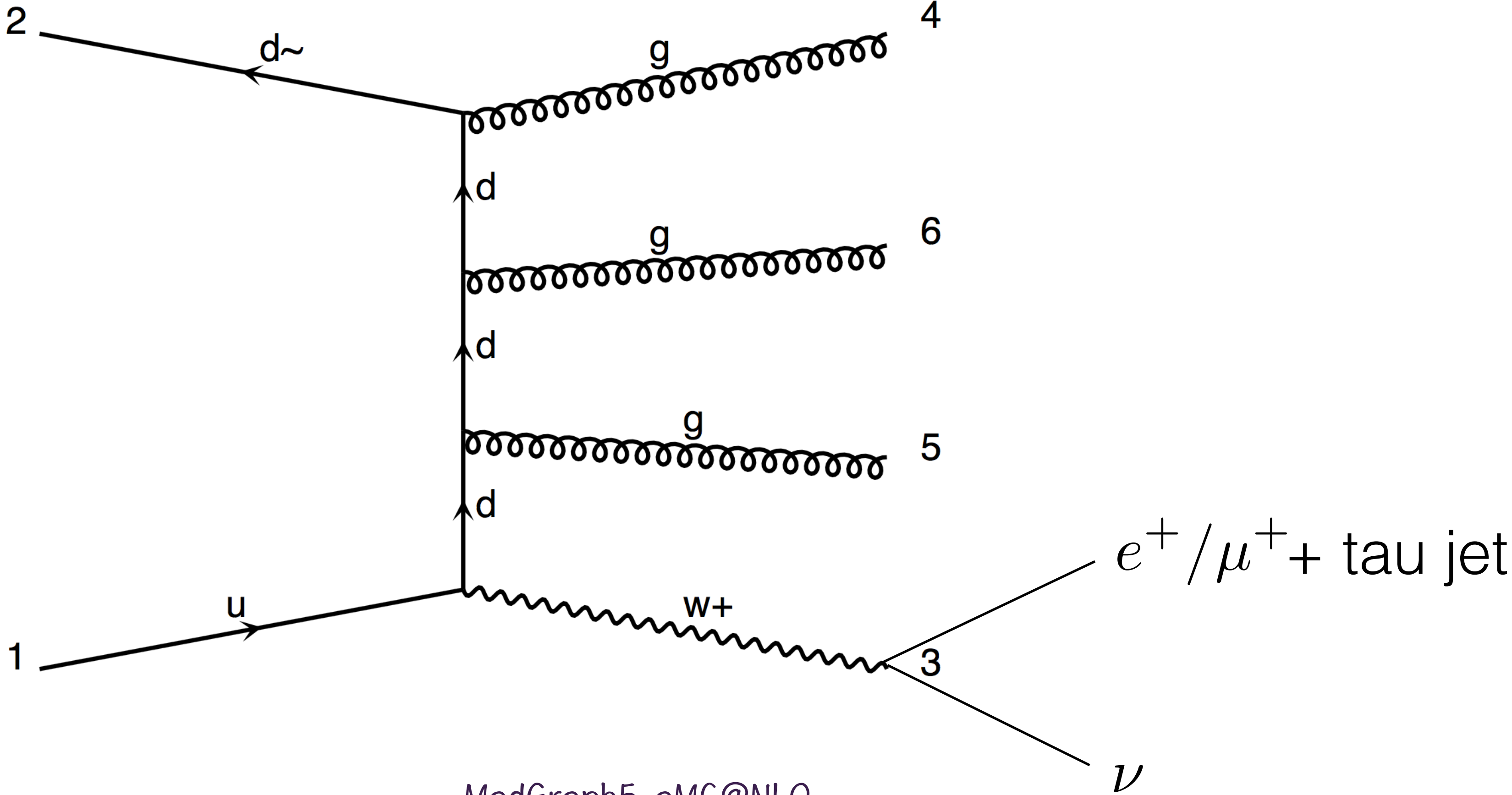
Z + jets



MadGraph5_aMC@NLO

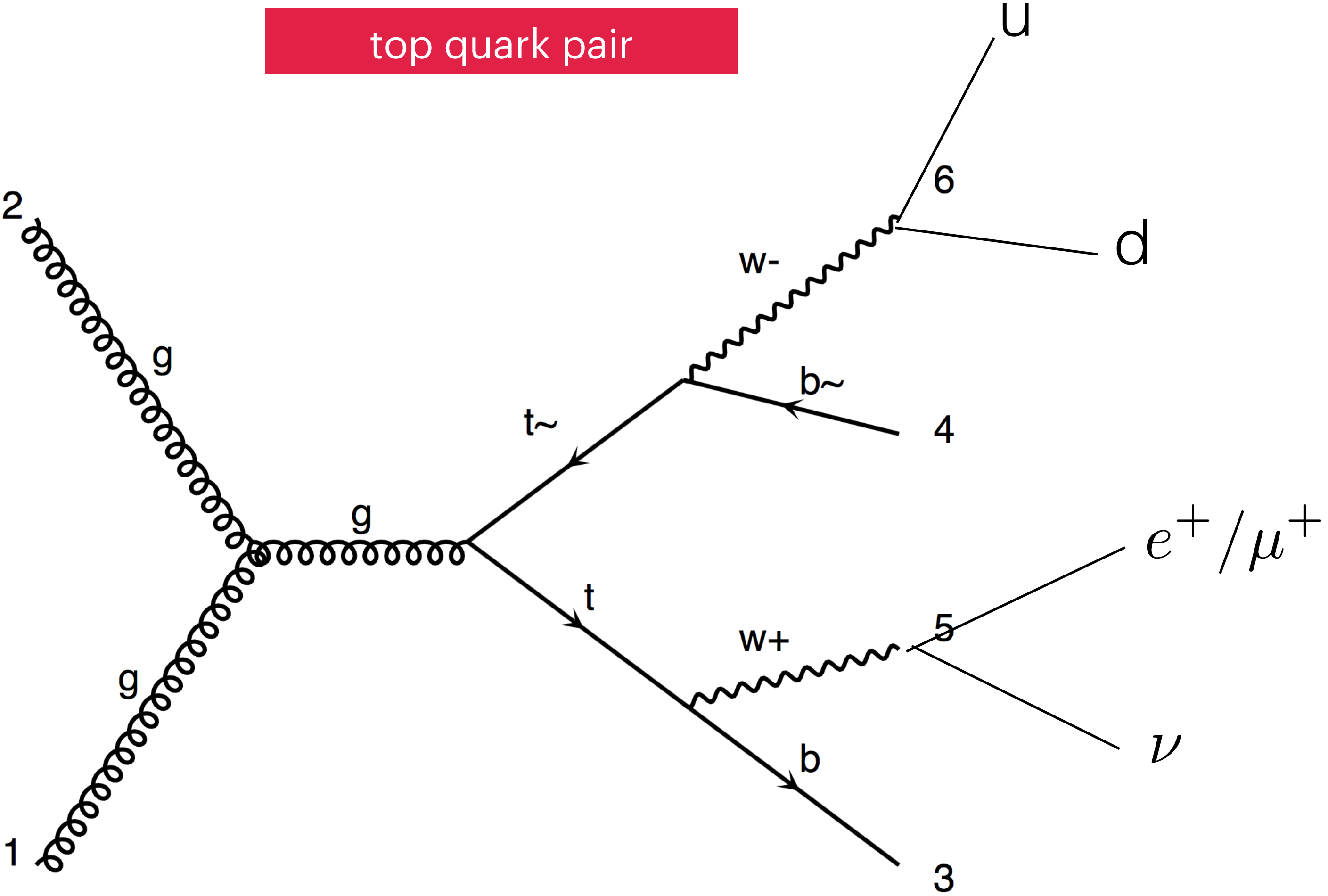
SM backgrounds

W + jets



MadGraph5_aMC@NLO

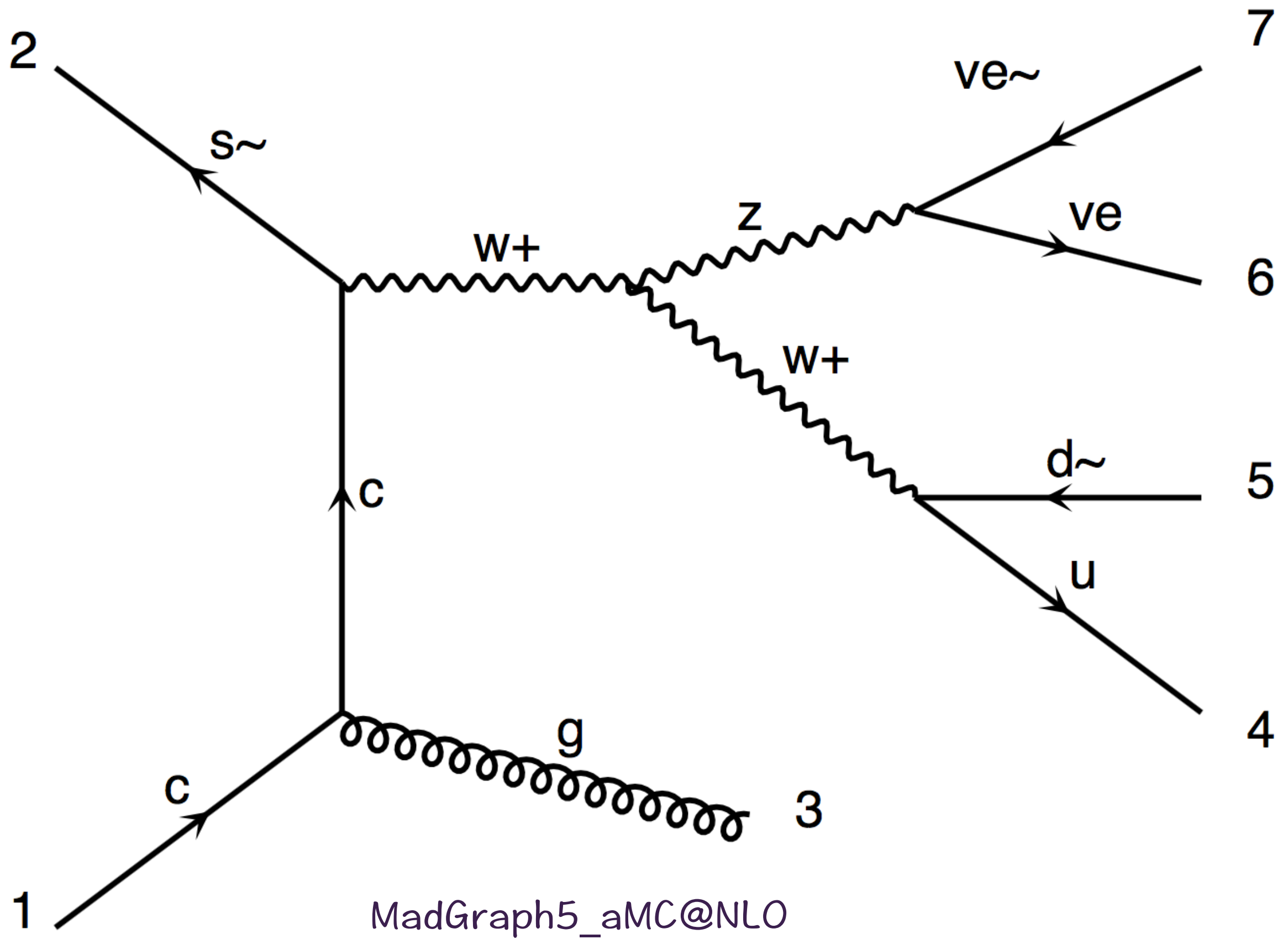
SM backgrounds



top quark pair

SM backgrounds

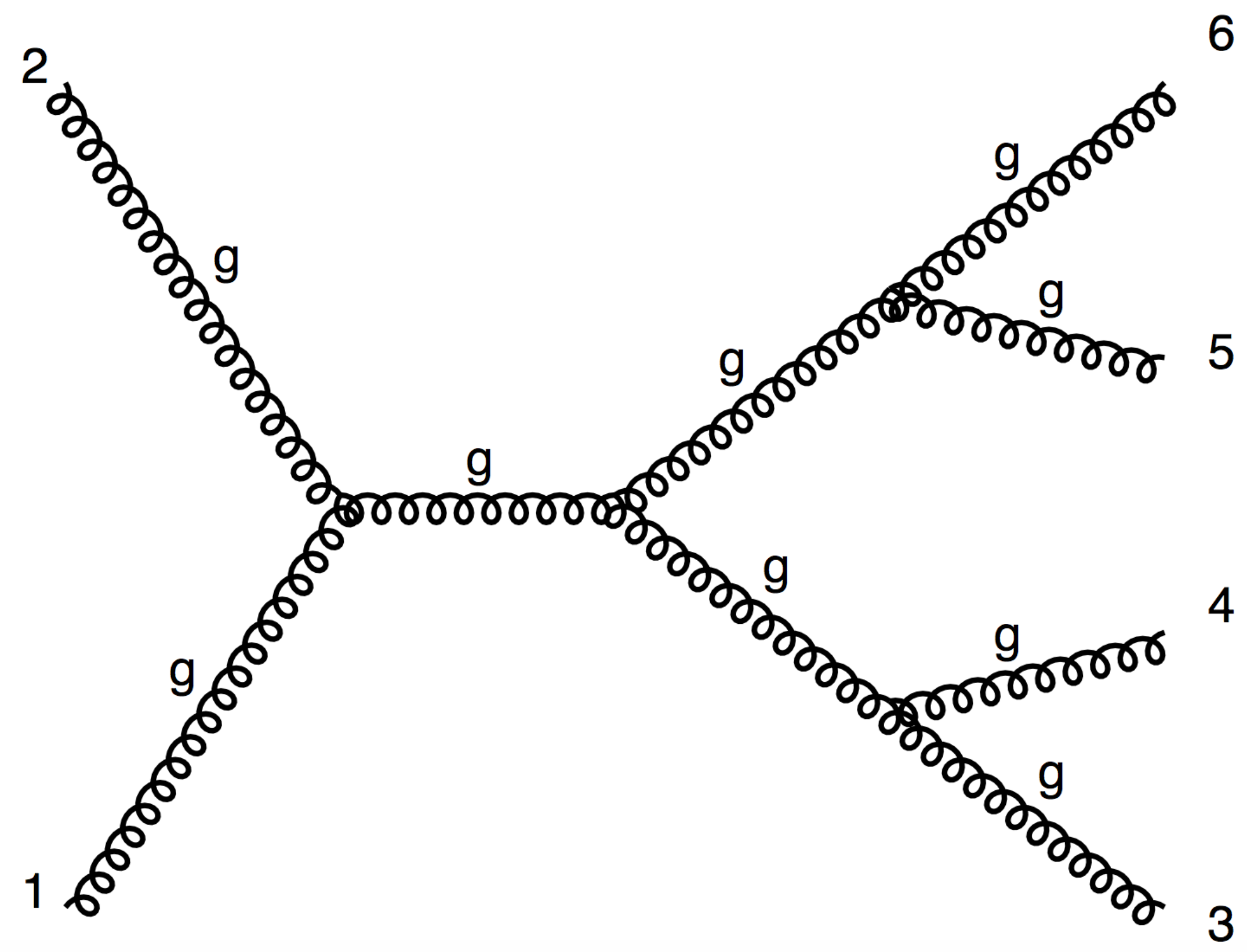
Other subdominant backgrounds VV + jets , single top



MadGraph5_aMC@NLO

SM backgrounds

QCD Multi-jet background



MadGraph5_aMC@NLO

Simple Illustration

$$pp \rightarrow \tilde{q}\tilde{q}$$

$$\tilde{q} \rightarrow q\chi_1^0$$

squark pair production (Mass = 1 TeV) using Pythia-6

squark to quark + neutralino (mass = 100 GeV)

Delphes 3 simulation

backgrounds: Z+ 2 jets , QCD dijet

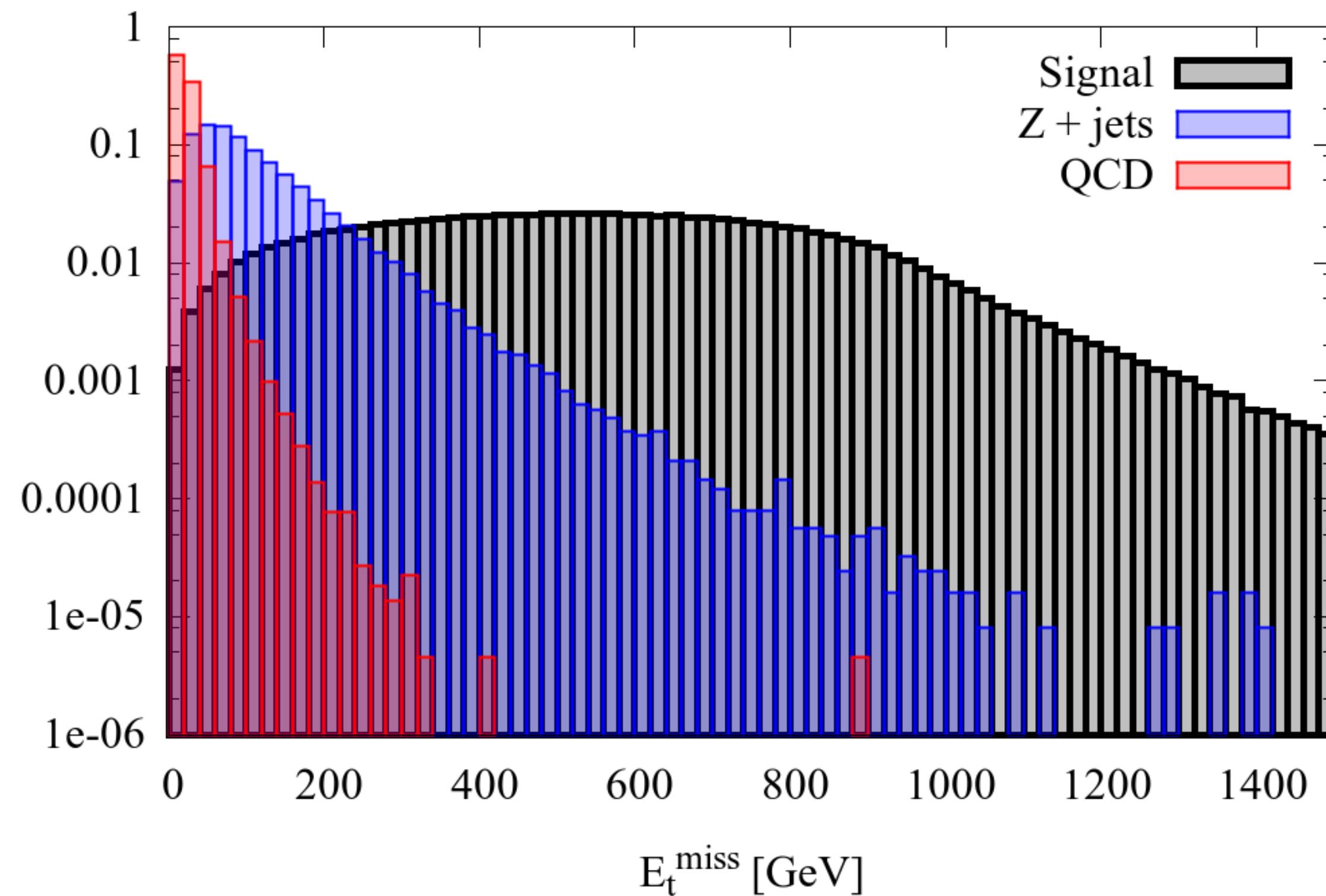
(This is only for illustration)

$$p_T^{j_1} \geq 100 \text{ GeV} \quad p_T^{j_2} \geq 100 \text{ GeV}$$

MET distribution

squark pair production (Mass = 1 TeV) using Pythia-6
squark to quark + neutralino (mass = 100 GeV)
Delphes 3 simulation

$$p_T^{j1} \geq 100 \text{ GeV} \quad p_T^{j2} \geq 100 \text{ GeV}$$



SM cross sections (background)

QCD($p_T > 100$ GeV) ~ 2000000 pb
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SUSY cross sections (signal)

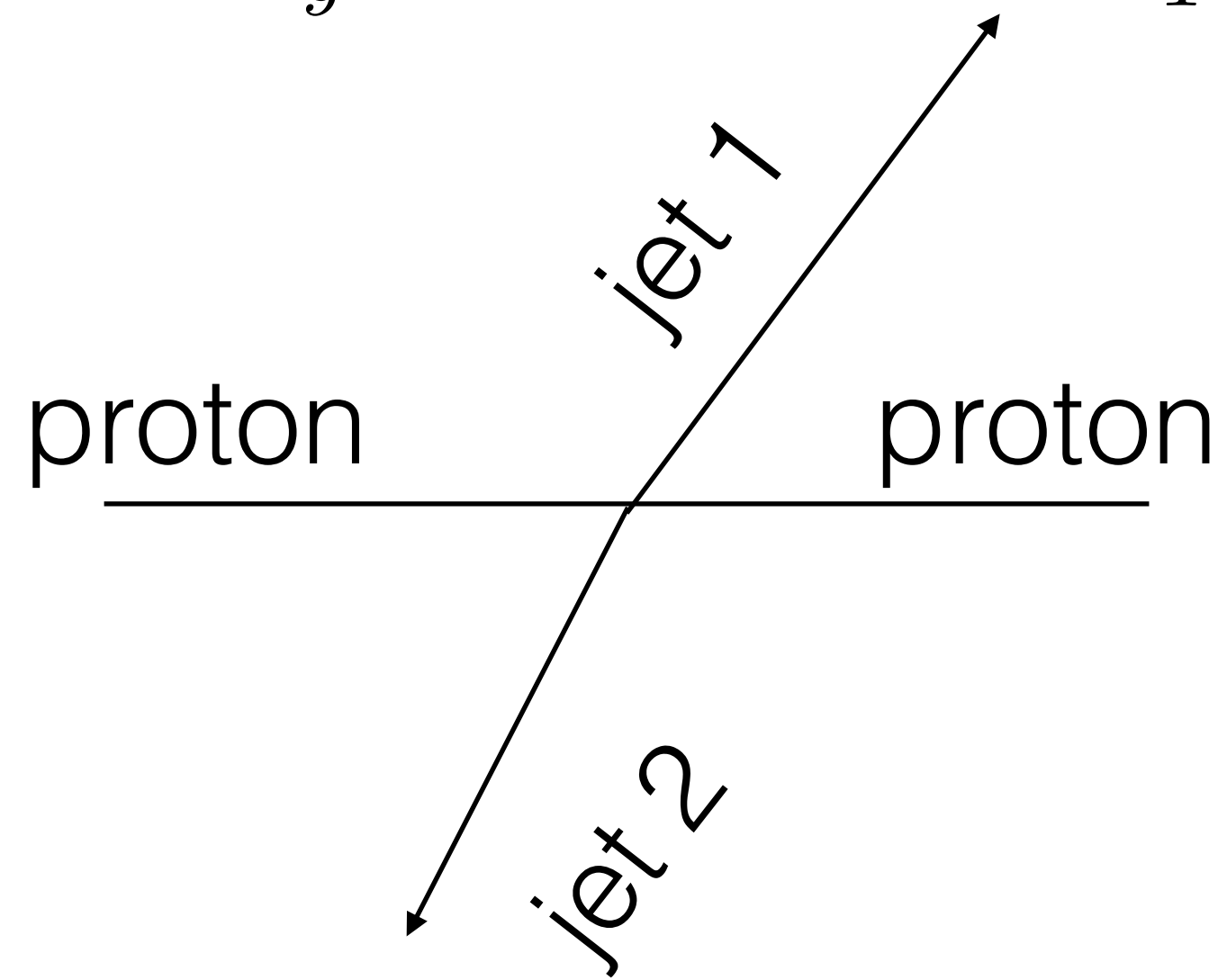
Gluino pair (mass = 1 TeV)
 ~ 450 fb
stop pair (mass = 1 TeV)
 ~ 10 fb

Plot Credit : Rahool Kumar Barman

MET from QCD

ideal situation

$$p_x^{j_1} = 562 \text{ GeV}, \quad p_y^{j_1} = 195 \text{ GeV}, \quad p_T^{j_1} \sim 595 \text{ GeV}$$



$$p_x^{j_2} = -564 \text{ GeV}, \quad p_y^{j_2} = -193 \text{ GeV}, \quad p_T^{j_2} \sim 596 \text{ GeV}$$

$$p_x^{visible} = p_x^{j_1} + p_x^{j_2} = 562 - 564 = -2 \text{ GeV}$$

$$p_y^{visible} = p_y^{j_1} + p_y^{j_2} = 195 - 193 = -2 \text{ GeV}$$

$$p_y^{missing} = - p_y^{visible}$$

$$p_x^{missing} = - p_x^{visible}$$

$$p_T^{missing} = \sqrt{(p_x^{missing})^2 + (p_y^{missing})^2} \sim 3 \text{ GeV}$$

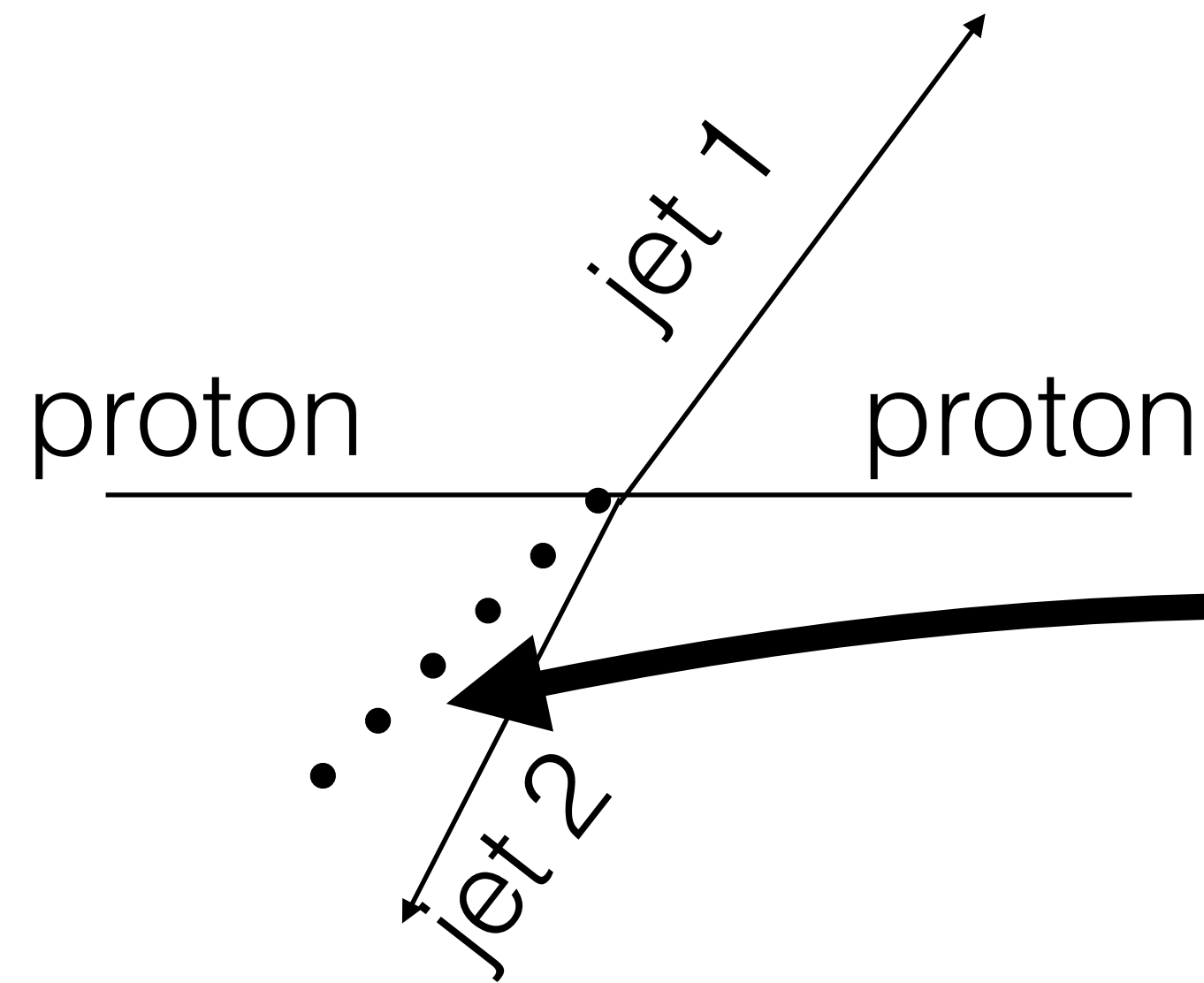
perfectly balanced di-jet

MET ~ 0 GeV

MET from QCD

real example

$$p_x^{j_1} = 562 \text{ GeV}, \quad p_y^{j_1} = 195 \text{ GeV}, \quad p_T^{j_1} \sim 595 \text{ GeV}$$



$$p_y^{missing} = - p_y^{visible}$$

$$p_x^{missing} = - p_x^{visible}$$

$$p_x^{missing} = -212 \text{ GeV}$$

$$p_y^{missing} = 55 \text{ GeV}$$

$$p_T^{missing} = 219 \text{ GeV}$$

$$p_x^{j_2} = -350 \text{ GeV}, \quad p_y^{j_2} = -250 \text{ GeV}$$

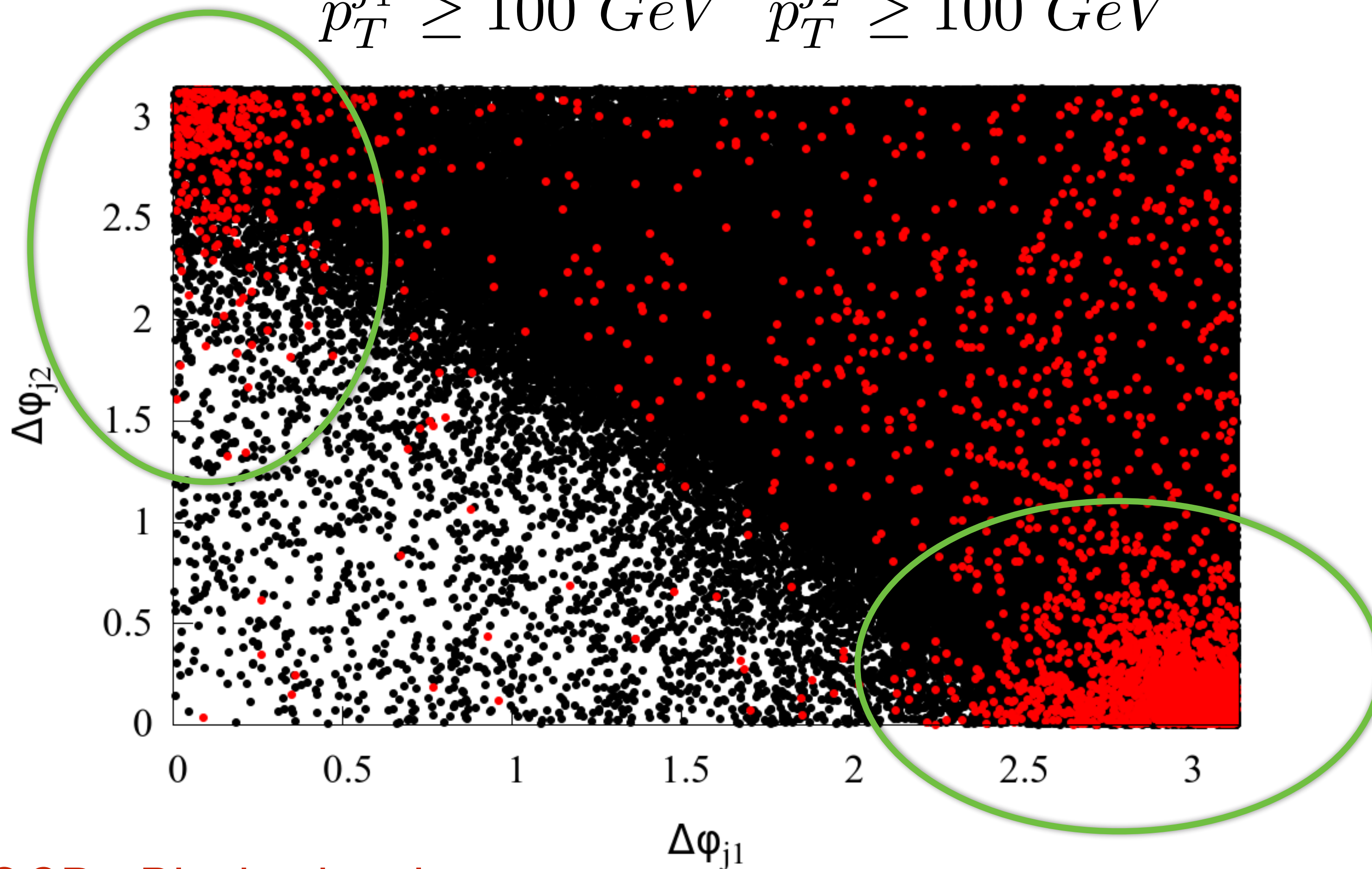
jet 2 is badly mis-measured

mis-measured di-jet (multi-jet)
large MET is not impossible

$\Delta\phi$ Cut

squark pair production (Mass = 1 TeV) using Pythia-6
squark to quark + neutralino (mass = 100 GeV)
Delphes 3 simulation

$$p_T^{j_1} \geq 100 \text{ GeV} \quad p_T^{j_2} \geq 100 \text{ GeV}$$

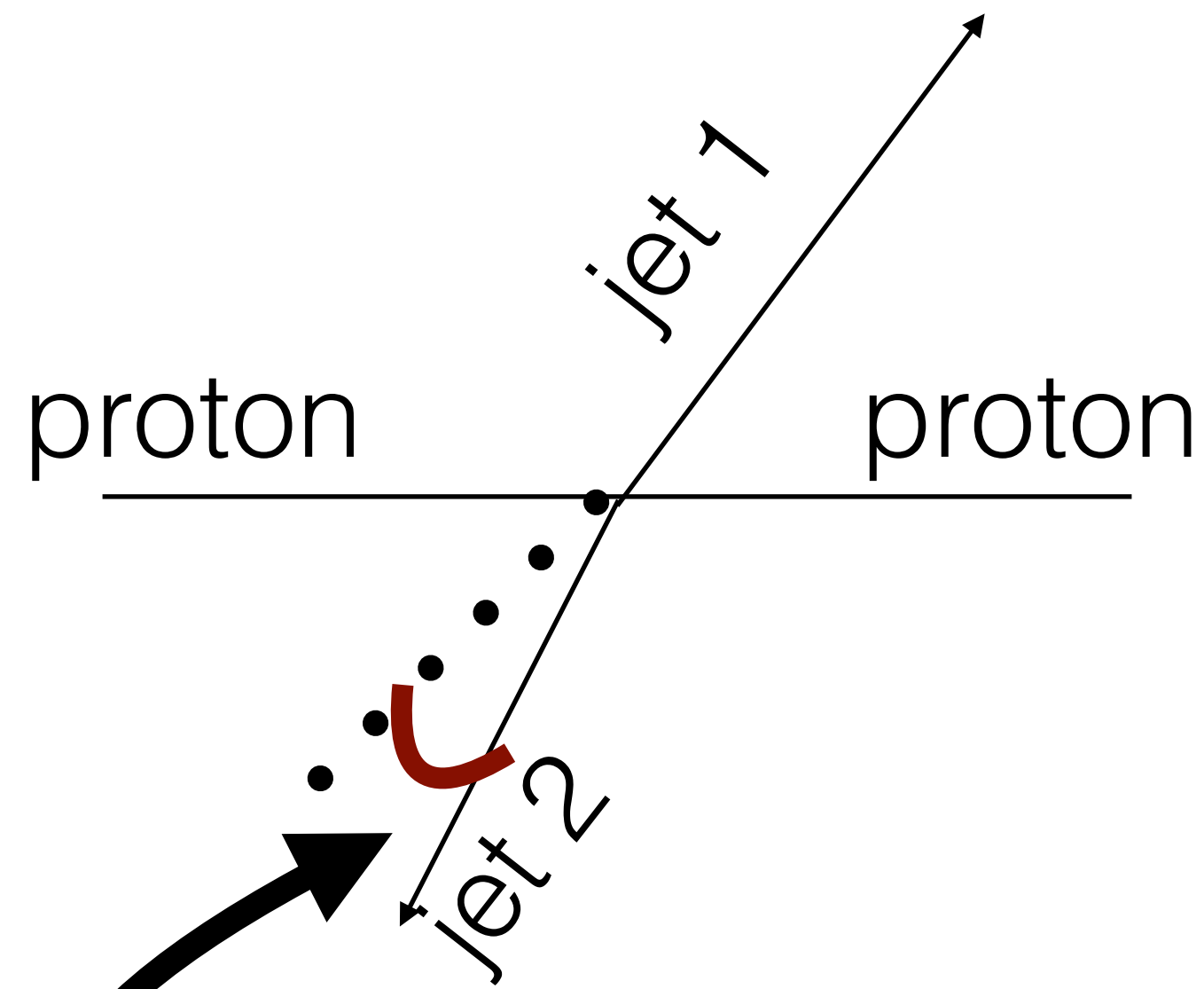


Red : QCD , Black: signal

Plot Credit : Rahoo Kumar Barman

MET from QCD

$$p_x^{j_1} = 562 \text{ GeV}, \quad p_y^{j_1} = 195 \text{ GeV}, \quad p_T^{j_1} \sim 595 \text{ GeV}$$



$$p_x^{j_2} = -350 \text{ GeV}, \quad p_y^{j_2} = -250 \text{ GeV}$$

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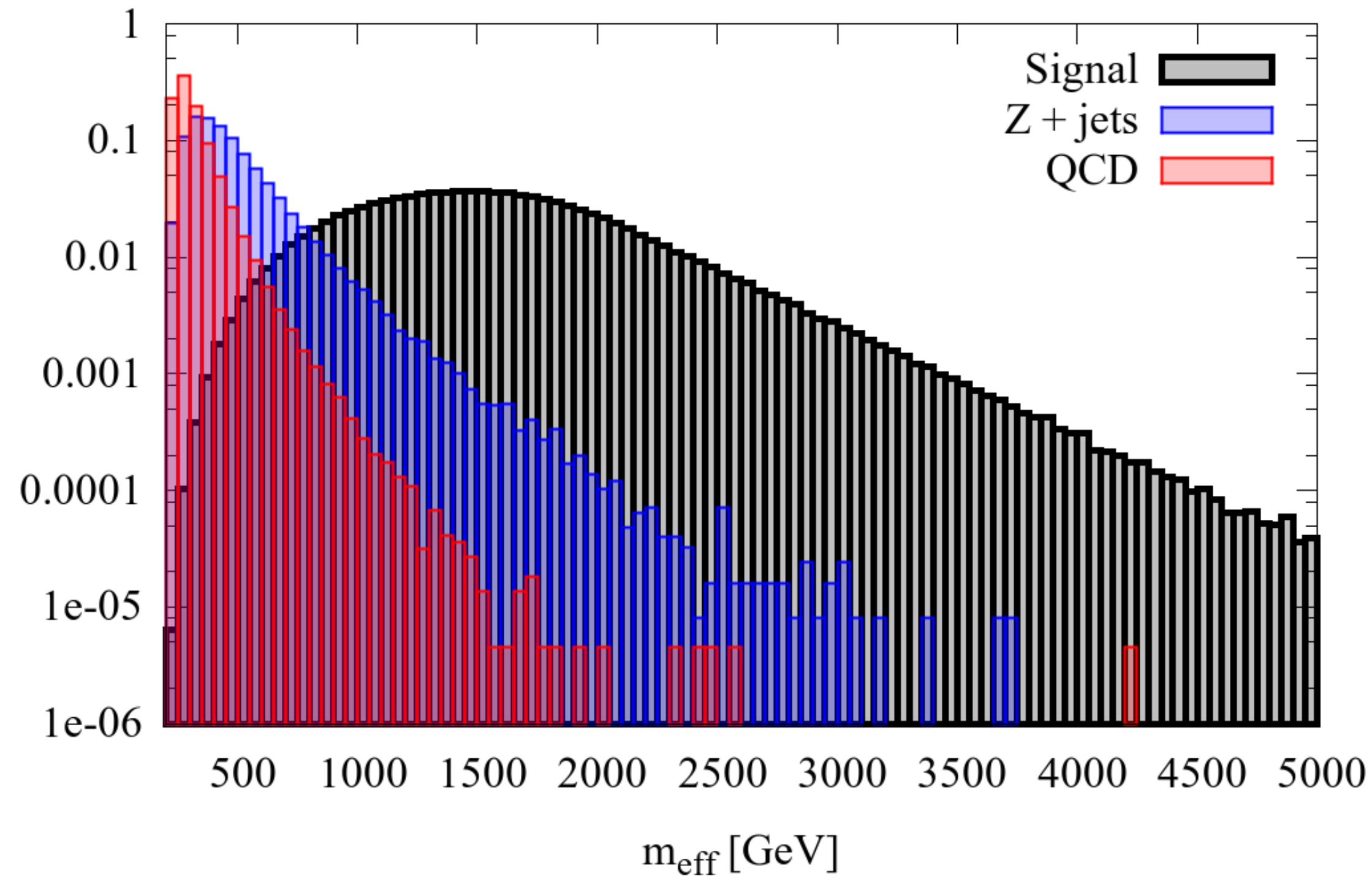
$$p_T^{missing} = 219 \text{ GeV}$$

(the angle between jet 2 and MET is small)

Effective Mass

squark pair production (Mass = 1 TeV) using Pythia-6
squark to quark + neutralino (mass = 100 GeV)
Delphes 3 simulation

$$p_T^{j_1} \geq 100 \text{ GeV} \quad p_T^{j_2} \geq 100 \text{ GeV}$$



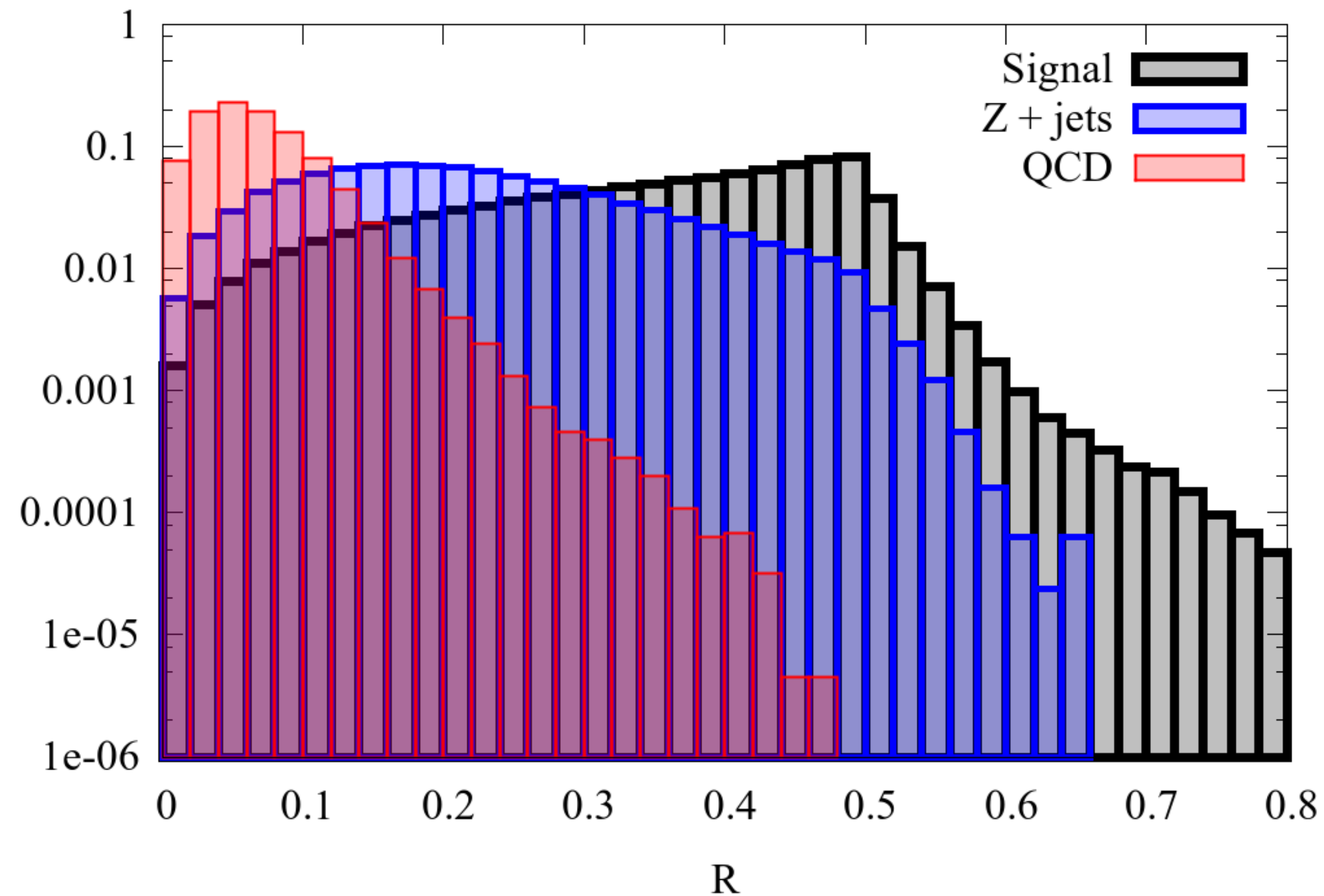
$$m_{\text{eff}} = \sum p_T^{\text{jets}} + p_T^{\text{mis}}$$

Plot Credit : Rahoo Kumar Barman

MET/ Effective Mass Cut

squark pair production (Mass = 1 TeV) using Pythia-6
squark to quark + neutralino (mass = 100 GeV)
Delphes 3 simulation

$$p_T^{j_1} \geq 100 \text{ GeV} \quad p_T^{j_2} \geq 100 \text{ GeV}$$



Plot Credit : Rahool Kumar Barman

Results

Signal Region [M _{eff} -]	2j-1200	2j-1600	2j-2000	2j-2400	2j-2800
MC expected events					
Diboson	28.17	14.37	7.02	3.09	0.86
Z/γ* +jets	346.37	140.61	54.13	24.23	10.22
W+jets	142.39	47.49	18.33	8.23	3.37
t \bar{t} (+EW) + single top	21.40	5.84	2.54	1.13	0.32
Fitted background events					
Diboson	28 ± 4	14.4 ± 2.3	7.0 ± 1.1	3.1 ± 0.5	0.86 ± 0.17
Z/γ* +jets	337 ± 19	141 ± 10	61 ± 8	26.8 ± 3.1	11.4 ± 1.4
W+jets	136 ± 24	57 ± 16	19 ± 5	9.4 ± 2.6	3.1 ± 1.1
t \bar{t} (+EW) + single top	15 ± 4	3.1 ± 1.7	1.34 ± 1.0	0.4 ± 0.4	0.18 ± 0.15
Multi-jet	1.8 ± 1.8	0.34 ± 0.34	–	–	–
Total bkg	517 ± 31	216 ± 18	88 ± 9	40 ± 4	15.5 ± 1.9
Observed	582	204	70	33	17
$\langle \epsilon\sigma \rangle_{\text{obs}}^{95}$ [fb]	3.6	1.00	0.42	0.30	0.32
S_{obs}^{95}	131	36	15	11	11
S_{exp}^{95}	78 ⁺³³ ₋₂₁	43 ⁺¹⁷ ₋₁₂	24 ⁺¹⁰ ₋₆	15 ⁺⁷ ₋₄	10 ⁺⁴ ₋₃
p_0 (Z)	0.06 (1.53)	0.50 (0.00)	0.50 (0.00)	0.50 (0.00)	0.33 (0.43)

Transverse Mass

$$A \rightarrow B + X \text{ (inv)}$$

$$M_A^2 = M_B^2 + M_X^2 + 2(E_T^B E_T^X \cosh(\Delta\eta_{BX}) - \mathbf{p}_T^B \cdot \mathbf{p}_T^X)$$

$$\cosh(x) \geq 1 \qquad E_T = \sqrt{p_T^2 + m^2}$$

$$M_T^2 = M_B^2 + M_X^2 + 2(E_T^B E_T^X - \mathbf{p}_T^B \cdot \mathbf{p}_T^X)$$

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$$M_T^2 = M_B^2 + M_X^2 + 2(E_T^B E_T^X - \mathbf{p}_T^B \cdot \mathbf{p}_T^X) \qquad M_A^2 \geq M_T^2$$

Suppose B and X are massless

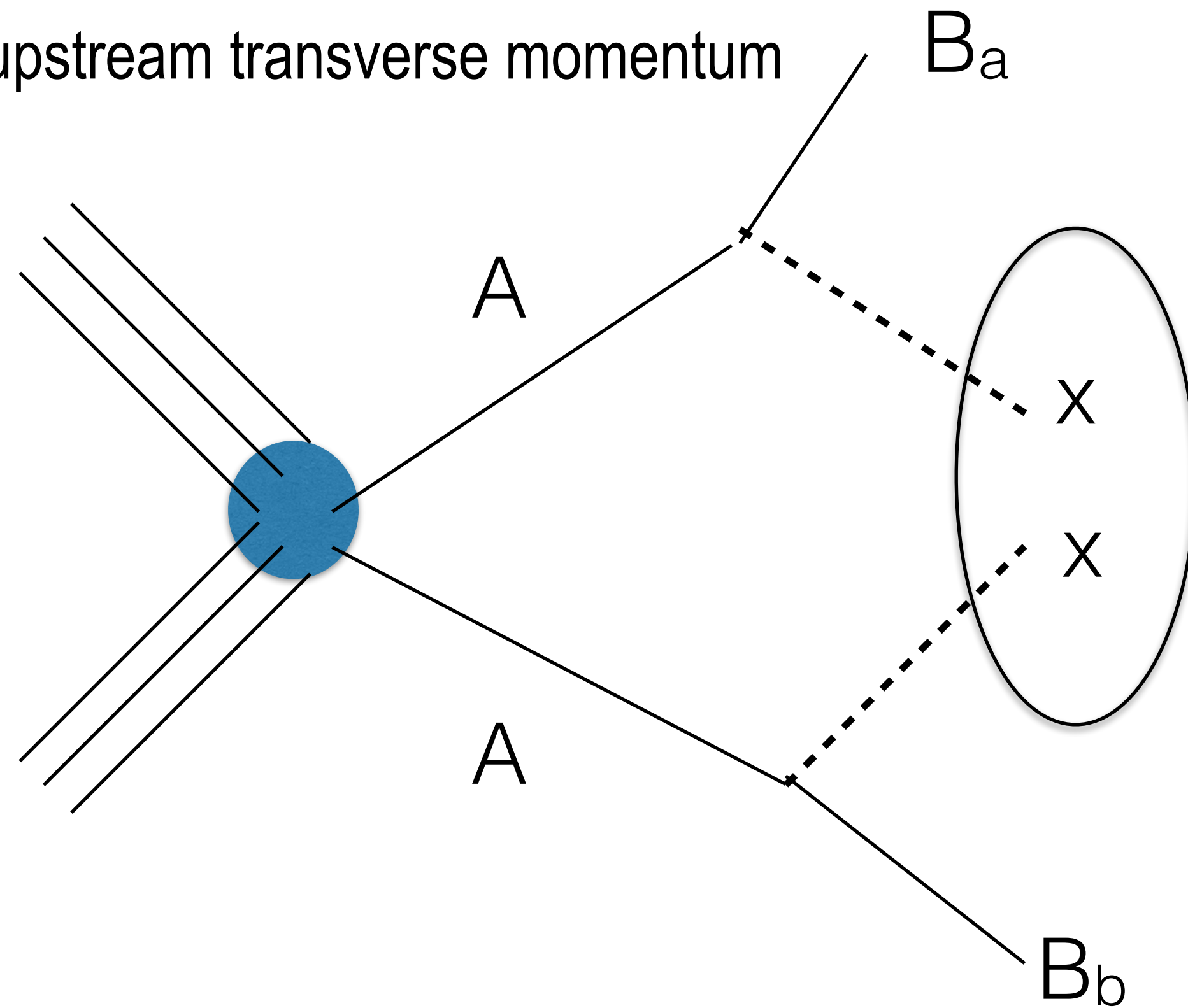
Suppose B and X are massless

$$M_T^2 = 2E_T^B E_T^X (1 - \cos \phi)$$

Discovery of W boson in lepton + MET channel : Transverse Mass variable used

Stransverse Mass

No ISR and upstream transverse momentum



Two invisible particles
 x particle coming from A $\Rightarrow x_a$
 x particle coming from B $\Rightarrow x_b$

The vector sum will give MET

Split the missing transverse energy into two parts

$$p_T^{mis} = p_T^{x_a} + p_T^{x_b}$$

Assume the mass of the invisible particle and calculate

$$M_T(x_a, B_a) \text{ and } M_T(x_b, B_b)$$

Take the Max of $M_T(x_a, B_a)$ and $M_T(x_b, B_b)$

Now vary the MET splitting* which minimises the $\text{Max}(M_T(x_a, B_a), M_T(x_b, B_b))$

$$M_{T2} = \min_{p_T^{mis} = p_T^{x_a} + p_T^{x_b}} [\text{Max}(M_T(x_a, B_a), M_T(x_b, B_b))]$$

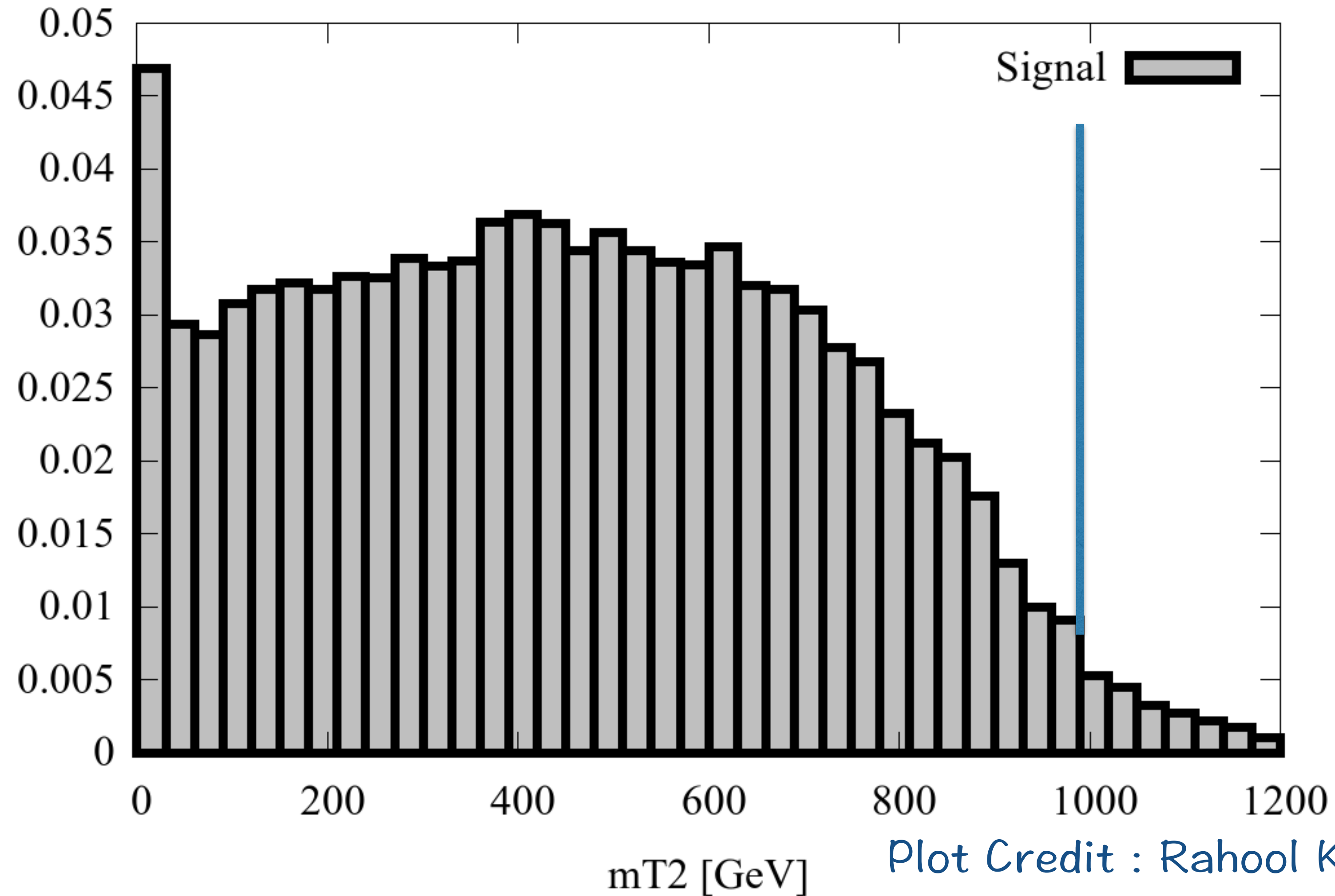
MT2 Variable

squark pair production (Mass = 1 TeV) using Pythia-6

squark to quark + neutralino (mass = 100 GeV)

Delphes 3 simulation

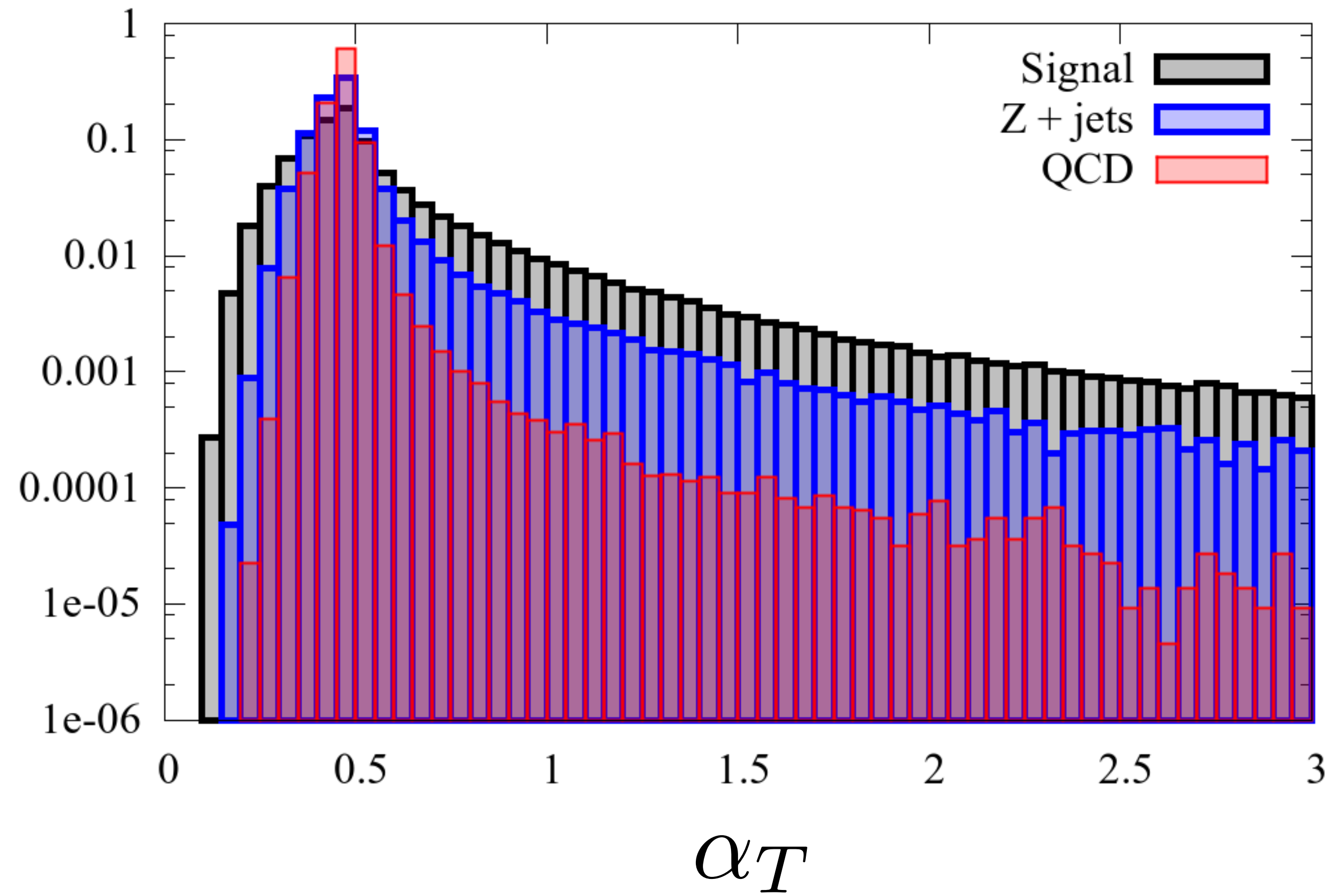
(naively written code for MT2, slight discrepancy in result when compared with the public code)



Plot Credit : Rahoo Kumar Barman

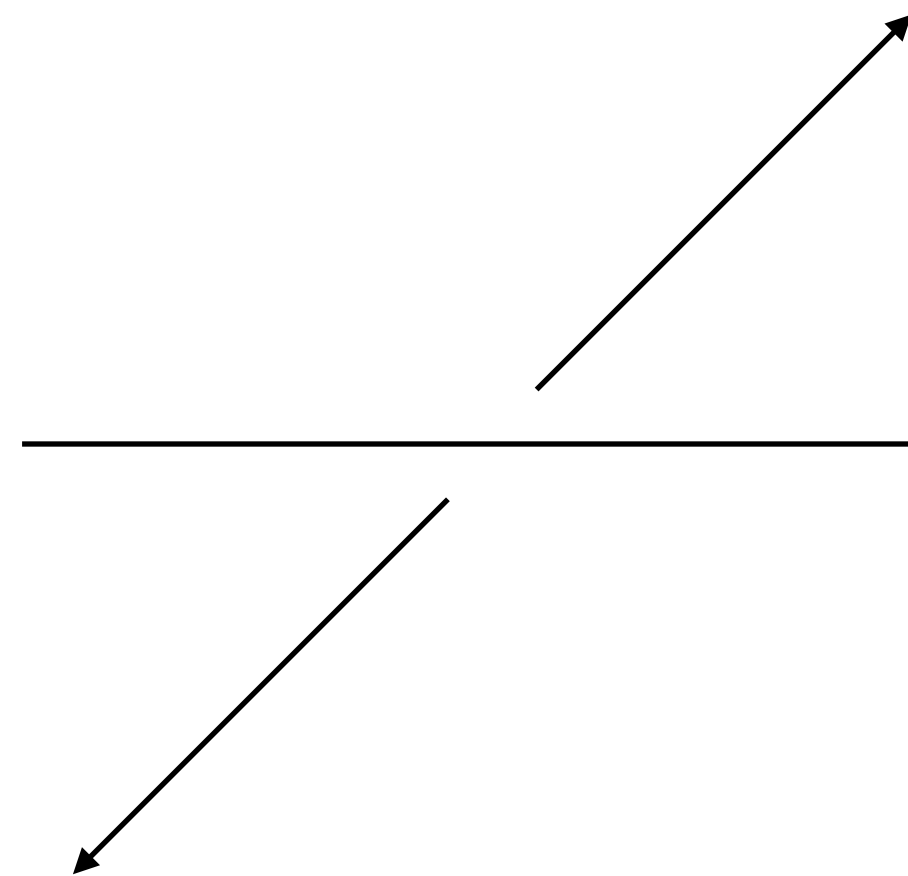
α_T Variable

$$\alpha_T = \frac{p_T^{j_2}}{M_T^{j_1 j_2}}$$



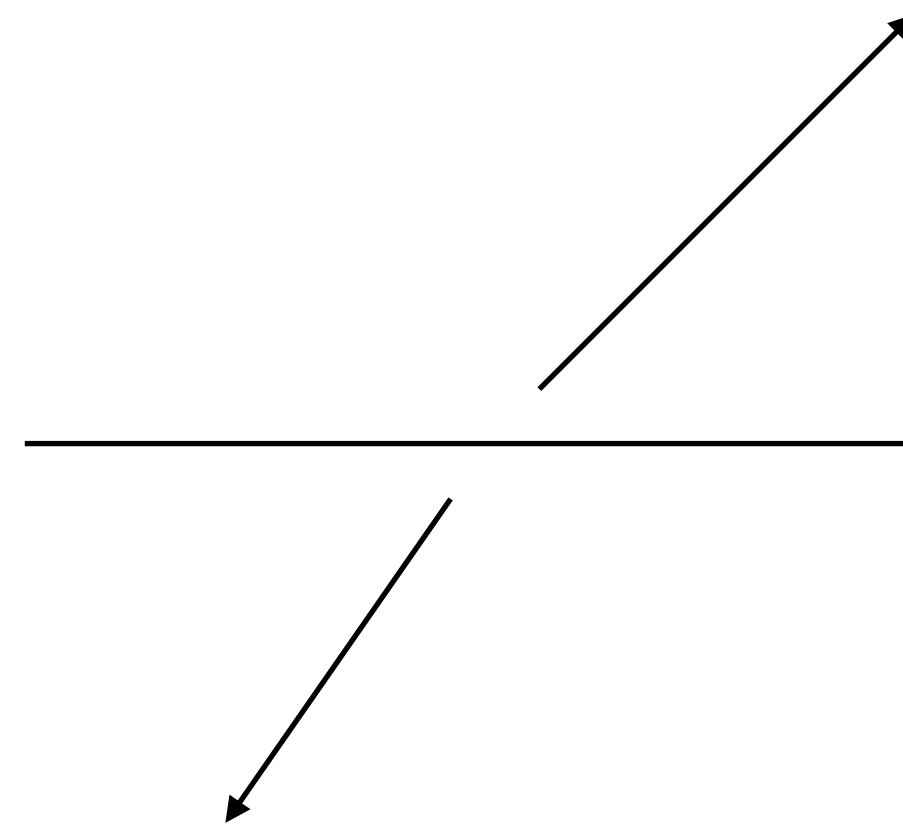
α_T Variable

$$\alpha_T = \frac{p_T^{j_2}}{M_T^{j_1 j_2}} = \sqrt{\frac{p_T^{j_2}}{p_T^{j_1}}} \frac{1}{\sqrt{2(1 - \cos \Delta\phi)}}$$



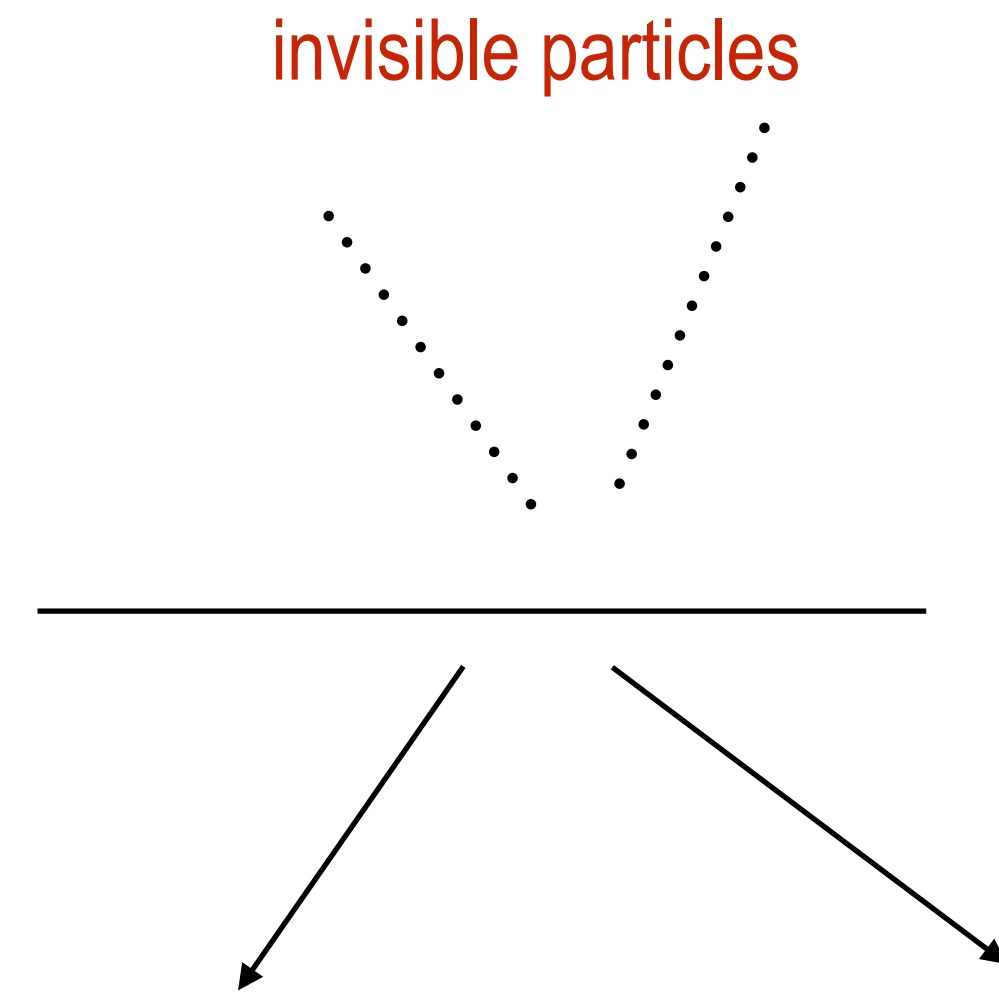
well balanced di-jet system

$$\begin{aligned}\Delta\phi &= \pi \\ p_T^{j_2} &= p_T^{j_1} \\ \alpha_T &= 0.5\end{aligned}$$



one jet mismeasured

$$\alpha_T < 0.5$$



SUSY SIGNAL
(rare configuration for QCD)

$$\alpha_T > 0.5$$

Pile up

Luminosity

Colliding beams



The number of events per second $= \frac{dR}{dt} \propto \sigma$
$$\frac{dR}{dt} = \mathcal{L} \sigma$$

\mathcal{L} = luminosity ($cm^{-2} second^{-1}$)

$$1 \text{ cm}^{-2} \text{ s}^{-1} = 10^{-33} \text{ nb}^{-1} \text{ s}^{-1}$$

The proportionality constant is called Luminosity

Luminosity

Colliding beams



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$$\frac{dR}{dt} = \mathcal{L} \sigma$$

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$$1 \text{ cm}^{-2} \text{ s}^{-1} = 10^{-33} \text{ nb}^{-1} \text{ s}^{-1}$$

The proportionality constant is called Luminosity

Consider two gaussian bunches (spread in the x-y plane) containing n_1 and n_2 particles respectively

These collide with frequency f and N_b is the number of bunches in one beam then

$$\mathcal{L} = \frac{N_1 N_2 f N_B}{4\pi\sigma_x\sigma_y}$$

where σ_x and σ_y are the Gaussian horizontal and vertical widths, respectively.

Example : $\sigma_x = \sigma_y = 20\mu m$ $N_B = 2800$ $f = 40MHz$ $N_1 = N_2 = 10^{11}$ $\mathcal{L} \sim 10^{34} cm^{-2} s^{-1}$

Pile up

Each proton bunch contains billions of protons

Consider Instantaneous luminosity $10^{34} \text{cm}^{-2} \text{s}^{-1} = 10^7 \text{mb}^{-1} \text{Hz}$

Proton proton cross section $\sim 100 \text{mb}$ (dominated by inelastic processes)

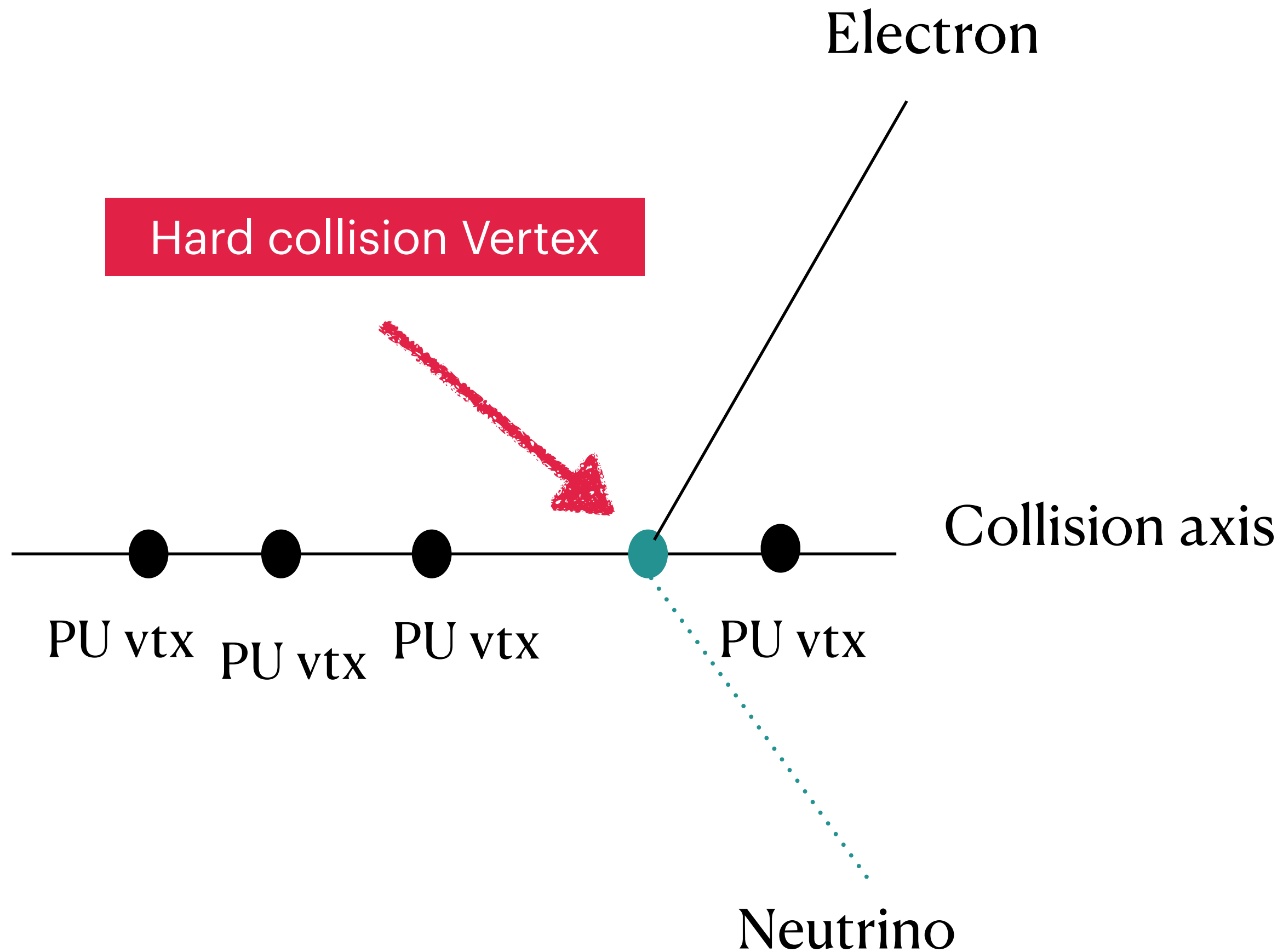
Event rate = $10^7 \text{mb}^{-1} \text{Hz} \times 100 \text{mb} = 10 \times 10^8 \text{Hz}$

Time gap between two bunch crossing = $25 \text{ns} = 25 \times 10^{-9} \text{Hz}^{-1}$

Expected number of event per 25 ns = 25 events

In any bunch crossing we expect about 25 events superimposed on interesting process like Higgs production, top quark , new physics etc. => Pileup

Pile up



Average number of PU vertices at Tevatron ~ 5

Average number of PU vertices at the HL-LHC $\sim 140-200$

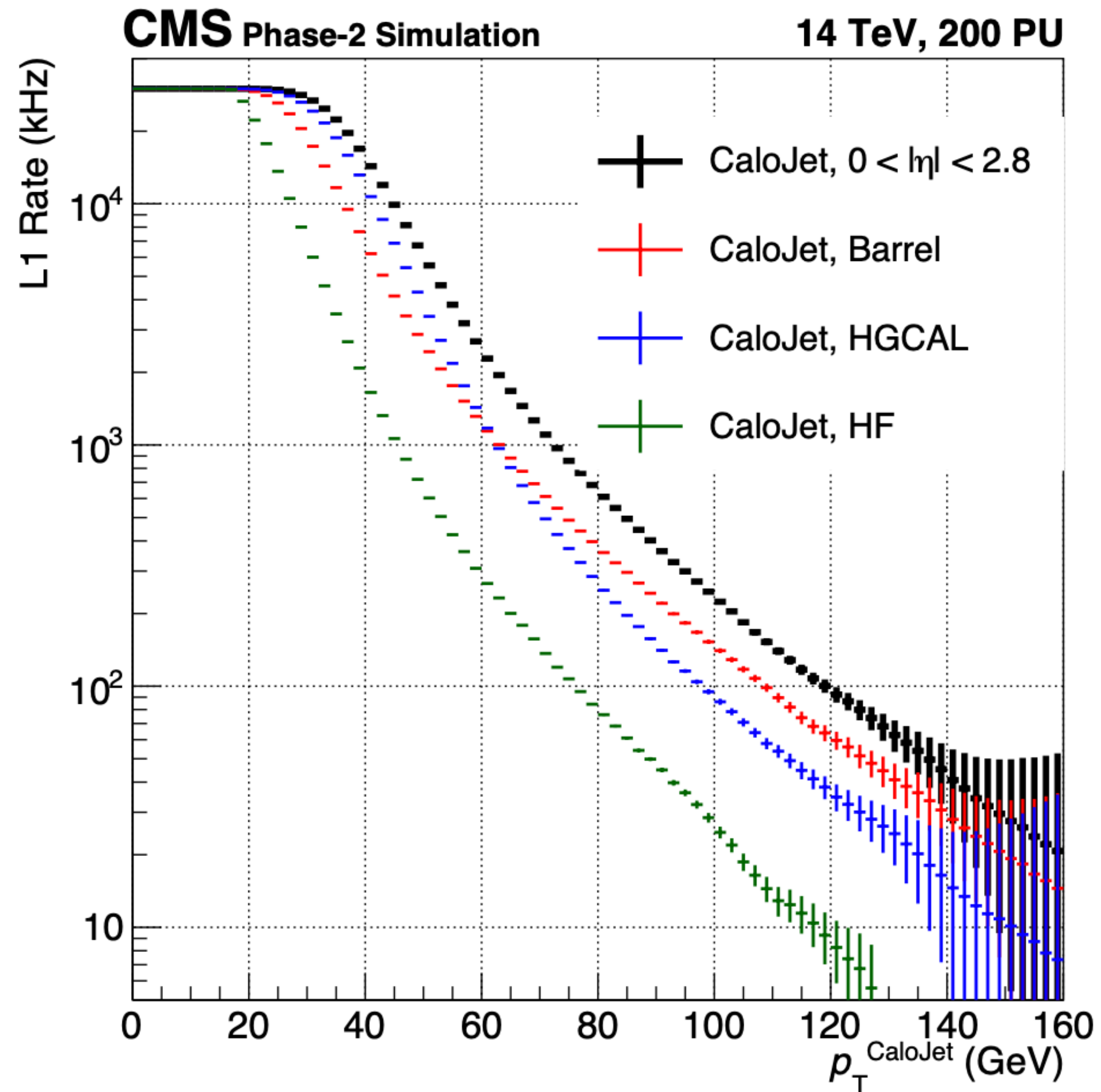
Actual number in a given bunch crossing fluctuates
follows Poisson distribution around its mean value

Each PU vertex generally produce a few tens of soft hadrons
The detected final state particles will be the superposition
Of particles coming from hard process and soft particles
Coming from PU vertices (soft Hadrons)

1 Event takes 1-2 MB of storage : storage required for 10^9 . Events per second = 1000 TB/s !!

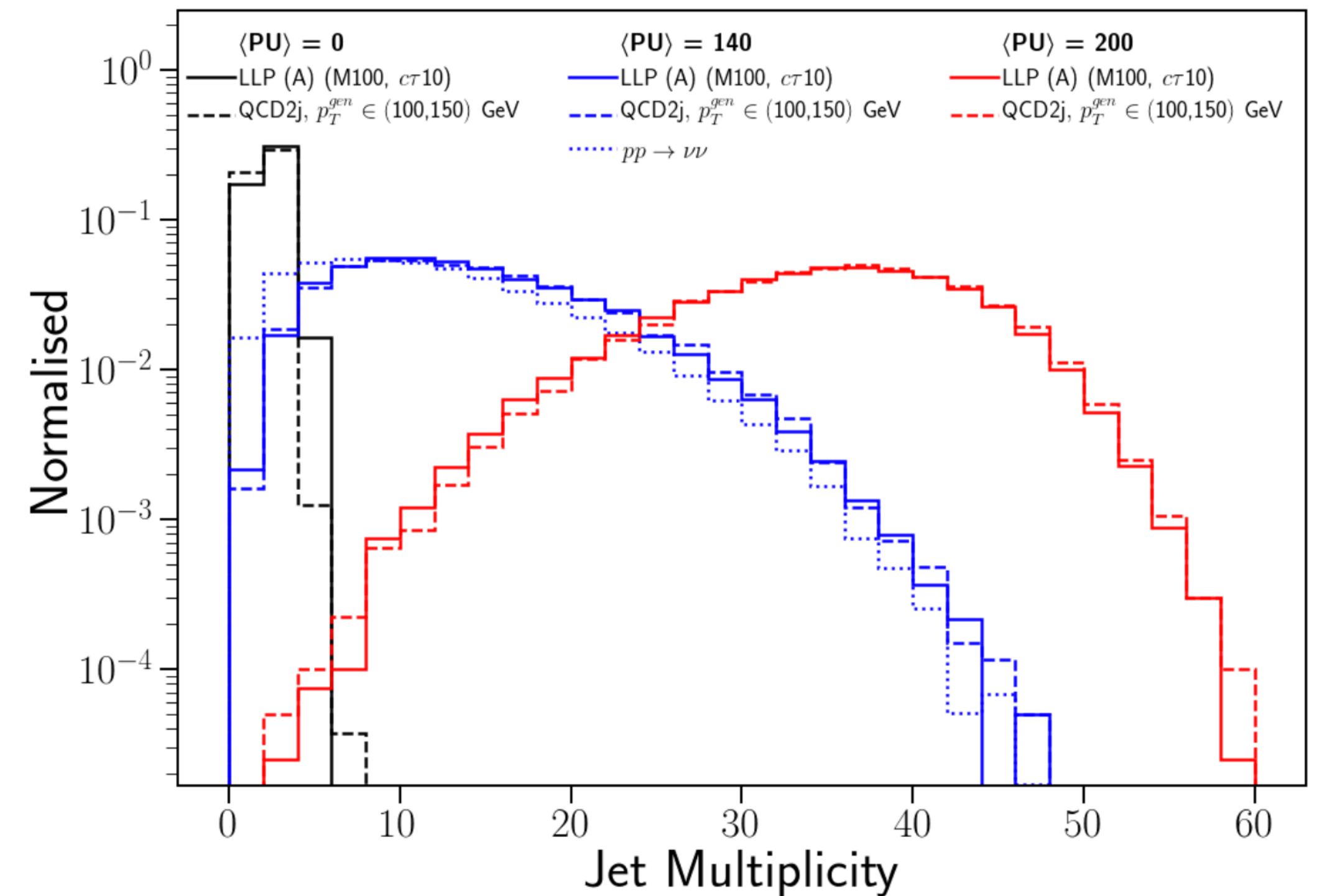
Jets@HL-LHC

Number of jets increases with PU



REF:CMS L1 TDR 2020

LLP Model: $pp \rightarrow XX, X \rightarrow q\bar{q}$



Jet info
Jet parameter = 0.4
 $p_T > 60$ GeV
 $|\eta| < 2.5$

BB, Swagata Mukherjee, Rhitaja Sengupta, Prabhat Solanki e-Print: 2003.03943, JHEP 2020

Event rates

Inelastic events : 10^9 Hz (cross section 100 mb)

W Events : (Cross section)

Top quark Events: (Cross section ~ 1000 pb)

Higgs Events : (cross section ~ 50 pb)

New Physics Rate : (Cross section 1 fb)

Event selection should be sensitive at $1: 10^{11}$ level

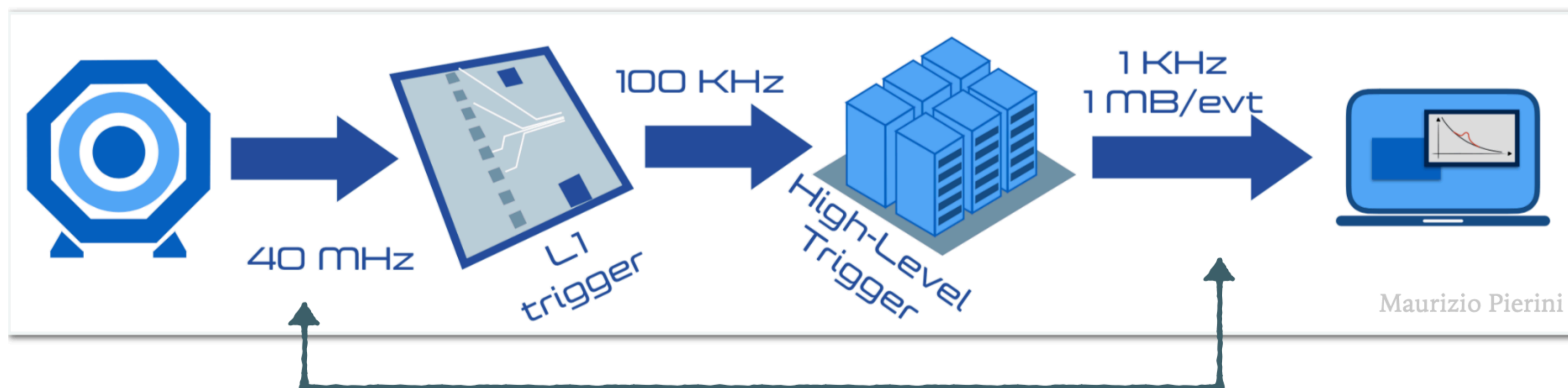
Dedicated selection conditions required to select a few interesting events => Trigger

Trigger system in CMS

Level I (L1) Trigger : Coarse Granularity, Hardware based, fast decision (3 micro second), Output 100 KHz

High Level Trigger (HLT) : Full Granularity, Software based, avg time req:300 milli second, Output 1 KHz

Low or **zero** sensitivity to new physics with low-mass.



Taken from Swagata Mukherjee's talk

<https://indico.cern.ch/event/1182683/attachments/2518736/4330705/7August.pdf>

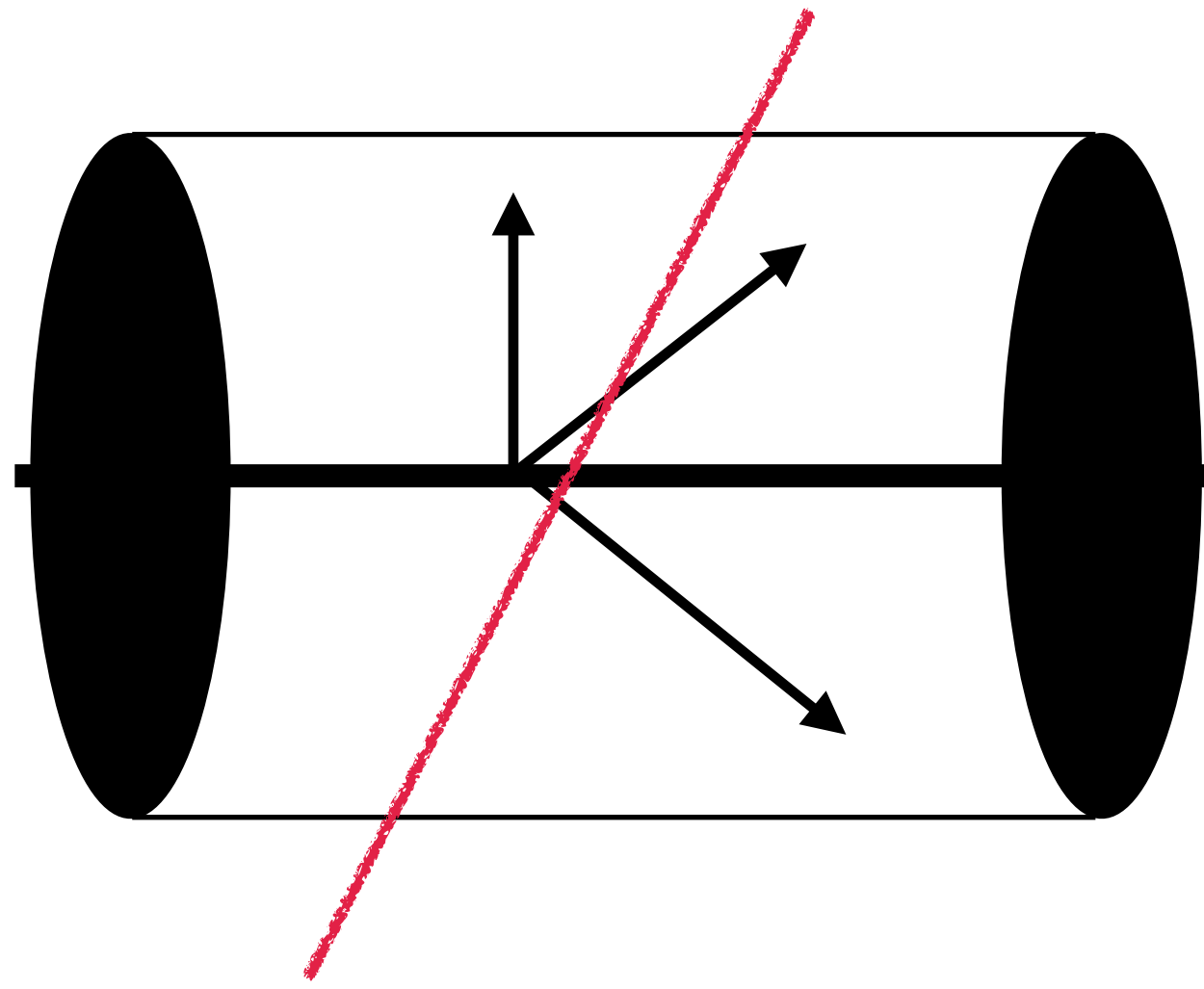
Trigger Menu@ HL-LHC(PU=200)

L1 Trigger seeds	Offline Threshold(s) at 90% or 95% (50%) [GeV]	Rate $\langle PU \rangle = 200$ [kHz]	Additional Requirement(s) [cm, GeV]	Objects plateau efficiency [%]
Single/Double/Triple Lepton (electron, muon) seeds				
Single TkMuon	22	12	$ \eta < 2.4$	95
Double TkMuon	15,7	1	$ \eta < 2.4, \Delta z < 1$	95
Triple TkMuon	5,3,3	16	$ \eta < 2.4, \Delta z < 1$	95
Single TkElectron	36	24	$ \eta < 2.4$	93
Single TkIsoElectron	28	28	$ \eta < 2.4$	93
TkIsoElectron-StaEG	22, 12	36	$ \eta < 2.4$	93, 99
Double TkElectron	25, 12	4	$ \eta < 2.4$	93
Single StaEG	51	25	$ \eta < 2.4$	99
Double StaEG	37,24	5	$ \eta < 2.4$	99
Photon seeds				
Single TkIsoPhoton	36	43	$ \eta < 2.4$	97
Double TkIsoPhoton	22, 12	50	$ \eta < 2.4$	97
Taus seeds				
Single CaloTau	150(119)	21	$ \eta < 2.1$	99
Double CaloTau	90,90(69,69)	25	$ \eta < 2.1, \Delta R > 0.5$	99
Double PuppiTau	52,52(36,36)	7	$ \eta < 2.1, \Delta R > 0.5$	90
Hadronic seeds (jets, H_T)				
Single PuppiJet	180	70	$ \eta < 2.4$	100
Double PuppiJet	112,112	71	$ \eta < 2.4, \Delta\eta < 1.6$	100
Puppi H_T	450(377)	11	jets: $ \eta < 2.4, p_T > 30$	100
QuadPuppiJets-Puppi H_T	70,55,40,40,400(328)	9	jets: $ \eta < 2.4, p_T > 30$	100,100
E_T^{miss} seeds				
Puppi E_T^{miss}	200(128)	18		100

REF: CMS L1 TDR 2020

More and More backgrounds

Non Collisional: Some trigger fired and a cosmic muon can pass the detector at the same time



If it passes through the both hemisphere of the detector it will be identified as two back to back muons

Removal: impact parameter cut, timing cut and angular cut between two muons

Beam halo: Collision of proton beam with some part of the LHC part, mostly collimator (required to clean stray particles)

Beam Gas: Collision of proton beam with gas molecule inside the beam pipe (both elastic and inelastic)

Detector induced: Some parts of the detector may not work or misfire => change the 4 momentum measurements Of the particles or generate missing energy signal

Dedicated efforts are required to understand to mitigate such backgrounds